

# Computer algebra independent integration tests

1-Algebraic-functions/1.1-Binomial-products/1.1.3-General/1.1.3.6-g-x-  
 $^m-a+b-x^n-^p-c+d-x^n-^q-e+f-x^n-^r$

Nasser M. Abbasi

September 20, 2021

Compiled on September 20, 2021 at 5:22am

## Contents

<b>1</b>	<b>Introduction</b>	<b>3</b>
<b>2</b>	<b>detailed summary tables of results</b>	<b>17</b>
<b>3</b>	<b>Listing of integrals</b>	<b>25</b>
<b>4</b>	<b>Appendix</b>	<b>121</b>



# Chapter 1

## Introduction

### Local contents

1.1	Listing of CAS systems tested . . . . .	4
1.2	Results . . . . .	5
1.3	Performance . . . . .	8
1.4	list of integrals that has no closed form antiderivative . . . . .	10
1.5	list of integrals solved by CAS but has no known antiderivative . . . . .	11
1.6	list of integrals solved by CAS but failed verification . . . . .	12
1.7	Timing . . . . .	12
1.8	Verification . . . . .	13
1.9	Important notes about some of the results . . . . .	13
1.10	Design of the test system . . . . .	15

This report gives the result of running the computer algebra independent integration test. Elementary Algebraic integrals version.

The download section below contains links to download the problems in plain text format used for all CAS systems.

The number of integrals in this report is [ 12 ]. This is test number [ 15 ].

## 1.1 Listing of CAS systems tested

The following systems were tested at this time.

1. Mathematica 12.3.1 (64 bit) on windows 10.
2. Rubi 4.16.1 in Mathematica 12.3.1 on windows 10.
3. Maple 2021.1 (64 bit) on windows 10.
4. Maxima 5.45 on Linux. (via sagemath 9.3)
5. Fricas 1.3.7 on Linux (via sagemath 9.3)
6. Giac/Xcas 1.7 on Linux. (via sagemath 9.3)
7. Sympy 1.8 under Python 3.8.8 using Anaconda distribution on Ubuntu.
8. Mupad using Matlab 2021a with Symbolic Math Toolbox Version 8.7 under windows 10 (64 bit)
9. IntegrateAlgebraic under Mathematica 12.3.1 on windows 10. [https://github.com/stblake/algebraic\\_integration](https://github.com/stblake/algebraic_integration). September 15, 2021 version.

Maxima, Fricas and Giac/Xcas were called from inside SageMath. This was done using SageMath integrate command by changing the name of the algorithm to use the different CAS systems.

Sympy was called directly using Python.

## 1.2 Results

Important note: A number of problems in this test suite have no antiderivative in closed form. This means the antiderivative of these integrals can not be expressed in terms of elementary, special functions or Hypergeometric2F1 functions. RootSum and RootOf are not allowed.

If a CAS returns the above integral unevaluated within the time limit, then the result is counted as passed and assigned an A grade.

However, if CAS times out, then it is assigned an F grade even if the integral is not integrable, as this implies CAS could not determine that the integral is not integrable in the time limit.

If a CAS returns an antiderivative to such an integral, it is assigned an A grade automatically and this special result is listed in the introduction section of each individual test report to make it easy to identify as this can be important result to investigate.

The results given in in the table below reflects the above.

System	% solved	% Failed
Rubi	100.00 ( 12 )	0.00 ( 0 )
Mathematica	100.00 ( 12 )	0.00 ( 0 )
Fricas	100.00 ( 12 )	0.00 ( 0 )
Maple	100.00 ( 12 )	0.00 ( 0 )
Mupad	100.00 ( 12 )	0.00 ( 0 )
Maxima	100.00 ( 12 )	0.00 ( 0 )
Giac	91.67 ( 11 )	8.33 ( 1 )
Sympy	25.00 ( 3 )	% 75.00 ( 9 )
IntegrateAlgebraic	0.00 ( 0 )	100.00 ( 12 )

Table 1.1: Percentage solved for each CAS

The table below gives additional break down of the grading of quality of the antiderivatives generated by each CAS. The grading is given using the letters A,B,C and F with A being the best quality. The grading is accomplished by comparing the antiderivative generated with the optimal antiderivatives included in the test suite. The following table describes the meaning of these grades.

grade	description
A	Integral was solved and antiderivative is optimal in quality and leaf size.
B	Integral was solved and antiderivative is optimal in quality but leaf size is larger than twice the optimal antiderivatives leaf size.
C	Integral was solved and antiderivative is non-optimal in quality. This can be due to one or more of the following reasons <ol style="list-style-type: none"> <li>1. antiderivative contains a hypergeometric function and the optimal antiderivative does not.</li> <li>2. antiderivative contains a special function and the optimal antiderivative does not.</li> <li>3. antiderivative contains the imaginary unit and the optimal antiderivative does not.</li> </ol>
F	Integral was not solved. Either the integral was returned unevaluated within the time limit, or it timed out, or CAS hanged or crashed or an exception was raised.

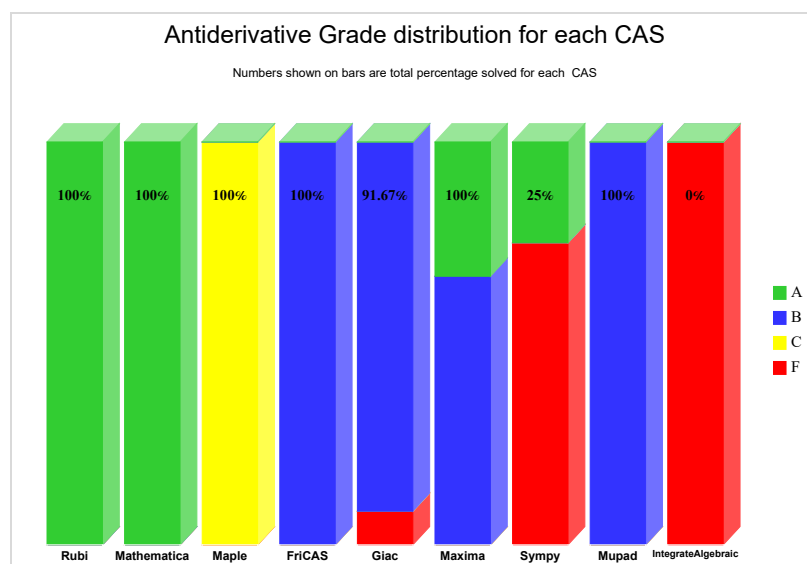
Table 1.2: Description of grading applied to integration result

Grading is implemented for all CAS systems. Based on the above, the following table summarizes the grading for this test suite.

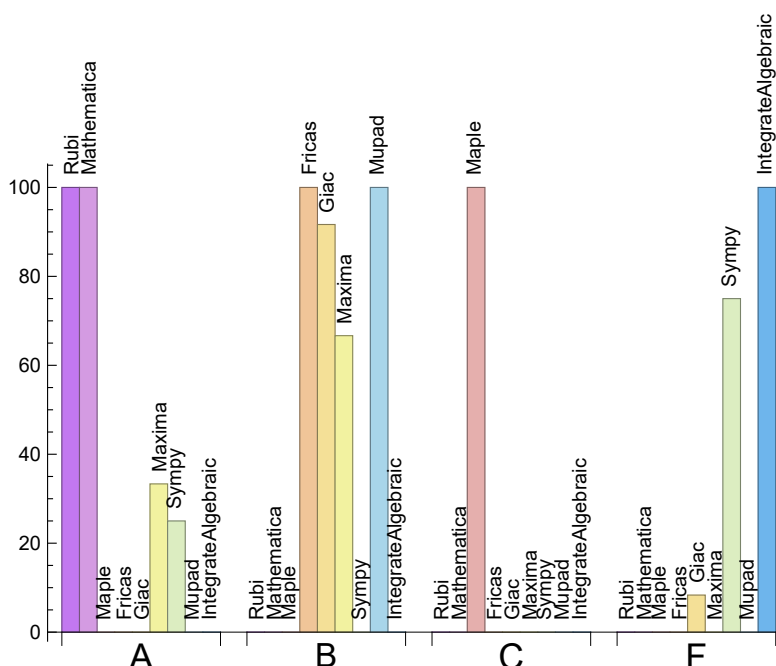
System	% A grade	% B grade	% C grade	% F grade
Rubi	100.00	0.00	0.00	0.00
Mathematica	100.00	0.00	0.00	0.00
Maxima	33.33	66.67	0.00	0.00
Sympy	25.00	0.00	0.00	75.00
Fricas	0.00	100.00	0.00	0.00
Maple	0.00	0.00	100.00	0.00
IntegrateAlgebraic	0.00	0.00	0.00	100.00
Mupad	N/A	100.00	0.00	0.00
Giac	0.00	91.67	0.00	8.33

Table 1.3: Antiderivative Grade distribution of each CAS

The following is a Bar chart illustration of the data in the above table.



The figure below compares the CAS systems for each grade level.



The following table shows the distribution of the different types of failure for each CAS. There are 3 types of reasons why it can fail. The first is when CAS returns back the input within the time limit, which means it could not solve it. This is the typical normal failure **F**.

The second is due to time out. CAS could not solve the integral within the 3 minutes time limit which is assigned **F(-1)**.

The third is due to an exception generated. Assigned **F(-2)**. This most likely indicates an interface problem between sagemath and the CAS (applicable only to FriCAS, Maxima and Giac) or it could be an indication of an internal error in CAS. This type of error requires more investigations to determine the cause.

System	Number failed	Percentage normal failure	Percentage time-out failure	Percentage exception failure
Rubi	0	0.00 %	0.00 %	0.00 %
Mathematica	0	0.00 %	0.00 %	0.00 %
Maple	0	0.00 %	0.00 %	0.00 %
Fricas	0	0.00 %	0.00 %	0.00 %
IntegrateAlgebraic	12	100.00 %	0.00 %	0.00 %
Giac	1	0.00 %	100.00 %	0.00 %
Maxima	0	0.00 %	0.00 %	0.00 %
Sympy	9	0.00 %	100.00 %	0.00 %
Mupad	0	0.00 %	0.00 %	0.00 %

Table 1.4: Failure statistics for each CAS

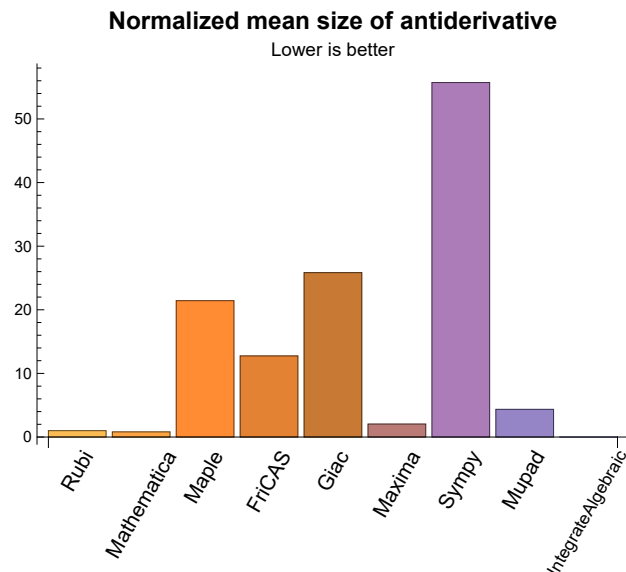
### 1.3 Performance

The table below summarizes the performance of each CAS system in terms of CPU time and leaf size of results.

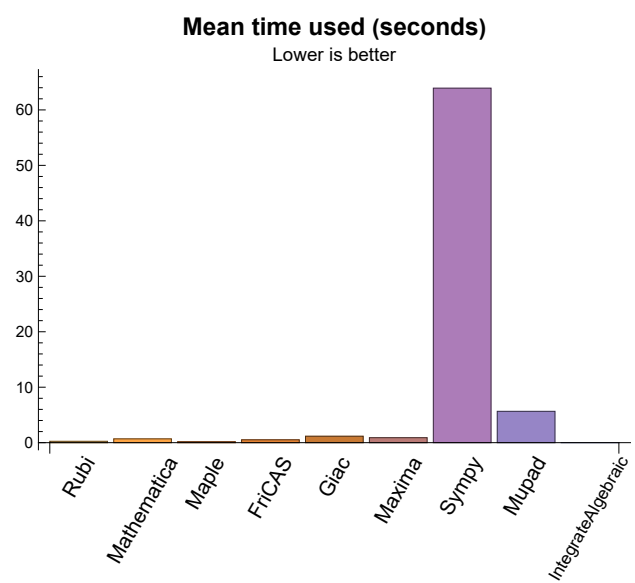
System	Mean time (sec)	Mean size	Normalized mean	Median size	Normalized median
Rubi	0.25	202.33	1.00	185.00	1.00
Mathematica	0.69	167.83	0.81	150.50	0.81
Maple	0.18	5656.75	21.43	3691.00	19.37
Maxima	0.90	443.75	2.04	398.00	2.14
Fricas	0.52	3297.67	12.75	2178.50	11.51
Sympy	63.92	5532.33	55.72	6399.00	62.74
Giac	1.16	5856.45	25.84	3415.00	21.34
Mupad	5.65	1031.33	4.35	838.50	4.42
IntegrateAlgebraic	0.00	0.00	0.00	0.00	0.00

Table 1.5: Time and leaf size performance for each CAS

The following are bar charts for the normalized leafsize and time used columns from the above table.







## 1.4 list of integrals that has no closed form antiderivative

{

## 1.5 list of integrals solved by CAS but has no known antiderivative

Rubi {}

Mathematica {}

Maple {}

Maxima {}

Fricas {}

Sympy {}

Giac {}

Mupad {}

IntegrateAlgebraic {}

## 1.6 list of integrals solved by CAS but failed verification

The following are integrals solved by CAS but the verification phase failed to verify the anti-derivative produced is correct. This does not mean necessarily that the anti-derivative is wrong, as additional methods of verification might be needed, or more time is needed (3 minutes time limit was used). These integrals are listed here to make it easier to do further investigation to determine why it was not possible to verify the result produced.

**Rubi** {}

**Mathematica** {}

**IntegrateAlgebraic** {}

**Maple** Verification phase not implemented yet.

**Maxima** Verification phase not implemented yet.

**Fricas** Verification phase not implemented yet.

**Sympy** Verification phase not implemented yet.

**Giac** Verification phase not implemented yet.

**Mupad** Verification phase not implemented yet.

## 1.7 Timing

The command `AbsoluteTiming[]` was used in Mathematica to obtain the elapsed time for each integrate call. In Maple, the command `Usage` was used as in the following example

```
cpu_time := Usage(assign ('result_of _int',int(expr,x)),output='realtime')
```

For all other CAS systems, the elapsed time to complete each integral was found by taking the difference between the time after the call has completed from the time before the call was made. This was done using Python's `time.time()` call.

All elapsed times shown are in seconds. A time limit of 3 minutes was used for each integral. If the integrate command did not complete within this time limit, the integral was aborted and considered to have failed and assigned an F grade. The time used by failed integrals due to time out is not counted in the final statistics.

## 1.8 Verification

A verification phase was applied on the result of integration for Rubi and Mathematica. Future version of this report will implement verification for the other CAS systems. For the integrals whose result was not run through a verification phase, it is assumed that the antiderivative produced was correct.

Verification phase has 3 minutes time out. An integral whose result was not verified could still be correct. Further investigation is needed on those integrals which failed verifications. Such integrals are marked in the summary table below and also in each integral separate section so they are easy to identify and locate.

## 1.9 Important notes about some of the results

### 1.9.1 Important note about Maxima results

Since these integrals are run in a batch mode, using an automated script, and by using sagemath (SageMath uses Maxima), then any integral where Maxima needs an interactive response from the user to answer a question during evaluation of the integral in order to complete the integration, will fail and is counted as failed.

The exception raised is `ValueError`. Therefore Maxima result below is lower than what could result if Maxima was run directly and each question Maxima asks was answered correctly.

The percentage of such failures were not counted for each test file, but for an example, for the Timofeev test file, there were about 14 such integrals out of total 705, or about 2 percent. This percentage can be higher or lower depending on the specific input test file.

Such integrals can be indentified by looking at the output of the integration in each section for Maxima. The exception message will indicate of the error is due to the interactive question being asked or not.

Maxima integrate was run using SageMath with the following settings set by default

```
'besselexpand : true'
'display2d : false'
'domain : complex'
'keepfloat : true'
'load(to_poly_solve)'
'load(simplify_sum)'
'load(abs_integrate)' 'load(diag)'
```

SageMath loading of Maxima `abs_integrate` was found to cause some problem. So the following code was added to disable this effect.

```
from sage.interfaces.maxima_lib import maxima_lib
maxima_lib.set('extra_definite_integration_methods', '[]')
maxima_lib.set('extra_integration_methods', '[]')
```

See <https://ask.sagemath.org/question/43088/integrate-results-that-are-different-from-using-maxima/> for reference.

### 1.9.2 Important note about FriCAS and Giac/XCAS results

There are Few integrals which failed due to SageMath not able to translate the result back to SageMath syntax and not because these CAS system were not able to do the integrations.

These will fail With error Exception raised: NotImplementedError

The number of such cases seems to be very small. About 1 or 2 percent of all integrals.

Hopefully the next version of SageMath will have complete translation of FriCAS and XCAS syntax and I will re-run all the tests again when this happens.

### 1.9.3 Important note about finding leaf size of antiderivative

For Mathematica, Rubi and Maple, the builtin system function LeafSize is used to find the leaf size of each antiderivative.

The other CAS systems (SageMath and Sympy) do not have special builtin function for this purpose at this time. Therefore the leaf size for Fricas and Sympy and Giac antiderivatives is determined using the following function, thanks to user slelievre at [https://ask.sagemath.org/question/57123/could-we-have-a-leaf\\_count-function-in-base-sagemath/](https://ask.sagemath.org/question/57123/could-we-have-a-leaf_count-function-in-base-sagemath/)

```
def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)
```

For Sympy, which is called directly from Python, the following code is used to obtain the leafsize of its result

```
try:
    # 1.7 is a fudge factor since it is low side from actual leaf count
    leafCount = round(1.7*count_ops(anti))

except Exception as ee:
    leafCount =1
```

### 1.9.4 Important note about Mupad results

Matlab's symbolic toolbox does not have a leaf count function to measure the size of the antiderivative, Maple was used to determine the leaf size of Mupad output by post processing.

Currently no grading of the antiderivative for Mupad is implemented. If it can integrate the problem, it was assigned a B grade automatically as a placeholder. In the future, when grading function is implemented for Mupad, the tests will be rerun again.

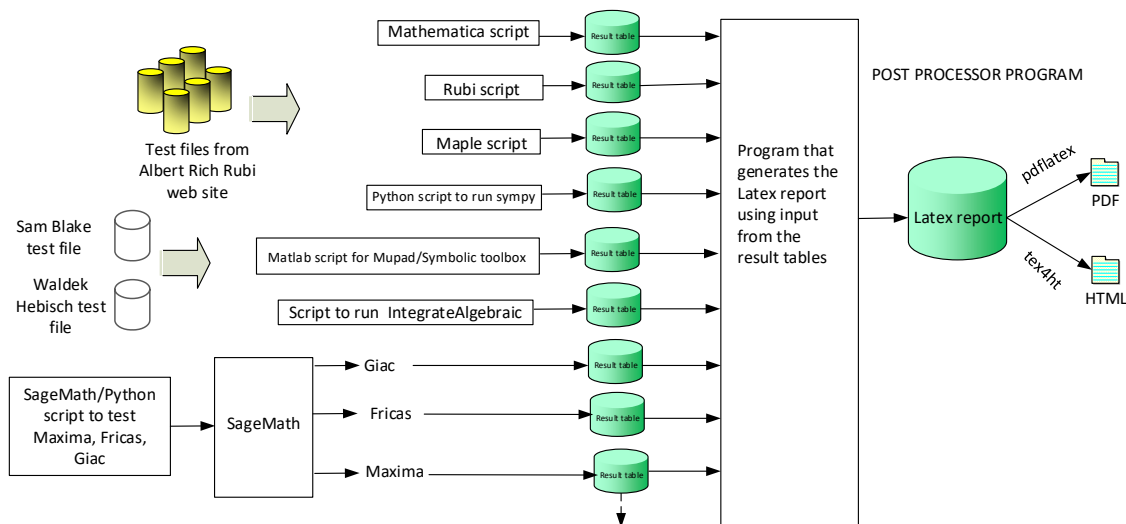
The following is an example of using Matlab's symbolic toolbox (Mupad) to solve an integral

```
integrand = evalin(symengine, 'cos(x)*sin(x)')
the_variable = evalin(symengine, 'x')
anti = int(integrand, the_variable)
```

Which gives  $\sin(x)^{2/2}$

## 1.10 Design of the test system

The following diagram gives a high level view of the current test build system.



**One record (line) per one integral result. The line is CSV comma separated. This is description of each record**

1. integer. the problem number.
2. integer. 0 for failed, 1 for passed, -1 for timeout, -2 for CAS specific exception. (this is not the grade field)
3. integer. Leaf size of result.
4. integer. Leaf size of the optimal antiderivative.
5. number. CPU time used to solve this integral. 0 if failed.
6. string. The integral in Latex format
7. string. The input used in CAS own syntax.
8. string. The result (antiderivative) produced by CAS in Latex format
9. string. The optimal antiderivative in Latex format.
10. integer. 0 or 1. Indicates if problem has known antiderivative or not
11. String. The result (antiderivative) in CAS own syntax.
12. String. The grade of the antiderivative. Can be "A", "B", "C", or "F"  
*The following field present only in Rubi and Mathematica Tables*
13. integer. 1 if result was verified or 0 if not verified.  
*The following fields present only in Rubi Tables*
14. integer. Number of rules used.
15. integer. Integrand leaf size.
16. real number. Ratio of field 14 over field 15
17. integer. 1 if result was verified or 0 if not verified.
18. String of form "{n,n,...}" which is list of the rules used by Rubi

**High level overview of the CAS independent integration test build system**





# Chapter 2

## detailed summary tables of results

### Local contents

2.1	List of integrals sorted by grade for each CAS . . . . .	18
2.2	Detailed conclusion table per each integral for all CAS systems . . . . .	21
2.3	Detailed conclusion table specific for Rubi results . . . . .	24

## 2.1 List of integrals sorted by grade for each CAS

### Local contents

2.1.1	Rubi	19
2.1.2	Mathematica	19
2.1.3	Maple	19
2.1.4	Maxima	19
2.1.5	FriCAS	19
2.1.6	Sympy	19
2.1.7	Giac	20
2.1.8	Mupad	20
2.1.9	IntegrateAlgebraic	20

### 2.1.1 Rubi

A grade: { 1,2,3,4,5,6,7,8,9,10,11,12 }

B grade: { }

C grade: { }

F grade: { }

### 2.1.2 Mathematica

A grade: { 1,2,3,4,5,6,7,8,9,10,11,12 }

B grade: { }

C grade: { }

F grade: { }

### 2.1.3 Maple

A grade: { }

B grade: { }

C grade: { 1,2,3,4,5,6,7,8,9,10,11,12 }

F grade: { }

### 2.1.4 Maxima

A grade: { 3,4,8,12 }

B grade: { 1,2,5,6,7,9,10,11 }

C grade: { }

F grade: { }

### 2.1.5 FriCAS

A grade: { }

B grade: { 1,2,3,4,5,6,7,8,9,10,11,12 }

C grade: { }

F grade: { }

### 2.1.6 Sympy

A grade: { 3,4,8 }

B grade: { }

C grade: { }

F grade: { 1,2,5,6,7,9,10,11,12 }

### 2.1.7 Giac

A grade: { }

B grade: { 1, 2, 3, 4, 5, 6, 7, 8, 10, 11, 12 }

C grade: { }

F grade: { 9 }

### 2.1.8 Mupad

A grade: { }

B grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12 }

C grade: { }

F grade: { }

### 2.1.9 IntegrateAlgebraic

A grade: { }

B grade: { }

C grade: { }

F grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12 }

## 2.2 Detailed conclusion table per each integral for all CAS systems

Detailed conclusion table per each integral is given by table below. The elapsed time is in seconds. For failed result it is given as F(-1) if the failure was due to timeout. It is given as F(-2) if the failure was due to an exception being raised, which could indicate a bug in the system. If the failure was due to integral not being evaluated within the time limit, then it is given just an F.

In this table, the column N.S. in the table below, which stands for **normalized size** is defined as  $\frac{\text{antiderivative leaf size}}{\text{optimal antiderivative leaf size}}$ . To help make the table fit, Mathematica was abbreviated to MMA and IntegrateAlgebraic to I.A.

Problem 1	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	B	B	F(-1)	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	210	210	172	4972	464	3073	0	6927	1089	0
N.S.	1	1.00	0.82	23.68	2.21	14.63	0.00	32.99	5.19	0.00
time (sec)	N/A	0.270	0.994	0.211	0.936	0.578	0.000	1.191	5.644	0.653
Problem 2	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	B	B	F(-1)	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	160	160	129	2410	332	1524	0	3415	588	0
N.S.	1	1.00	0.81	15.06	2.08	9.52	0.00	21.34	3.68	0.00
time (sec)	N/A	0.176	0.525	0.138	0.861	0.490	0.000	0.809	5.231	0.168
Problem 3	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	A	B	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	108	108	84	891	200	562	8500	1290	271	0
N.S.	1	1.00	0.78	8.25	1.85	5.20	78.70	11.94	2.51	0.00
time (sec)	N/A	0.084	0.247	0.109	0.697	0.452	88.266	1.796	4.958	0.114
Problem 4	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	A	B	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	66	66	49	262	91	185	1698	327	91	0
N.S.	1	1.00	0.74	3.97	1.38	2.80	25.73	4.95	1.38	0.00
time (sec)	N/A	0.040	0.067	0.117	0.598	0.440	29.325	0.455	4.830	0.067
Problem 5	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	B	B	F(-1)	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	318	318	273	11389	748	6638	0	15358	1882	0
N.S.	1	1.00	0.86	35.81	2.35	20.87	0.00	48.30	5.92	0.00
time (sec)	N/A	0.411	1.478	0.226	1.119	0.584	0.000	2.013	6.348	0.865

Problem 6	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	B	B	F(-1)	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	237	237	199	5908	540	3515	0	8103	1119	0
N.S.	1	1.00	0.84	24.93	2.28	14.83	0.00	34.19	4.72	0.00
time (sec)	N/A	0.310	0.605	0.171	0.905	0.506	0.000	2.006	5.591	0.303
Problem 7	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	B	B	F(-1)	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	160	160	129	2410	332	1426	0	3415	588	0
N.S.	1	1.00	0.81	15.06	2.08	8.91	0.00	21.34	3.68	0.00
time (sec)	N/A	0.172	0.313	0.144	0.782	0.484	0.000	0.818	5.196	0.161
Problem 8	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	A	B	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	102	102	78	732	155	527	6399	1023	265	0
N.S.	1	1.00	0.76	7.18	1.52	5.17	62.74	10.03	2.60	0.00
time (sec)	N/A	0.076	0.175	0.109	0.634	0.450	74.164	0.582	5.113	0.097
Problem 9	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	B	B	F(-1)	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	410	410	358	20937	1032	11628	0	0	2949	0
N.S.	1	1.00	0.87	51.07	2.52	28.36	0.00	0.00	7.19	0.00
time (sec)	N/A	0.624	1.430	0.344	1.467	0.735	0.000	0.000	7.495	1.251
Problem 10	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	B	B	F(-1)	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	310	310	265	11389	748	6557	0	15358	1882	0
N.S.	1	1.00	0.85	36.74	2.41	21.15	0.00	49.54	6.07	0.00
time (sec)	N/A	0.414	1.520	0.249	0.923	0.576	0.000	1.303	6.414	1.011
Problem 11	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	B	B	F(-1)	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	210	210	172	4972	464	2833	0	6927	1089	0
N.S.	1	1.00	0.82	23.68	2.21	13.49	0.00	32.99	5.19	0.00
time (sec)	N/A	0.258	0.753	0.178	1.008	0.505	0.000	1.057	5.653	0.645

Problem 12	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad	I.A.
grade	A	A	A	C	A	B	F(-1)	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD	Yes
size	137	137	106	1609	219	1104	0	2278	563	0
N.S.	1	1.00	0.77	11.74	1.60	8.06	0.00	16.63	4.11	0.00
time (sec)	N/A	0.111	0.177	0.126	0.845	0.466	0.000	0.750	5.307	0.111

## 2.3 Detailed conclusion table specific for Rubi results

The following table is specific to Rubi. It gives additional statistics for each integral. the column **steps** is the number of steps used by Rubi to obtain the antiderivative. The **rules** column is the number of unique rules used. The **integrand size** column is the leaf size of the integrand. Finally the ratio  $\frac{\text{number of rules}}{\text{integrand size}}$  is given. The larger this ratio is, the harder the integral was to solve. In this test, problem number [4] had the largest ratio of [.1500]

Table 2.1: Rubi specific breakdown of results for each integral

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1	A	12	3	1.00	29	0.103
2	A	10	3	1.00	29	0.103
3	A	8	3	1.00	27	0.111
4	A	6	3	1.00	20	0.150
5	A	14	3	1.00	31	0.097
6	A	12	3	1.00	31	0.097
7	A	10	3	1.00	29	0.103
8	A	8	3	1.00	22	0.136
9	A	16	3	1.00	31	0.097
10	A	14	3	1.00	31	0.097
11	A	12	3	1.00	29	0.103
12	A	10	3	1.00	22	0.136



# Chapter 3

## Listing of integrals

### Local contents

3.1	$\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n) dx$	26
3.2	$\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n) dx$	35
3.3	$\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n) dx$	41
3.4	$\int (ex)^m (A + Bx^n) (c + dx^n) dx$	49
3.5	$\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^2 dx$	53
3.6	$\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^2 dx$	65
3.7	$\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^2 dx$	73
3.8	$\int (ex)^m (A + Bx^n) (c + dx^n)^2 dx$	79
3.9	$\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^3 dx$	85
3.10	$\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^3 dx$	94
3.11	$\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^3 dx$	106
3.12	$\int (ex)^m (A + Bx^n) (c + dx^n)^3 dx$	115

### 3.1 $\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n) dx$

**Optimal.** Leaf size=210

$$\frac{a^3 Ac(ex)^{m+1}}{e(m+1)} + \frac{a^2 x^{n+1}(ex)^m (aAd + aBc + 3Abc)}{m+n+1} + \frac{b^2 x^{4n+1}(ex)^m (3aBd + Abd + bBc)}{m+4n+1} + \frac{ax^{2n+1}(ex)^m (3Ab(ad+bc) + aB(ad+3bc))}{m+2n+1} + \frac{b^3 Bdx^{5n+1}(ex)^m}{m+5n+1}$$

**Rubi [A]** time = 0.27, antiderivative size = 210, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ , Rules used = {570, 20, 30}

$$\frac{a^2 x^{n+1}(ex)^m (aAd + aBc + 3Abc)}{m+n+1} + \frac{a^3 Ac(ex)^{m+1}}{e(m+1)} + \frac{b^2 x^{4n+1}(ex)^m (3aBd + Abd + bBc)}{m+4n+1} + \frac{ax^{2n+1}(ex)^m (3Ab(ad+bc) + aB(ad+3bc))}{m+2n+1} + \frac{bx^{3n+1}(ex)^m (Ab(3ad+bc) + 3aB(ad+bc))}{m+3n+1} + \frac{b^3 Bdx^{5n+1}(ex)^m}{m+5n+1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n), x]

[Out] (a^2\*(3\*A\*b\*c + a\*B\*c + a\*A\*d)\*x^(1 + n)\*(e\*x)^m)/(1 + m + n) + (a\*(3\*A\*b\*(b\*c + a\*d) + a\*B\*(3\*b\*c + a\*d))\*x^(1 + 2\*n)\*(e\*x)^m)/(1 + m + 2\*n) + (b\*(3\*a\*B\*(b\*c + a\*d) + A\*b\*(b\*c + 3\*a\*d))\*x^(1 + 3\*n)\*(e\*x)^m)/(1 + m + 3\*n) + (b^2\*(b\*B\*c + A\*b\*d + 3\*a\*B\*d)\*x^(1 + 4\*n)\*(e\*x)^m)/(1 + m + 4\*n) + (b^3\*B\*d\*x^(1 + 5\*n)\*(e\*x)^m)/(1 + m + 5\*n) + (a^3\*A\*c\*(e\*x)^(1 + m))/(e\*(1 + m))

#### Rule 20

Int[(u\_)\*((a\_)\*(v\_))^(m\_)\*((b\_)\*(v\_))^(n\_), x\_Symbol] := Dist[(b^IntPart[n]\*(b\*v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

#### Rule 30

Int[(x\_)^(m\_), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]

#### Rule 570

Int[((g\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_)\*((e\_) + (f\_)\*(x\_)^(n\_))^(r\_), x\_Symbol] := Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

#### Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n) dx &= \int (a^3 Ac(ex)^m + a^2(3Abc + aBc + aAd)x^n(ex)^m + a(3Ab(bc + ad) + aB(3bc + ad))x^{2n}(ex)^m + (b^3 Bd)x^{4n}(ex)^m + (b^3 Bdx^{5n})(ex)^m) dx \\ &= \frac{a^3 Ac(ex)^{1+m}}{e(1+m)} + (b^3 Bd) \int x^{5n}(ex)^m dx + (a^2(3Abc + aBc + aAd)) \int x^{2n}(ex)^m dx \\ &= \frac{a^3 Ac(ex)^{1+m}}{e(1+m)} + (b^3 Bdx^{-m}(ex)^m) \int x^{m+5n} dx + (a^2(3Abc + aBc + aAd)) \int x^{m+n} dx \\ &= \frac{a^2(3Abc + aBc + aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{a(3Ab(bc + ad) + aB(3bc + ad))x^{1+n}(ex)^m}{1+m+2n} \end{aligned}$$

**Mathematica [A]** time = 0.99, size = 172, normalized size = 0.82

$$x(ex)^m \left( \frac{a^3 Ac}{m+1} + \frac{a^2 x^n (aAd + aBc + 3Abc)}{m+n+1} + \frac{b^2 x^{4n} (3aBd + Abd + bBc)}{m+4n+1} + \frac{ax^{2n} (3Ab(ad+bc) + aB(ad+3bc))}{m+2n+1} + \frac{bx^{3n} (Ab(3ad+bc) + 3aB(ad+bc))}{m+3n+1} + \frac{b^3 Bdx^{5n}}{m+5n+1} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n),x]

[Out]  $x*(e*x)^m*((a^3*A*c)/(1+m) + (a^2*(3*A*b*c + a*B*c + a*A*d)*x^n)/(1+m+n) + (a*(3*A*b*(b*c + a*d) + a*B*(3*b*c + a*d))*x^{2*n})/(1+m+2*n) + (b*(3*a*B*(b*c + a*d) + A*b*(b*c + 3*a*d))*x^{3*n})/(1+m+3*n) + (b^2*(b*B*c + A*b*d + 3*a*B*d)*x^{4*n})/(1+m+4*n) + (b^3*B*d*x^{5*n})/(1+m+5*n))$

**IntegrateAlgebraic [F]** time = 0.65, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n) dx$$

Verification is not applicable to the result.

[In] IntegrateAlgebraic[(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n),x]

[Out] Defer[IntegrateAlgebraic] [(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n), x]

**fricas [B]** time = 0.58, size = 3073, normalized size = 14.63

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="fricas")

[Out]  $((B*b^3*d*m^5 + 5*B*b^3*d*m^4 + 10*B*b^3*d*m^3 + 10*B*b^3*d*m^2 + 5*B*b^3*d*m + B*b^3*d + 24*(B*b^3*d*m + B*b^3*d)*n^4 + 50*(B*b^3*d*m^2 + 2*B*b^3*d*m + B*b^3*d)*n^3 + 35*(B*b^3*d*m^3 + 3*B*b^3*d*m^2 + 3*B*b^3*d*m + B*b^3*d)*n^2 + 10*(B*b^3*d*m^4 + 4*B*b^3*d*m^3 + 6*B*b^3*d*m^2 + 4*B*b^3*d*m + B*b^3*d)*n)*x*x^{5*n}*e^{(m*\log(e) + m*\log(x))} + ((B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^5 + B*b^3*c + 5*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^4 + 30*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d + (B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m)*n^4 + 10*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^3 + 61*(B*b^3*c + (B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^2 + (3*B*a*b^2 + A*b^3)*d + 2*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m)*n^3 + 10*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^2 + 41*(B*b^3*c + (B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^3 + 3*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^2 + (3*B*a*b^2 + A*b^3)*d + 3*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m)*n^2 + (3*B*a*b^2 + A*b^3)*d + 5*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m + 11*(B*b^3*c + (B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^4 + 4*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^3 + 6*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^2 + (3*B*a*b^2 + A*b^3)*d + 4*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m)*n)*x*x^{4*n}*e^{(m*\log(e) + m*\log(x))} + (((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^5 + 5*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^4 + 40*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d + ((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m)*n^4 + 10*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^3 + 78*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^2 + (3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d + 2*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m)*n^3 + 10*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^2 + 49*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^3 + 3*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^2 + (3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d + 5*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m + 12*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^4 + 4*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^3 + 6*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^2 + (3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d + 4*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m)*n)*x*x^{3*n}*e^{(m*\log(e) + m*\log(x))} + ((3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^5 + 5*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^4 + 60*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d + (3*(B*a^2*b +$

$$\begin{aligned}
& A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m)*n^4 + 10*(3*(B*a^2*b + A*a*b^2)*c + \\
& (B*a^3 + 3*A*a^2*b)*d)*m^3 + 107*((3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a \\
& ^2*b)*d)*m^2 + 3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d + 2*(3*(B*a^ \\
& 2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m)*n^3 + 10*(3*(B*a^2*b + A*a*b^2 \\
& )*c + (B*a^3 + 3*A*a^2*b)*d)*m^2 + 59*((3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + \\
& 3*A*a^2*b)*d)*m^3 + 3*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^2 \\
& + 3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d + 3*(3*(B*a^2*b + A*a*b^ \\
& 2)*c + (B*a^3 + 3*A*a^2*b)*d)*m)*n^2 + 3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3 \\
& *A*a^2*b)*d + 5*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m + 13*(( \\
& 3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^4 + 4*(3*(B*a^2*b + A*a* \\
& b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^3 + 6*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + \\
& 3*A*a^2*b)*d)*m^2 + 3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d + 4*(3 \\
& *(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m)*n)*x*x^(2*n)*e^(m*log(e) \\
& + m*log(x)) + ((A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m^5 + A*a^3*d + 5*(A*a^3*d \\
& + (B*a^3 + 3*A*a^2*b)*c)*m^4 + 120*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c + (A* \\
& a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m)*n^4 + 10*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c \\
& )*m^3 + 154*(A*a^3*d + (A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m^2 + (B*a^3 + 3*A \\
& *a^2*b)*c + 2*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m)*n^3 + 10*(A*a^3*d + (B*a \\
& ^3 + 3*A*a^2*b)*c)*m^2 + 71*(A*a^3*d + (A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m^ \\
& 3 + 3*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m^2 + (B*a^3 + 3*A*a^2*b)*c + 3*(A \\
& a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m)*n^2 + (B*a^3 + 3*A*a^2*b)*c + 5*(A*a^3*d \\
& + (B*a^3 + 3*A*a^2*b)*c)*m + 14*(A*a^3*d + (A*a^3*d + (B*a^3 + 3*A*a^2*b)*c \\
& )*m^4 + 4*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m^3 + 6*(A*a^3*d + (B*a^3 + 3*A \\
& *a^2*b)*c)*m^2 + (B*a^3 + 3*A*a^2*b)*c + 4*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c \\
& )*m)*n)*x*x^n*e^(m*log(e) + m*log(x)) + (A*a^3*c*m^5 + 120*A*a^3*c*n^5 + 5* \\
& A*a^3*c*m^4 + 10*A*a^3*c*m^3 + 10*A*a^3*c*m^2 + 5*A*a^3*c*m + A*a^3*c + 274 \\
& *(A*a^3*c*m + A*a^3*c)*n^4 + 225*(A*a^3*c*m^2 + 2*A*a^3*c*m + A*a^3*c)*n^3 \\
& + 85*(A*a^3*c*m^3 + 3*A*a^3*c*m^2 + 3*A*a^3*c*m + A*a^3*c)*n^2 + 15*(A*a^3*c \\
& *m^4 + 4*A*a^3*c*m^3 + 6*A*a^3*c*m^2 + 4*A*a^3*c*m + A*a^3*c)*n)*x*e^(m*log \\
& (e) + m*log(x))/(m^6 + 120*(m + 1)*n^5 + 6*m^5 + 274*(m^2 + 2*m + 1)*n^4 \\
& + 15*m^4 + 225*(m^3 + 3*m^2 + 3*m + 1)*n^3 + 20*m^3 + 85*(m^4 + 4*m^3 + 6*m \\
& ^2 + 4*m + 1)*n^2 + 15*m^2 + 15*(m^5 + 5*m^4 + 10*m^3 + 10*m^2 + 5*m + 1)*n \\
& + 6*m + 1)
\end{aligned}$$

**giac [B]** time = 1.19, size = 6927, normalized size = 32.99

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="giac")

[Out] (B\*b^3\*d\*m^5\*x\*x^m\*x^(5\*n)\*e^m + 10\*B\*b^3\*d\*m^4\*n\*x\*x^m\*x^(5\*n)\*e^m + 35\*B\*b^3\*d\*m^3\*n^2\*x\*x^m\*x^(5\*n)\*e^m + 50\*B\*b^3\*d\*m^2\*n^3\*x\*x^m\*x^(5\*n)\*e^m + 24\*B\*b^3\*d\*m\*n^4\*x\*x^m\*x^(5\*n)\*e^m + B\*b^3\*c\*m^5\*x\*x^m\*x^(4\*n)\*e^m + 3\*B\*a\*b^2\*d\*m^5\*x\*x^m\*x^(4\*n)\*e^m + A\*b^3\*d\*m^5\*x\*x^m\*x^(4\*n)\*e^m + 11\*B\*b^3\*c\*m^4\*n\*x\*x^m\*x^(4\*n)\*e^m + 33\*B\*a\*b^2\*d\*m^4\*n\*x\*x^m\*x^(4\*n)\*e^m + 11\*A\*b^3\*d\*m^4\*n\*x\*x^m\*x^(4\*n)\*e^m + 41\*B\*b^3\*c\*m^3\*n^2\*x\*x^m\*x^(4\*n)\*e^m + 123\*B\*a\*b^2\*d\*m^3\*n^2\*x\*x^m\*x^(4\*n)\*e^m + 41\*A\*b^3\*d\*m^3\*n^2\*x\*x^m\*x^(4\*n)\*e^m + 61\*B\*b^3\*c\*m^2\*n^3\*x\*x^m\*x^(4\*n)\*e^m + 183\*B\*a\*b^2\*d\*m^2\*n^3\*x\*x^m\*x^(4\*n)\*e^m + 61\*A\*b^3\*d\*m^2\*n^3\*x\*x^m\*x^(4\*n)\*e^m + 30\*B\*b^3\*c\*m\*n^4\*x\*x^m\*x^(4\*n)\*e^m + 90\*B\*a\*b^2\*d\*m\*n^4\*x\*x^m\*x^(4\*n)\*e^m + 30\*A\*b^3\*d\*m\*n^4\*x\*x^m\*x^(4\*n)\*e^m + 3\*B\*a\*b^2\*c\*m^5\*x\*x^m\*x^(3\*n)\*e^m + A\*b^3\*c\*m^5\*x\*x^m\*x^(3\*n)\*e^m + 3\*B\*a^2\*b\*d\*m^5\*x\*x^m\*x^(3\*n)\*e^m + 3\*A\*a\*b^2\*d\*m^5\*x\*x^m\*x^(3\*n)\*e^m + 36\*B\*a\*b^2\*c\*m^4\*n\*x\*x^m\*x^(3\*n)\*e^m + 12\*A\*b^3\*c\*m^4\*n\*x\*x^m\*x^(3\*n)\*e^m + 36\*B\*a^2\*b\*d\*m^4\*n\*x\*x^m\*x^(3\*n)\*e^m + 36\*A\*a\*b^2\*d\*m^4\*n\*x\*x^m\*x^(3\*n)\*e^m + 147\*B\*a\*b^2\*c\*m^3\*n^2\*x\*x^m\*x^(3\*n)\*e^m + 49\*A\*b^3\*c\*m^3\*n^2\*x\*x^m\*x^(3\*n)\*e^m + 147\*B\*a^2\*b\*d\*m^3\*n^2\*x\*x^m\*x^(3\*n)\*e^m + 147\*A\*a\*b^2\*d\*m^3\*n^2\*x\*x^m\*x^(3\*n)\*e^m + 234\*B\*a\*b^2\*c\*m^2\*n^3\*x\*x^m\*x^(3\*n)\*e^m + 78\*A\*b^3\*c\*m^2\*n^3\*x\*x^m\*x^(3\*n)\*e^m + 234\*B\*a^2\*b\*d\*m^2\*n^3\*x\*x^m\*x^(3\*n)\*e^m + 234\*A\*a\*b^2\*d\*m^2\*n^3\*x\*x^m\*x^(3\*n)\*e^m + 120\*B\*a\*b^2\*c\*m\*n^4\*x\*x^m\*x^(3\*n)\*e^m + 40\*A\*b^3\*c

$$\begin{aligned}
& *m^n^4*x*x^m*x^{(3*n)}*e^m + 120*B*a^2*b*d*m^n^4*x*x^m*x^{(3*n)}*e^m + 120*A*a*b^2*d*m^n^4*x*x^m*x^{(3*n)}*e^m + 3*B*a^2*b*c*m^5*x*x^m*x^{(2*n)}*e^m + 3*A*a*b^2*c*m^5*x*x^m*x^{(2*n)}*e^m + B*a^3*d*m^5*x*x^m*x^{(2*n)}*e^m + 3*A*a^2*b*d*m^5*x*x^m*x^{(2*n)}*e^m + 39*B*a^2*b*c*m^4*n*x*x^m*x^{(2*n)}*e^m + 39*A*a*b^2*c*m^4*n*x*x^m*x^{(2*n)}*e^m + 13*B*a^3*d*m^4*n*x*x^m*x^{(2*n)}*e^m + 39*A*a^2*b*d*m^4*n*x*x^m*x^{(2*n)}*e^m + 177*B*a^2*b*c*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 177*A*a*b^2*c*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 59*B*a^3*d*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 177*A*a^2*b*d*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 321*B*a^2*b*c*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 321*A*a*b^2*c*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 107*B*a^3*d*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 321*A*a^2*b*d*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 180*B*a^2*b*c*m*n^4*x*x^m*x^{(2*n)}*e^m + 180*A*a*b^2*c*m*n^4*x*x^m*x^{(2*n)}*e^m + 60*B*a^3*d*m*n^4*x*x^m*x^{(2*n)}*e^m + 180*A*a^2*b*d*m*n^4*x*x^m*x^{(2*n)}*e^m + B*a^3*c*m^5*x*x^m*x^n*e^m + 3*A*a^2*b*c*m^5*x*x^m*x^n*e^m + A*a^3*d*m^5*x*x^m*x^n*e^m + 14*B*a^3*c*m^4*n*x*x^m*x^n*e^m + 42*A*a^2*b*c*m^4*n*x*x^m*x^n*e^m + 14*A*a^3*d*m^4*n*x*x^m*x^n*e^m + 71*B*a^3*c*m^3*n^2*x*x^m*x^n*e^m + 213*A*a^2*b*c*m^3*n^2*x*x^m*x^n*e^m + 71*A*a^3*d*m^3*n^2*x*x^m*x^n*e^m + 154*B*a^3*c*m^2*n^3*x*x^m*x^n*e^m + 462*A*a^2*b*c*m^2*n^3*x*x^m*x^n*e^m + 154*A*a^3*d*m^2*n^3*x*x^m*x^n*e^m + 120*B*a^3*c*m*n^4*x*x^m*x^n*e^m + 360*A*a^2*b*c*m*n^4*x*x^m*x^n*e^m + 120*A*a^3*d*m*n^4*x*x^m*x^n*e^m + A*a^3*c*m^5*x*x^m*e^m + 15*A*a^3*c*m^4*n*x*x^m*e^m + 85*A*a^3*c*m^3*n^2*x*x^m*e^m + 225*A*a^3*c*m^2*n^3*x*x^m*e^m + 274*A*a^3*c*m*n^4*x*x^m*e^m + 120*A*a^3*c*n^5*x*x^m*e^m + 5*B*b^3*d*m^4*x*x^m*x^{(5*n)}*e^m + 40*B*b^3*d*m^3*n*x*x^m*x^{(5*n)}*e^m + 105*B*b^3*d*m^2*n^2*x*x^m*x^{(5*n)}*e^m + 100*B*b^3*d*m*n^3*x*x^m*x^{(5*n)}*e^m + 24*B*b^3*d*n^4*x*x^m*x^{(5*n)}*e^m + 5*B*b^3*c*m^4*x*x^m*x^{(4*n)}*e^m + 15*B*a*b^2*d*m^4*x*x^m*x^{(4*n)}*e^m + 5*A*b^3*d*m^4*x*x^m*x^{(4*n)}*e^m + 44*B*b^3*c*m^3*n*x*x^m*x^{(4*n)}*e^m + 132*B*a*b^2*d*m^3*n*x*x^m*x^{(4*n)}*e^m + 44*A*b^3*d*m^3*n*x*x^m*x^{(4*n)}*e^m + 123*B*b^3*c*m^2*n^2*x*x^m*x^{(4*n)}*e^m + 369*B*a*b^2*d*m^2*n^2*x*x^m*x^{(4*n)}*e^m + 123*A*b^3*d*m^2*n^2*x*x^m*x^{(4*n)}*e^m + 122*B*b^3*c*m*n^3*x*x^m*x^{(4*n)}*e^m + 366*B*a*b^2*d*m*n^3*x*x^m*x^{(4*n)}*e^m + 122*A*b^3*d*m*n^3*x*x^m*x^{(4*n)}*e^m + 30*B*b^3*c*n^4*x*x^m*x^{(4*n)}*e^m + 90*B*a*b^2*d*n^4*x*x^m*x^{(4*n)}*e^m + 30*A*b^3*d*n^4*x*x^m*x^{(4*n)}*e^m + 15*B*a*b^2*c*m^4*x*x^m*x^{(3*n)}*e^m + 5*A*b^3*c*m^4*x*x^m*x^{(3*n)}*e^m + 15*B*a^2*b*d*m^4*x*x^m*x^{(3*n)}*e^m + 15*A*a*b^2*d*m^4*x*x^m*x^{(3*n)}*e^m + 144*B*a*b^2*c*m^3*n*x*x^m*x^{(3*n)}*e^m + 48*A*b^3*c*m^3*n*x*x^m*x^{(3*n)}*e^m + 144*B*a^2*b*d*m^3*n*x*x^m*x^{(3*n)}*e^m + 144*A*a*b^2*d*m^3*n*x*x^m*x^{(3*n)}*e^m + 441*B*a*b^2*c*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 147*A*b^3*c*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 441*B*a^2*b*d*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 441*A*a*b^2*d*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 468*B*a*b^2*c*m*n^3*x*x^m*x^{(3*n)}*e^m + 156*A*b^3*c*m*n^3*x*x^m*x^{(3*n)}*e^m + 468*B*a^2*b*d*m*n^3*x*x^m*x^{(3*n)}*e^m + 468*A*a*b^2*d*m*n^3*x*x^m*x^{(3*n)}*e^m + 120*B*a*b^2*c*n^4*x*x^m*x^{(3*n)}*e^m + 40*A*b^3*c*n^4*x*x^m*x^{(3*n)}*e^m + 120*B*a^2*b*d*n^4*x*x^m*x^{(3*n)}*e^m + 120*A*a*b^2*d*n^4*x*x^m*x^{(3*n)}*e^m + 15*B*a^2*b*c*m^4*x*x^m*x^{(2*n)}*e^m + 15*A*a*b^2*c*m^4*x*x^m*x^{(2*n)}*e^m + 156*B*a^2*b*c*m^3*n*x*x^m*x^{(2*n)}*e^m + 156*A*a*b^2*c*m^3*n*x*x^m*x^{(2*n)}*e^m + 52*B*a^3*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 156*A*a^2*b*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 531*B*a^2*b*c*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 531*A*a*b^2*c*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 177*B*a^3*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 531*A*a^2*b*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 642*B*a^2*b*c*m*n^3*x*x^m*x^{(2*n)}*e^m + 642*A*a*b^2*c*m*n^3*x*x^m*x^{(2*n)}*e^m + 214*B*a^3*d*m*n^3*x*x^m*x^{(2*n)}*e^m + 642*A*a^2*b*d*m*n^3*x*x^m*x^{(2*n)}*e^m + 180*B*a^2*b*c*n^4*x*x^m*x^{(2*n)}*e^m + 180*A*a*b^2*c*n^4*x*x^m*x^{(2*n)}*e^m + 60*B*a^3*d*n^4*x*x^m*x^{(2*n)}*e^m + 180*A*a^2*b*d*n^4*x*x^m*x^{(2*n)}*e^m + 5*B*a^3*c*m^4*x*x^m*x^n*e^m + 15*A*a^2*b*c*m^4*x*x^m*x^n*e^m + 5*A*a^3*d*m^4*x*x^m*x^n*e^m + 56*B*a^3*c*m^3*n*x*x^m*x^n*e^m + 168*A*a^2*b*c*m^3*n*x*x^m*x^n*e^m + 56*A*a^3*d*m^3*n*x*x^m*x^n*e^m + 213*B*a^3*c*m^2*n^2*x*x^m*x^n*e^m + 639*A*a^2*b*c*m^2*n^2*x*x^m*x^n*e^m + 213*A*a^3*d*m^2*n^2*x*x^m*x^n*e^m + 308*B*a^3*c*m*n^3*x*x^m*x^n*e^m + 924*A*a^2*b*c*m*n^3*x*x^m*x^n*e^m + 308*A*a^3*d*m*n^3*x*x^m*x^n*e^m + 120*B*a^3*c*n^4*x*x^m*x^n*e^m + 360*A*a^2*b*c*n^4*x*x^m*x^n*e^m + 120*A*a^3*d*n^4*x*x^m*x^n*e^m + 5*A*a^3*c*m^4*x*x^m*e^m + 60*A*a^3*c*m^3*n*x*x
\end{aligned}$$

$$\begin{aligned}
& \cdot m^2 e^m + 255 A^3 c^3 m^2 n^2 x^2 m^2 e^m + 450 A^3 c^3 m^2 n^3 x^2 m^2 e^m + 274 A^3 c^3 m^2 n^4 x^2 m^2 e^m + 10 B^3 b^3 d^3 m^3 x^2 m^2 x^{(5n)} e^m + 60 B^3 b^3 d^3 m^2 n x^2 m^2 x^{(5n)} e^m + 105 B^3 b^3 d^3 m^2 n^2 x^2 m^2 x^{(5n)} e^m + 50 B^3 b^3 d^3 m^2 n^3 x^2 m^2 x^{(5n)} e^m + 10 B^3 b^3 c^3 m^3 x^2 m^2 x^{(4n)} e^m + 30 B^3 a^2 b^2 d^3 m^3 x^2 m^2 x^{(4n)} e^m + 10 A^3 b^3 d^3 m^3 x^2 m^2 x^{(4n)} e^m + 66 B^3 b^3 c^3 m^2 n x^2 m^2 x^{(4n)} e^m + 198 B^3 a^2 b^2 d^3 m^2 n x^2 m^2 x^{(4n)} e^m + 66 A^3 b^3 d^3 m^2 n x^2 m^2 x^{(4n)} e^m + 123 B^3 b^3 c^3 m^2 n^2 x^2 m^2 x^{(4n)} e^m + 369 B^3 a^2 b^2 d^3 m^2 n^2 x^2 m^2 x^{(4n)} e^m + 123 A^3 b^3 d^3 m^2 n^2 x^2 m^2 x^{(4n)} e^m + 61 B^3 b^3 c^3 m^2 n^3 x^2 m^2 x^{(4n)} e^m + 183 B^3 a^2 b^2 d^3 m^2 n^3 x^2 m^2 x^{(4n)} e^m + 61 A^3 b^3 d^3 m^2 n^3 x^2 m^2 x^{(4n)} e^m + 30 B^3 a^2 b^2 c^3 m^3 x^2 m^2 x^{(3n)} e^m + 10 A^3 b^3 c^3 m^3 x^2 m^2 x^{(3n)} e^m + 30 B^3 a^2 b^2 d^3 m^3 x^2 m^2 x^{(3n)} e^m + 30 A^3 a^2 b^2 d^3 m^3 x^2 m^2 x^{(3n)} e^m + 216 B^3 a^2 b^2 c^3 m^2 n x^2 m^2 x^{(3n)} e^m + 72 A^3 b^3 c^3 m^2 n x^2 m^2 x^{(3n)} e^m + 216 B^3 a^2 b^2 d^3 m^2 n x^2 m^2 x^{(3n)} e^m + 216 A^3 a^2 b^2 d^3 m^2 n x^2 m^2 x^{(3n)} e^m + 441 B^3 a^2 b^2 c^3 m^2 n^2 x^2 m^2 x^{(3n)} e^m + 147 A^3 b^3 c^3 m^2 n^2 x^2 m^2 x^{(3n)} e^m + 441 B^3 a^2 b^2 d^3 m^2 n^2 x^2 m^2 x^{(3n)} e^m + 441 A^3 a^2 b^2 d^3 m^2 n^2 x^2 m^2 x^{(3n)} e^m + 234 B^3 a^2 b^2 c^3 m^2 n^3 x^2 m^2 x^{(3n)} e^m + 78 A^3 b^3 c^3 m^2 n^3 x^2 m^2 x^{(3n)} e^m + 234 B^3 a^2 b^2 d^3 m^2 n^3 x^2 m^2 x^{(3n)} e^m + 234 A^3 a^2 b^2 d^3 m^2 n^3 x^2 m^2 x^{(3n)} e^m + 30 B^3 a^2 b^2 c^3 m^3 x^2 m^2 x^{(2n)} e^m + 30 A^3 a^2 b^2 c^3 m^3 x^2 m^2 x^{(2n)} e^m + 10 B^3 a^3 d^3 m^3 x^2 m^2 x^{(2n)} e^m + 30 A^3 a^2 b^2 d^3 m^3 x^2 m^2 x^{(2n)} e^m + 234 B^3 a^2 b^2 c^3 m^2 n x^2 m^2 x^{(2n)} e^m + 234 A^3 a^2 b^2 c^3 m^2 n x^2 m^2 x^{(2n)} e^m + 78 B^3 a^3 d^3 m^2 n x^2 m^2 x^{(2n)} e^m + 234 A^3 a^2 b^2 d^3 m^2 n x^2 m^2 x^{(2n)} e^m + 531 B^3 a^2 b^2 c^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 531 A^3 a^2 b^2 c^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 177 B^3 a^3 d^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 531 A^3 a^2 b^2 d^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 321 B^3 a^2 b^2 c^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 321 A^3 a^2 b^2 c^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 107 B^3 a^3 d^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 321 A^3 a^2 b^2 d^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 10 B^3 a^3 c^3 m^3 x^2 m^2 x^{(2n)} e^m + 30 A^3 a^2 b^2 c^3 m^3 x^2 m^2 x^{(2n)} e^m + 10 A^3 a^3 d^3 m^3 x^2 m^2 x^{(2n)} e^m + 84 B^3 a^3 c^3 m^2 n x^2 m^2 x^{(2n)} e^m + 252 A^3 a^2 b^2 c^3 m^2 n x^2 m^2 x^{(2n)} e^m + 84 A^3 a^3 d^3 m^2 n x^2 m^2 x^{(2n)} e^m + 213 B^3 a^3 c^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 639 A^3 a^2 b^2 c^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 213 A^3 a^3 d^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 154 B^3 a^3 c^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 462 A^3 a^2 b^2 c^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 154 A^3 a^3 d^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 10 A^3 a^3 c^3 m^3 x^2 m^2 e^m + 90 A^3 a^3 c^3 m^2 n x^2 m^2 e^m + 255 A^3 c^3 m^2 n^2 x^2 m^2 e^m + 225 A^3 a^3 c^3 m^2 n^3 x^2 m^2 e^m + 10 B^3 b^3 d^3 m^2 n x^2 m^2 x^{(5n)} e^m + 40 B^3 b^3 d^3 m^2 n^2 x^2 m^2 x^{(5n)} e^m + 35 B^3 b^3 d^3 m^2 n^3 x^2 m^2 x^{(5n)} e^m + 10 B^3 b^3 c^3 m^2 n x^2 m^2 x^{(4n)} e^m + 30 B^3 a^2 b^2 d^3 m^2 n x^2 m^2 x^{(4n)} e^m + 10 A^3 b^3 d^3 m^2 n x^2 m^2 x^{(4n)} e^m + 44 B^3 b^3 c^3 m^2 n^2 x^2 m^2 x^{(4n)} e^m + 132 B^3 a^2 b^2 d^3 m^2 n^2 x^2 m^2 x^{(4n)} e^m + 44 A^3 b^3 d^3 m^2 n^2 x^2 m^2 x^{(4n)} e^m + 41 B^3 b^3 c^3 m^2 n^3 x^2 m^2 x^{(4n)} e^m + 123 B^3 a^2 b^2 d^3 m^2 n^3 x^2 m^2 x^{(4n)} e^m + 41 A^3 b^3 d^3 m^2 n^3 x^2 m^2 x^{(4n)} e^m + 30 B^3 a^2 b^2 c^3 m^2 n x^2 m^2 x^{(3n)} e^m + 10 A^3 b^3 c^3 m^2 n x^2 m^2 x^{(3n)} e^m + 30 B^3 a^2 b^2 d^3 m^2 n x^2 m^2 x^{(3n)} e^m + 30 A^3 a^2 b^2 d^3 m^2 n x^2 m^2 x^{(3n)} e^m + 144 B^3 a^2 b^2 c^3 m^2 n^2 x^2 m^2 x^{(3n)} e^m + 48 A^3 b^3 c^3 m^2 n^2 x^2 m^2 x^{(3n)} e^m + 144 B^3 a^2 b^2 d^3 m^2 n^2 x^2 m^2 x^{(3n)} e^m + 144 A^3 a^2 b^2 d^3 m^2 n^2 x^2 m^2 x^{(3n)} e^m + 147 B^3 a^2 b^2 c^3 m^2 n^3 x^2 m^2 x^{(3n)} e^m + 49 A^3 b^3 c^3 m^2 n^3 x^2 m^2 x^{(3n)} e^m + 147 B^3 a^2 b^2 d^3 m^2 n^3 x^2 m^2 x^{(3n)} e^m + 147 A^3 a^2 b^2 d^3 m^2 n^3 x^2 m^2 x^{(3n)} e^m + 30 B^3 a^2 b^2 c^3 m^2 n x^2 m^2 x^{(2n)} e^m + 30 A^3 a^2 b^2 c^3 m^2 n x^2 m^2 x^{(2n)} e^m + 10 B^3 a^3 d^3 m^2 n x^2 m^2 x^{(2n)} e^m + 30 A^3 a^2 b^2 d^3 m^2 n x^2 m^2 x^{(2n)} e^m + 156 B^3 a^2 b^2 c^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 156 A^3 a^2 b^2 c^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 52 B^3 a^3 d^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 156 A^3 a^2 b^2 d^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 177 B^3 a^2 b^2 c^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 177 A^3 a^2 b^2 c^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 59 B^3 a^3 d^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 177 A^3 a^2 b^2 d^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 10 B^3 a^3 c^3 m^2 n x^2 m^2 x^{(2n)} e^m + 30 A^3 a^2 b^2 c^3 m^2 n x^2 m^2 x^{(2n)} e^m + 10 A^3 a^3 d^3 m^2 n x^2 m^2 x^{(2n)} e^m + 56 B^3 a^3 c^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 168 A^3 a^2 b^2 c^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 56 A^3 a^3 d^3 m^2 n^2 x^2 m^2 x^{(2n)} e^m + 71 B^3 a^3 c^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 213 A^3 a^2 b^2 c^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 71 A^3 a^3 d^3 m^2 n^3 x^2 m^2 x^{(2n)} e^m + 10 A^3 a^3 c^3 m^2 n x^2 m^2 e^m + 60 A^3 a^3 c^3 m^2 n x^2 m^2 e^m + 85 A^3 a^3 c^3 m^2 n x^2 m^2 e^m + 5 B^3 b^3 d^3 m^2 n x^2 m^2 x^{(5n)} e^m + 10 B^3 b^3 d^3 m^2 n^2 x^2 m^2 x^{(5n)} e^m + 5 B^3 b^3 c^3 m^2 n x^2 m^2 x^{(4n)} e^m + 15 B^3 a^2 b^2 d^3 m^2 n x^2 m^2 x^{(4n)} e^m + 5 A^3 b^3 d^3 m^2 n x^2 m^2 x^{(4n)} e^m + 11 B^3 b^3 c^3 m^2 n x^2 m^2 x^{(4n)} e^m + 33 B^3 a^2 b^2 d^3 m^2 n x^2 m^2 x^{(4n)} e^m + 11 A^3 b^3 d^3 m^2 n x^2 m^2 x^{(4n)} e^m + 15 B^3 a^2 b^2 c^3 m^2 n x^2 m^2 x^{(3n)} e^m + 5 A^3 b^3 c^3 m^2 n x^2 m^2 x^{(3n)} e^m
\end{aligned}$$

$$\begin{aligned}
 &x^{(3n)}e^m + 15B^2a^2b^2d^2m^2x^m x^{(3n)}e^m + 15A^2a^2b^2d^2m^2x^m x^{(3n)}e^m + 36B^2a^2b^2c^2n^2x^m x^{(3n)}e^m + 12A^2b^3c^2n^2x^m x^{(3n)}e^m \\
 &+ 36B^2a^2b^2d^2m^2x^m x^{(3n)}e^m + 36A^2a^2b^2d^2m^2x^m x^{(3n)}e^m + 15B^2a^2b^2c^2m^2x^m x^{(2n)}e^m + 15A^2a^2b^2c^2m^2x^m x^{(2n)}e^m + 5B^2a^3d^2m^2x^m x^{(2n)}e^m \\
 &+ 15A^2a^2b^2d^2m^2x^m x^{(2n)}e^m + 39B^2a^2b^2c^2n^2x^m x^{(2n)}e^m + 39A^2a^2b^2c^2n^2x^m x^{(2n)}e^m + 13B^2a^3d^2m^2x^m x^{(2n)}e^m \\
 &+ 39A^2a^2b^2d^2m^2x^m x^{(2n)}e^m + 5B^2a^3c^2m^2x^m x^{(n)}e^m + 15A^2a^2b^2c^2m^2x^m x^{(n)}e^m + 5A^2a^3d^2m^2x^m x^{(n)}e^m + 14B^2a^3c^2n^2x^m x^{(n)}e^m \\
 &+ 42A^2a^2b^2c^2n^2x^m x^{(n)}e^m + 14A^2a^3d^2m^2x^m x^{(n)}e^m + 5A^2a^3c^2m^2x^m x^{(n)}e^m + 15A^2a^3c^2n^2x^m x^{(n)}e^m + B^2b^3d^2x^m x^{(5n)}e^m \\
 &+ B^2b^3c^2x^m x^{(4n)}e^m + 3B^2a^2b^2d^2x^m x^{(4n)}e^m + A^2b^3d^2x^m x^{(4n)}e^m + 3B^2a^2b^2c^2x^m x^{(3n)}e^m + A^2b^3c^2x^m x^{(3n)}e^m + 3B^2a^2b^2d^2x^m x^{(3n)}e^m \\
 &+ 3A^2a^2b^2d^2x^m x^{(3n)}e^m + 3B^2a^2b^2c^2x^m x^{(2n)}e^m + 3A^2a^2b^2c^2x^m x^{(2n)}e^m + B^2a^3d^2x^m x^{(2n)}e^m + 3A^2a^2b^2d^2x^m x^{(2n)}e^m + B^2a^3c^2x^m x^{(n)}e^m \\
 &+ 3A^2a^2b^2c^2x^m x^{(n)}e^m + A^2a^3d^2x^m x^{(n)}e^m + A^2a^3c^2x^m x^{(n)}e^m)/(m^6 + 15m^5n + 85m^4n^2 + 225m^3n^3 + 274m^2n^4 + 120mn^5 + 6m^5 + 75m^4n + 340m^3n^2 \\
 &+ 675m^2n^3 + 548mn^4 + 120n^5 + 15m^4 + 150m^3n + 510m^2n^2 + 675mn^3 + 274n^4 + 20m^3 + 150m^2n + 340mn^2 + 225n^3 + 15m^2 + 75mn + 85n^2 + 6m + 15n + 1)
 \end{aligned}$$

**maple [C]** time = 0.21, size = 4972, normalized size = 23.68

output too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((e*x)^m*(b*x^n+a)^3*(A+B*x^n)*(d*x^n+c), x)`

[Out] `x*(41*A*b^3*d*m^3*n^2*(x^n)^4+61*A*b^3*d*m^2*n^3*(x^n)^4+30*A*b^3*d*m*n^4*(x^n)^4+24*B*b^3*d*m*n^4*(x^n)^5+11*A*b^3*d*m^4*n*(x^n)^4+40*B*b^3*d*m^3*n*(x^n)^5+3*B*a*b^2*d*m^5*(x^n)^4+11*B*b^3*c*m^4*n*(x^n)^4+41*B*b^3*c*m^3*n^2*(x^n)^4+61*B*b^3*c*m^2*n^3*(x^n)^4+10*B*b^3*d*m^4*n*(x^n)^5+35*B*b^3*d*m^3*n^2*(x^n)^5+50*B*b^3*d*m^2*n^3*(x^n)^5+105*B*b^3*d*m^2*n^2*(x^n)^5+100*B*b^3*d*m*n^3*(x^n)^5+3*A*a*b^2*d*m^5*(x^n)^3+12*A*b^3*c*m^4*n*(x^n)^3+49*A*b^3*c*m^3*n^2*(x^n)^3+78*A*b^3*c*m^2*n^3*(x^n)^3+40*A*b^3*c*m*n^4*(x^n)^3+44*A*b^3*d*m^3*n*(x^n)^4+123*A*b^3*d*m^2*n^2*(x^n)^4+30*B*b^3*c*m*n^4*(x^n)^4+3*B*a*b^2*c*m^5*(x^n)^3+15*B*a*b^2*d*m^4*(x^n)^4+90*B*a*b^2*d*n^4*(x^n)^4+44*B*b^3*c*m^3*n*(x^n)^4+123*B*b^3*c*m^2*n^2*(x^n)^4+122*B*b^3*c*m*n^3*(x^n)^4+60*B*b^3*d*m^2*n*(x^n)^5+105*B*b^3*d*m*n^2*(x^n)^5+3*A*a^2*b*d*m^5*(x^n)^2+3*A*a*b^2*c*m^5*(x^n)^2+66*A*b^3*d*m^2*n*(x^n)^4+123*A*b^3*d*m*n^2*(x^n)^4+122*A*b^3*d*m*n^3*(x^n)^4+3*B*a^2*b*d*m^5*(x^n)^3+15*A*a*b^2*d*m^4*(x^n)^3+120*A*a*b^2*d*n^4*(x^n)^3+48*A*b^3*c*m^3*n*(x^n)^3+147*A*b^3*c*m^2*n^2*(x^n)^3+156*A*b^3*c*m*n^3*(x^n)^3+15*B*a*b^2*c*m^4*(x^n)^3+120*B*a*b^2*c*n^4*(x^n)^3+30*B*a*b^2*d*m^3*(x^n)^4+183*B*a*b^2*d*n^3*(x^n)^4+66*B*b^3*c*m^2*n*(x^n)^4+123*B*b^3*c*m*n^2*(x^n)^4+40*B*b^3*d*m*n*(x^n)^5+14*A*a^3*d*m^4*n*x^n+71*A*a^3*d*m^3*n^2*x^n+120*B*a^3*c*m*n^4*x^n+52*B*a^3*d*m^3*n*(x^n)^2+13*B*a^3*d*m^4*n*(x^n)^2+59*B*a^3*d*m^3*n^2*(x^n)^2+107*B*a^3*d*m^2*n^3*(x^n)^2+60*B*a^3*d*m*n^4*(x^n)^2+3*B*a^2*b*c*m^5*(x^n)^2+15*B*a^2*b*d*m^4*(x^n)^3+120*B*a^2*b*d*n^4*(x^n)^3+180*A*a*b^2*c*n^4*(x^n)^2+30*A*a*b^2*d*m^3*(x^n)^3+234*A*a*b^2*d*n^3*(x^n)^3+72*A*b^3*c*m^2*n*(x^n)^3+147*A*b^3*c*m*n^2*(x^n)^3+44*A*b^3*d*m*n*(x^n)^4+14*B*a^3*c*m^4*n*x^n+71*B*a^3*c*m^3*n^2*x^n+154*B*a^3*c*m^2*n^3*x^n+321*A*a^2*b*d*n^3*(x^n)^2+30*A*a*b^2*c*m^3*(x^n)^2+321*A*a*b^2*c*n^3*(x^n)^2+154*A*a^3*d*m^2*n^3*x^n+120*A*a^3*d*m*n^4*x^n+3*A*a^2*b*c*m^5*x^n+15*A*a^2*b*d*m^4*(x^n)^2+180*A*a^2*b*d*n^4*(x^n)^2+15*A*a*b^2*c*m^4*(x^n)^2+234*B*a^2*b*d*n^3*(x^n)^3+30*B*a*b^2*c*m^3*(x^n)^3+234*B*a*b^2*c*n^3*(x^n)^3+30*B*a*b^2*d*m^2*(x^n)^4+123*B*a*b^2*d*n^2*(x^n)^4+44*B*b^3*c*m*n*(x^n)^4+56*A*a^3*d*m^3*n*x^n+213*A*a^3*d*m^2*n^2*x^n+308*A*a^3*d*m*n^3*x^n+15*A*a^2*b*c*m^4*x^n+360*A*a^2*b*c*n^4*x^n+30*A*a^2*b*d*m^3*(x^n)^2+84*A*a^3*d*m^2*n*x^n+213*A*a^3*d*m*n^2*x^n+30*A*a^2*b*c*m^3*x^n+462*A*a^2*b*c*n^3*x^n+177*B*a^3*d*m^2*n^2*(x^n)^2+214*B*a^3*d*m*n^3*(x^n)^2+15*B*a^`

$$\begin{aligned}
& 2*b*c*m^4*(x^n)^2+180*B*a^2*b*c*n^4*(x^n)^2+30*B*a^2*b*d*m^3*(x^n)^3+177*B* \\
& a^3*d*m*n^2*(x^n)^2+30*B*a^2*b*c*m^3*(x^n)^2+321*B*a^2*b*c*n^3*(x^n)^2+30*B \\
& *a^2*b*d*m^2*(x^n)^3+147*B*a^2*b*d*n^2*(x^n)^3+30*B*a*b^2*c*m^2*(x^n)^3+147 \\
& *B*a*b^2*c*n^2*(x^n)^3+15*B*a*b^2*d*(x^n)^4+m+33*B*a*b^2*d*(x^n)^4*n+30*A*a \\
& *b^2*d*m^2*(x^n)^3+147*A*a*b^2*d*n^2*(x^n)^3+48*A*b^3*c*m*n*(x^n)^3+56*B*a^ \\
& 3*c*m^3*n*x^n+213*B*a^3*c*m^2*n^2*x^n+308*B*a^3*c*m*n^3*x^n+78*B*a^3*d*m^2* \\
& n*(x^n)^2+213*B*a^3*c*m*n^2*x^n+52*B*a^3*d*m*n*(x^n)^2+30*B*a^2*b*c*m^2*(x \\
& ^n)^2+177*B*a^2*b*c*n^2*(x^n)^2+15*B*a^2*b*d*(x^n)^3*m+36*B*a^2*b*d*(x^n)^3* \\
& n+15*B*a*b^2*c*(x^n)^3*m+30*A*a^2*b*d*m^2*(x^n)^2+177*A*a^2*b*d*n^2*(x^n)^2 \\
& +30*A*a*b^2*c*m^2*(x^n)^2+177*A*a*b^2*c*n^2*(x^n)^2+15*A*a*b^2*d*(x^n)^3*m+ \\
& 36*A*a*b^2*d*(x^n)^3*n+84*B*a^3*c*m^2*n*x^n+30*A*a^2*b*c*m^2*x^n+213*A*a^2* \\
& b*c*n^2*x^n+15*A*a^2*b*d*(x^n)^2*m+39*A*a^2*b*d*(x^n)^2*n+15*A*a*b^2*c*(x^n \\
& )^2*m+39*A*a*b^2*c*(x^n)^2*n+42*A*a^2*b*c*x^n*n+36*B*a*b^2*c*(x^n)^3*n+56*A \\
& *a^3*d*m*n*x^n+56*B*a^3*c*m*n*x^n+15*B*a^2*b*c*(x^n)^2*m+39*B*a^2*b*c*(x^n) \\
& ^2*n+15*A*a^2*b*c*x^n*m+B*b^3*c*(x^n)^4+A*b^3*c*(x^n)^3+B*a^3*d*(x^n)^2+A*a \\
& ^3*d*x^n+B*a^3*c*x^n+b^3*B*d*(x^n)^5+A*b^3*d*(x^n)^4+10*A*a^3*c*m^3+225*A*a \\
& ^3*c*n^3+10*A*a^3*c*m^2+85*A*a^3*c*n^2+A*a^3*c*m^5+5*A*a^3*c*m^4+274*A*a^3* \\
& c*n^4+120*A*a^3*c*n^5+5*a^3*A*c*m+15*a^3*A*c*n+90*B*a*b^2*d*m*n^4*(x^n)^4+3 \\
& 6*A*a*b^2*d*m^4*n*(x^n)^3+147*A*a*b^2*d*m^3*n^2*(x^n)^3+234*A*a*b^2*d*m^2*n \\
& ^3*(x^n)^3+a^3*A*c+468*B*a^2*b*d*m*n^3*(x^n)^3+144*A*a*b^2*d*m*n*(x^n)^3+23 \\
& 4*B*a^2*b*c*m^2*n*(x^n)^2+531*B*a^2*b*c*m*n^2*(x^n)^2+144*B*a^2*b*d*m*n*(x \\
& ^n)^3+144*B*a*b^2*c*m*n*(x^n)^3+3*(x^n)^3*B*a^2*b*d+3*(x^n)^4*B*a*b^2*d+156* \\
& A*a^2*b*d*m^3*n*(x^n)^2+531*A*a^2*b*d*m^2*n^2*(x^n)^2+642*A*a^2*b*d*m*n^3*( \\
& x^n)^2+156*A*a*b^2*c*m^3*n*(x^n)^2+531*A*a*b^2*c*m^2*n^2*(x^n)^2+642*A*a*b^ \\
& 2*c*m*n^3*(x^n)^2+216*A*a*b^2*d*m^2*n*(x^n)^3+441*A*a*b^2*d*m*n^2*(x^n)^3+2 \\
& 52*A*a^2*b*c*m^2*n*x^n+639*A*a^2*b*c*m*n^2*x^n+156*A*a^2*b*d*m*n*(x^n)^2+15 \\
& 6*A*a*b^2*c*m*n*(x^n)^2+156*B*a^2*b*c*m^3*n*(x^n)^2+531*B*a^2*b*c*m^2*n^2*( \\
& x^n)^2+642*B*a^2*b*c*m*n^3*(x^n)^2+216*B*a^2*b*d*m^2*n*(x^n)^3+369*B*a*b^2* \\
& d*m^2*n^2*(x^n)^4+366*B*a*b^2*d*m*n^3*(x^n)^4+39*A*a^2*b*d*m^4*n*(x^n)^2+17 \\
& 7*A*a^2*b*d*m^3*n^2*(x^n)^2+321*A*a^2*b*d*m^2*n^3*(x^n)^2+321*B*a^2*b*c*m^2 \\
& *n^3*(x^n)^2+180*B*a^2*b*c*m*n^4*(x^n)^2+144*B*a^2*b*d*m^3*n*(x^n)^3+441*B* \\
& a^2*b*d*m^2*n^2*(x^n)^3+33*B*a*b^2*d*m^4*n*(x^n)^4+123*B*a*b^2*d*m^3*n^2*(x \\
& ^n)^4+183*B*a*b^2*d*m^2*n^3*(x^n)^4+42*A*a^2*b*c*m^4*n*x^n+213*A*a^2*b*c*m^ \\
& 3*n^2*x^n+462*A*a^2*b*c*m^2*n^3*x^n+360*A*a^2*b*c*m*n^4*x^n+639*A*a^2*b*c*m \\
& ^2*n^2*x^n+924*A*a^2*b*c*m*n^3*x^n+234*A*a^2*b*d*m^2*n*(x^n)^2+531*A*a^2*b* \\
& d*m*n^2*(x^n)^2+234*A*a*b^2*c*m^2*n*(x^n)^2+531*A*a*b^2*c*m*n^2*(x^n)^2+120 \\
& *A*a*b^2*d*m*n^4*(x^n)^3+36*B*a^2*b*d*m^4*n*(x^n)^3+147*B*a^2*b*d*m^3*n^2*( \\
& x^n)^3+180*A*a^2*b*d*m*n^4*(x^n)^2+39*A*a*b^2*c*m^4*n*(x^n)^2+177*A*a*b^2*c \\
& *m^3*n^2*(x^n)^2+321*A*a*b^2*c*m^2*n^3*(x^n)^2+180*A*a*b^2*c*m*n^4*(x^n)^2+ \\
& 144*A*a*b^2*d*m^3*n*(x^n)^3+441*A*a*b^2*d*m^2*n^2*(x^n)^3+468*A*a*b^2*d*m*n \\
& ^3*(x^n)^3+39*B*a^2*b*c*m^4*n*(x^n)^2+177*B*a^2*b*c*m^3*n^2*(x^n)^2+156*B*a \\
& ^2*b*c*m*n*(x^n)^2+168*A*a^2*b*c*m*n*x^n+234*B*a^2*b*d*m^2*n^3*(x^n)^3+120* \\
& B*a^2*b*d*m*n^4*(x^n)^3+36*B*a*b^2*c*m^4*n*(x^n)^3+147*B*a*b^2*c*m^3*n^2*(x \\
& ^n)^3+234*B*a*b^2*c*m^2*n^3*(x^n)^3+120*B*a*b^2*c*m*n^4*(x^n)^3+132*B*a*b^2 \\
& *d*m^3*n*(x^n)^4+144*B*a*b^2*c*m^3*n*(x^n)^3+441*B*a*b^2*c*m^2*n^2*(x^n)^3+ \\
& 468*B*a*b^2*c*m*n^3*(x^n)^3+198*B*a*b^2*d*m^2*n*(x^n)^4+369*B*a*b^2*d*m*n^2 \\
& *(x^n)^4+441*B*a^2*b*d*m*n^2*(x^n)^3+216*B*a*b^2*c*m^2*n*(x^n)^3+441*B*a*b^ \\
& 2*c*m*n^2*(x^n)^3+132*B*a*b^2*d*m*n*(x^n)^4+168*A*a^2*b*c*m^3*n*x^n+107*B*a \\
& ^3*d*n^3*(x^n)^2+5*B*b^3*c*(x^n)^4+m+3*(x^n)^2*d*a^2*b*A+3*(x^n)^2*c*a*b^2* \\
& A+3*(x^n)^3*A*a*b^2*d+10*B*b^3*d*m^3*(x^n)^5+50*B*b^3*d*n^3*(x^n)^5+5*A*b^3 \\
& *c*m^4*(x^n)^3+40*A*b^3*c*n^4*(x^n)^3+10*A*b^3*d*m^3*(x^n)^4+61*A*b^3*d*n^3 \\
& *(x^n)^4+B*a^3*d*m^5*(x^n)^2+10*B*b^3*c*m^3*(x^n)^4+61*B*b^3*c*n^3*(x^n)^4+ \\
& 10*B*b^3*d*m^2*(x^n)^5+35*B*b^3*d*n^2*(x^n)^5+A*a^3*d*m^5*x^n+5*B*a^3*c*m^4 \\
& *x^n+120*B*a^3*c*n^4*x^n+10*A*a^3*d*m^3*x^n+3*(x^n)^2*c*a^2*b*B+3*x^n*c*a^2 \\
& *b*A+3*(x^n)^3*B*a*b^2*c+10*B*a^3*c*m^3*x^n+154*B*a^3*c*n^3*x^n+10*B*a^3*d* \\
& m^2*(x^n)^2+59*B*a^3*d*n^2*(x^n)^2+10*A*a^3*d*m^2*x^n+71*A*a^3*d*n^2*x^n+10 \\
& *B*a^3*c*m^2*x^n+71*B*a^3*c*n^2*x^n+5*B*a^3*d*(x^n)^2*m+13*B*a^3*d*(x^n)^2* \\
& n+B*b^3*d*m^5*(x^n)^5+11*B*b^3*c*(x^n)^4*n+154*A*a^3*d*n^3*x^n+450*A*a^3*c* \\
& m*n^3+90*A*a^3*c*m^2*n+255*A*a^3*c*m*n^2+60*A*a^3*c*m*n+274*A*a^3*c*m*n^4+6
\end{aligned}$$



$$0 \cdot A \cdot a^3 \cdot c \cdot m^3 \cdot n + 255 \cdot A \cdot a^3 \cdot c \cdot m^2 \cdot n^2 + 15 \cdot A \cdot a^3 \cdot c \cdot m^4 \cdot n + 85 \cdot A \cdot a^3 \cdot c \cdot m^3 \cdot n^2 + 225 \cdot A \cdot a^3 \cdot c \cdot m^2 \cdot n^3 + A \cdot b^3 \cdot d \cdot m^5 \cdot (x^n)^4 + B \cdot b^3 \cdot c \cdot m^5 \cdot (x^n)^4 + 5 \cdot B \cdot b^3 \cdot d \cdot m^4 \cdot (x^n)^5 + 24 \cdot B \cdot b^3 \cdot d \cdot n^4 \cdot (x^n)^5 + A \cdot b^3 \cdot c \cdot m^5 \cdot (x^n)^3 + 5 \cdot A \cdot b^3 \cdot d \cdot m^4 \cdot (x^n)^4 + 30 \cdot A \cdot b^3 \cdot d \cdot n^4 \cdot (x^n)^4 + 5 \cdot B \cdot b^3 \cdot c \cdot m^4 \cdot (x^n)^4 + 30 \cdot B \cdot b^3 \cdot c \cdot n^4 \cdot (x^n)^4 + 5 \cdot B \cdot a^3 \cdot c \cdot x^n \cdot m + 14 \cdot B \cdot a^3 \cdot c \cdot x^n \cdot n + 10 \cdot A \cdot b^3 \cdot c \cdot m^3 \cdot (x^n)^3 + 78 \cdot A \cdot b^3 \cdot c \cdot n^3 \cdot (x^n)^3 + 10 \cdot A \cdot b^3 \cdot d \cdot m^2 \cdot (x^n)^4 + 41 \cdot A \cdot b^3 \cdot d \cdot n^2 \cdot (x^n)^4 + B \cdot a^3 \cdot c \cdot m^5 \cdot x^n + 5 \cdot B \cdot a^3 \cdot d \cdot m^4 \cdot (x^n)^2 + 60 \cdot B \cdot a^3 \cdot d \cdot n^4 \cdot (x^n)^2 + 10 \cdot B \cdot b^3 \cdot c \cdot m^2 \cdot (x^n)^4 + 120 \cdot A \cdot a^3 \cdot d \cdot n^4 \cdot x^n + 10 \cdot A \cdot b^3 \cdot c \cdot m^2 \cdot (x^n)^3 + 49 \cdot A \cdot b^3 \cdot c \cdot n^2 \cdot (x^n)^3 + 5 \cdot A \cdot b^3 \cdot d \cdot (x^n)^4 \cdot m + 11 \cdot A \cdot b^3 \cdot d \cdot (x^n)^4 \cdot n + 5 \cdot A \cdot b^3 \cdot c \cdot (x^n)^3 \cdot m + 12 \cdot A \cdot b^3 \cdot c \cdot (x^n)^3 \cdot n + 41 \cdot B \cdot b^3 \cdot c \cdot n^2 \cdot (x^n)^4 + 5 \cdot m \cdot b^3 \cdot B \cdot d \cdot (x^n)^5 + 10 \cdot b^3 \cdot B \cdot d \cdot (x^n)^5 \cdot n + 5 \cdot A \cdot a^3 \cdot d \cdot m^4 \cdot x^n + 10 \cdot B \cdot a^3 \cdot d \cdot m^3 \cdot (x^n)^2 + 5 \cdot A \cdot a^3 \cdot d \cdot x^n \cdot m + 14 \cdot A \cdot a^3 \cdot d \cdot x^n \cdot n) / (m+1) / (m+n+1) / (m+2n+1) / (m+3n+1) / (1+m+4n) / (1+m+5n) \cdot \exp(1/2 \cdot m \cdot (-I \cdot \text{Pi} \cdot \text{csgn}(I \cdot e \cdot x)^3 + I \cdot \text{Pi} \cdot \text{csgn}(I \cdot e \cdot x)^2 \cdot \text{csgn}(I \cdot e) + I \cdot \text{Pi} \cdot \text{csgn}(I \cdot e \cdot x)^2 \cdot \text{csgn}(I \cdot x) - I \cdot \text{Pi} \cdot \text{csgn}(I \cdot e \cdot x) \cdot \text{csgn}(I \cdot e) \cdot \text{csgn}(I \cdot x) + 2 \cdot \ln(e) + 2 \cdot \ln(x)))$$

**maxima** [B] time = 0.94, size = 464, normalized size = 2.21

---

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="maxima")

[Out]  $B \cdot b^3 \cdot d \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 5 \cdot n \cdot \log(x)) / (m + 5 \cdot n + 1)} + B \cdot b^3 \cdot c \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 4 \cdot n \cdot \log(x)) / (m + 4 \cdot n + 1)} + 3 \cdot B \cdot a \cdot b^2 \cdot d \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 4 \cdot n \cdot \log(x)) / (m + 4 \cdot n + 1)} + A \cdot b^3 \cdot d \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 4 \cdot n \cdot \log(x)) / (m + 4 \cdot n + 1)} + 3 \cdot B \cdot a \cdot b^2 \cdot c \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 3 \cdot n \cdot \log(x)) / (m + 3 \cdot n + 1)} + A \cdot b^3 \cdot c \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 3 \cdot n \cdot \log(x)) / (m + 3 \cdot n + 1)} + 3 \cdot B \cdot a^2 \cdot b \cdot d \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 3 \cdot n \cdot \log(x)) / (m + 3 \cdot n + 1)} + 3 \cdot A \cdot a \cdot b^2 \cdot d \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 3 \cdot n \cdot \log(x)) / (m + 3 \cdot n + 1)} + 3 \cdot B \cdot a^2 \cdot b \cdot c \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 2 \cdot n \cdot \log(x)) / (m + 2 \cdot n + 1)} + 3 \cdot A \cdot a \cdot b^2 \cdot c \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 2 \cdot n \cdot \log(x)) / (m + 2 \cdot n + 1)} + B \cdot a^3 \cdot d \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 2 \cdot n \cdot \log(x)) / (m + 2 \cdot n + 1)} + 3 \cdot A \cdot a^2 \cdot b \cdot d \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 2 \cdot n \cdot \log(x)) / (m + 2 \cdot n + 1)} + 3 \cdot A \cdot a^2 \cdot b \cdot c \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + 2 \cdot n \cdot \log(x)) / (m + 2 \cdot n + 1)} + B \cdot a^3 \cdot c \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + n \cdot \log(x)) / (m + n + 1)} + 3 \cdot A \cdot a^2 \cdot b \cdot c \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + n \cdot \log(x)) / (m + n + 1)} + A \cdot a^3 \cdot d \cdot e^m \cdot x \cdot e^{(m \cdot \log(x) + n \cdot \log(x)) / (m + n + 1)} + (e \cdot x)^{(m + 1)} \cdot A \cdot a^3 \cdot c / (e \cdot (m + 1))$

**mupad** [B] time = 5.64, size = 1089, normalized size = 5.19

---

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^3\*(c + d\*x^n),x)

[Out]  $(A \cdot a^3 \cdot c \cdot x \cdot (e \cdot x)^m) / (m + 1) + (b^2 \cdot x \cdot x^{(4 \cdot n)} \cdot (e \cdot x)^m \cdot (A \cdot b \cdot d + 3 \cdot B \cdot a \cdot d + B \cdot b \cdot c) \cdot (4 \cdot m + 11 \cdot n + 33 \cdot m \cdot n + 82 \cdot m \cdot n^2 + 33 \cdot m^2 \cdot n + 61 \cdot m \cdot n^3 + 11 \cdot m^3 \cdot n + 6 \cdot m^2 + 4 \cdot m^3 + m^4 + 41 \cdot n^2 + 61 \cdot n^3 + 30 \cdot n^4 + 41 \cdot m^2 \cdot n^2 + 1)) / (5 \cdot m + 15 \cdot n + 60 \cdot m \cdot n + 255 \cdot m \cdot n^2 + 90 \cdot m^2 \cdot n + 450 \cdot m \cdot n^3 + 60 \cdot m^3 \cdot n + 274 \cdot m \cdot n^4 + 15 \cdot m^4 \cdot n + 10 \cdot m^2 + 10 \cdot m^3 + 5 \cdot m^4 + m^5 + 85 \cdot n^2 + 225 \cdot n^3 + 274 \cdot n^4 + 120 \cdot n^5 + 255 \cdot m^2 \cdot n^2 + 225 \cdot m^2 \cdot n^3 + 85 \cdot m^3 \cdot n^2 + 1) + (a \cdot x \cdot x^{(2 \cdot n)} \cdot (e \cdot x)^m \cdot (3 \cdot A \cdot b^2 \cdot c + B \cdot a^2 \cdot d + 3 \cdot A \cdot a \cdot b \cdot d + 3 \cdot B \cdot a \cdot b \cdot c) \cdot (4 \cdot m + 13 \cdot n + 39 \cdot m \cdot n + 118 \cdot m \cdot n^2 + 39 \cdot m^2 \cdot n + 107 \cdot m \cdot n^3 + 13 \cdot m^3 \cdot n + 6 \cdot m^2 + 4 \cdot m^3 + m^4 + 59 \cdot n^2 + 107 \cdot n^3 + 60 \cdot n^4 + 59 \cdot m^2 \cdot n^2 + 1)) / (5 \cdot m + 15 \cdot n + 60 \cdot m \cdot n + 255 \cdot m \cdot n^2 + 90 \cdot m^2 \cdot n + 450 \cdot m \cdot n^3 + 60 \cdot m^3 \cdot n + 274 \cdot m \cdot n^4 + 15 \cdot m^4 \cdot n + 10 \cdot m^2 + 10 \cdot m^3 + 5 \cdot m^4 + m^5 + 85 \cdot n^2 + 225 \cdot n^3 + 274 \cdot n^4 + 120 \cdot n^5 + 255 \cdot m^2 \cdot n^2 + 225 \cdot m^2 \cdot n^3 + 85 \cdot m^3 \cdot n^2 + 1) + (b \cdot x \cdot x^{(3 \cdot n)} \cdot (e \cdot x)^m \cdot (A \cdot b^2 \cdot c + 3 \cdot B \cdot a^2 \cdot d + 3 \cdot A \cdot a \cdot b \cdot d + 3 \cdot B \cdot a \cdot b \cdot c) \cdot (4 \cdot m + 12 \cdot n + 36 \cdot m \cdot n + 98 \cdot m \cdot n^2 + 36 \cdot m^2 \cdot n + 78 \cdot m \cdot n^3 + 12 \cdot m^3 \cdot n + 6 \cdot m^2 + 4 \cdot m^3 + m^4 + 49 \cdot n^2 + 78 \cdot n^3 + 40 \cdot n^4 + 49 \cdot m^2 \cdot n^2 + 1)) / (5 \cdot m + 15 \cdot n + 60 \cdot m \cdot n + 255 \cdot m \cdot n^2 + 90 \cdot m^2 \cdot n + 450 \cdot m \cdot n^3 + 60 \cdot m^3 \cdot n + 274 \cdot m \cdot n^4 + 15 \cdot m^4 \cdot n + 10 \cdot m^2 + 10 \cdot m^3 + 5 \cdot m^4 + m^5 + 85 \cdot n^2 + 225 \cdot n^3 + 274 \cdot n^4 + 120 \cdot n^5 + 255 \cdot m^2 \cdot n^2 + 225 \cdot m^2 \cdot n^3 + 85 \cdot m^3 \cdot n^2 + 1) + (a^2 \cdot x \cdot x^{(n)} \cdot (e \cdot x)^m \cdot (A \cdot a \cdot d + 3 \cdot A \cdot b$

```
*c + B*a*c)*(4*m + 14*n + 42*m*n + 142*m*n^2 + 42*m^2*n + 154*m*n^3 + 14*m^3*n + 6*m^2 + 4*m^3 + m^4 + 71*n^2 + 154*n^3 + 120*n^4 + 71*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (B*b^3*d*x*x^(5*n)*(e*x)^m*(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1)
```

**sympy** [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*3\*(A+B\*x\*\*n)\*(c+d\*x\*\*n),x)

[Out] Timed out

### 3.2 $\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n) dx$

**Optimal.** Leaf size=160

$$\frac{a^2 Ac(ex)^{m+1}}{e(m+1)} + \frac{ax^{n+1}(ex)^m(aAd + aBc + 2Abc)}{m+n+1} + \frac{x^{2n+1}(ex)^m(Ab(2ad + bc) + aB(ad + 2bc))}{m+2n+1} + \frac{bx^{3n+1}(ex)^m(2aBc + aBd + 2Abd)}{m+3n+1}$$

**Rubi [A]** time = 0.18, antiderivative size = 160, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ , Rules used = {570, 20, 30}

$$\frac{a^2 Ac(ex)^{m+1}}{e(m+1)} + \frac{ax^{n+1}(ex)^m(aAd + aBc + 2Abc)}{m+n+1} + \frac{x^{2n+1}(ex)^m(Ab(2ad + bc) + aB(ad + 2bc))}{m+2n+1} + \frac{bx^{3n+1}(ex)^m(2aBd + Abd + bBc)}{m+3n+1} + \frac{b^2 Bdx^{4n+1}(ex)^m}{m+4n+1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n), x]

[Out] (a\*(2\*A\*b\*c + a\*B\*c + a\*A\*d)\*x^(1 + n)\*(e\*x)^m)/(1 + m + n) + ((a\*B\*(2\*b\*c + a\*d) + A\*b\*(b\*c + 2\*a\*d))\*x^(1 + 2\*n)\*(e\*x)^m)/(1 + m + 2\*n) + (b\*(b\*B\*c + A\*b\*d + 2\*a\*B\*d)\*x^(1 + 3\*n)\*(e\*x)^m)/(1 + m + 3\*n) + (b^2\*B\*d\*x^(1 + 4\*n)\*(e\*x)^m)/(1 + m + 4\*n) + (a^2\*A\*c\*(e\*x)^(1 + m))/(e\*(1 + m))

Rule 20

Int[(u\_.)\*((a\_.)\*(v\_.))^(m\_.)\*((b\_.)\*(v\_.))^(n\_.), x\_Symbol] :> Dist[(b^IntPart[n]\*(b\*v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

Rule 30

Int[(x\_)^(m\_.), x\_Symbol] :> Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 570

Int[((g\_.)\*(x\_.))^(m\_.)\*((a\_.) + (b\_.)\*(x\_.)^(n\_.))^(p\_.)\*((c\_.) + (d\_.)\*(x\_.)^(n\_.))^(q\_.)\*((e\_.) + (f\_.)\*(x\_.)^(n\_.))^(r\_.), x\_Symbol] :> Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n) dx &= \int (a^2 Ac(ex)^m + a(2Abc + aBc + aAd)x^n(ex)^m + (aB(2bc + ad) + a^2 Bc)x^{2n}(ex)^m + (b^2 Bd + a^2 Ad)x^{3n}(ex)^m + a^2 Bdx^{4n}(ex)^m) dx \\ &= \frac{a^2 Ac(ex)^{1+m}}{e(1+m)} + (b^2 Bd) \int x^{4n}(ex)^m dx + (a(2Abc + aBc + aAd)) \int x^n(ex)^m dx \\ &= \frac{a^2 Ac(ex)^{1+m}}{e(1+m)} + (b^2 Bdx^{-m}(ex)^m) \int x^{m+4n} dx + (a(2Abc + aBc + aAd)) \int x^{m+n} dx \\ &= \frac{a(2Abc + aBc + aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{(aB(2bc + ad) + Ab(bc + 2ad))x^{m+4n+1}(ex)^m}{1+m+2n} \end{aligned}$$

**Mathematica [A]** time = 0.53, size = 129, normalized size = 0.81

$$x(ex)^m \left( \frac{a^2 Ac}{m+1} + \frac{x^{2n}(Ab(2ad + bc) + aB(ad + 2bc))}{m+2n+1} + \frac{bx^{3n}(2aBd + Abd + bBc)}{m+3n+1} + \frac{ax^n(aAd + aBc + 2Abc)}{m+n+1} + \frac{b^2 Bdx^{4n}}{m+4n+1} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n), x]

[Out] x\*(e\*x)^m\*((a^2\*A\*c)/(1 + m) + (a\*(2\*A\*b\*c + a\*B\*c + a\*A\*d)\*x^n)/(1 + m + n) + ((a\*B\*(2\*b\*c + a\*d) + A\*b\*(b\*c + 2\*a\*d))\*x^(2\*n))/(1 + m + 2\*n) + (b\*(b\*B\*c + A\*b\*d + 2\*a\*B\*d)\*x^(3\*n))/(1 + m + 3\*n) + (b^2\*B\*d\*x^(4\*n))/(1 + m + 4\*n))

**IntegrateAlgebraic** [F] time = 0.17, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n) dx$$

Verification is not applicable to the result.

[In] IntegrateAlgebraic[(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n), x]

[Out] Defer[IntegrateAlgebraic] [(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n), x]

**fricas** [B] time = 0.49, size = 1524, normalized size = 9.52

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n), x, algorithm="fricas")

[Out] ((B\*b^2\*d\*m^4 + 4\*B\*b^2\*d\*m^3 + 6\*B\*b^2\*d\*m^2 + 4\*B\*b^2\*d\*m + B\*b^2\*d + 6\*(B\*b^2\*d\*m + B\*b^2\*d)\*n^3 + 11\*(B\*b^2\*d\*m^2 + 2\*B\*b^2\*d\*m + B\*b^2\*d)\*n^2 + 6\*(B\*b^2\*d\*m^3 + 3\*B\*b^2\*d\*m^2 + 3\*B\*b^2\*d\*m + B\*b^2\*d)\*n)\*x\*x^(4\*n)\*e^(m\*log(e) + m\*log(x)) + ((B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^4 + B\*b^2\*c + 4\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^3 + 8\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d) + (B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m)\*n^3 + 6\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^2 + 14\*(B\*b^2\*c + (B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^2 + (2\*B\*a\*b + A\*b^2)\*d + 2\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m)\*n^2 + (2\*B\*a\*b + A\*b^2)\*d + 4\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m + 7\*(B\*b^2\*c + (B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^3 + 3\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^2 + (2\*B\*a\*b + A\*b^2)\*d + 3\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m)\*n)\*x\*x^(3\*n)\*e^(m\*log(e) + m\*log(x)) + (((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^4 + 4\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^3 + 12\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d) + ((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m)\*n^3 + 6\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^2 + 19\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d) + 2\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m)\*n^2 + (2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d + 4\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m + 8\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^3 + 3\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^2 + (2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d + 3\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m)\*n)\*x\*x^(2\*n)\*e^(m\*log(e) + m\*log(x)) + ((A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m^4 + A\*a^2\*d + 4\*(A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m^3 + 24\*(A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c) + (A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m)\*n^3 + 6\*(A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m^2 + 26\*(A\*a^2\*d + (A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m^2 + (B\*a^2 + 2\*A\*a\*b)\*c + 2\*(A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m)\*n^2 + (B\*a^2 + 2\*A\*a\*b)\*c + 4\*(A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m + 9\*(A\*a^2\*d + (A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m^3 + 3\*(A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m^2 + (B\*a^2 + 2\*A\*a\*b)\*c + 3\*(A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m)\*n)\*x\*x^n\*e^(m\*log(e) + m\*log(x)) + (A\*a^2\*c\*m^4 + 24\*A\*a^2\*c\*n^4 + 4\*A\*a^2\*c\*m^3 + 6\*A\*a^2\*c\*m^2 + 4\*A\*a^2\*c\*m + A\*a^2\*c + 50\*(A\*a^2\*c\*m + A\*a^2\*c)\*n^3 + 35\*(A\*a^2\*c\*m^2 + 2\*A\*a^2\*c\*m + A\*a^2\*c)\*n^2 + 10\*(A\*a^2\*c\*m^3 + 3\*A\*a^2\*c\*m^2 + 3\*A\*a^2\*c\*m + A\*a^2\*c)\*n)\*x\*e^(m\*log(e) + m\*log(x)))/(m^5 + 24\*(m + 1)\*n^4 + 5\*m^4 + 50\*(m^2 + 2\*m + 1)\*n^3 + 10\*m^3 + 35\*(m^3 + 3\*m^2 + 3\*m + 1)\*n^2 + 10\*m^2 + 10\*(m^4 + 4\*m^3 + 6\*m^2 + 4\*m + 1)\*n + 5\*m + 1)

**giac** [B] time = 0.81, size = 3415, normalized size = 21.34

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^2*(A+B*x^n)*(c+d*x^n),x, algorithm="giac")
[Out] (B*b^2*d*m^4*x*x^m*x^(4*n)*e^m + 6*B*b^2*d*m^3*n*x*x^m*x^(4*n)*e^m + 11*B*b^2*d*m^2*n^2*x*x^m*x^(4*n)*e^m + 6*B*b^2*d*m*n^3*x*x^m*x^(4*n)*e^m + B*b^2*c*m^4*x*x^m*x^(3*n)*e^m + 2*B*a*b*d*m^4*x*x^m*x^(3*n)*e^m + A*b^2*d*m^4*x*x^m*x^(3*n)*e^m + 7*B*b^2*c*m^3*n*x*x^m*x^(3*n)*e^m + 14*B*a*b*d*m^3*n*x*x^m*x^(3*n)*e^m + 7*A*b^2*d*m^3*n*x*x^m*x^(3*n)*e^m + 14*B*b^2*c*m^2*n^2*x*x^m*x^(3*n)*e^m + 28*B*a*b*d*m^2*n^2*x*x^m*x^(3*n)*e^m + 14*A*b^2*d*m^2*n^2*x*x^m*x^(3*n)*e^m + 8*B*b^2*c*m*n^3*x*x^m*x^(3*n)*e^m + 16*B*a*b*d*m*n^3*x*x^m*x^(3*n)*e^m + 8*A*b^2*d*m*n^3*x*x^m*x^(3*n)*e^m + 2*B*a*b*c*m^4*x*x^m*x^(2*n)*e^m + A*b^2*c*m^4*x*x^m*x^(2*n)*e^m + B*a^2*d*m^4*x*x^m*x^(2*n)*e^m + 2*A*a*b*d*m^4*x*x^m*x^(2*n)*e^m + 16*B*a*b*c*m^3*n*x*x^m*x^(2*n)*e^m + 8*A*b^2*c*m^3*n*x*x^m*x^(2*n)*e^m + 8*B*a^2*d*m^3*n*x*x^m*x^(2*n)*e^m + 16*A*a*b*d*m^3*n*x*x^m*x^(2*n)*e^m + 38*B*a*b*c*m^2*n^2*x*x^m*x^(2*n)*e^m + 19*A*b^2*c*m^2*n^2*x*x^m*x^(2*n)*e^m + 19*B*a^2*d*m^2*n^2*x*x^m*x^(2*n)*e^m + 38*A*a*b*d*m^2*n^2*x*x^m*x^(2*n)*e^m + 24*B*a*b*c*m*n^3*x*x^m*x^(2*n)*e^m + 12*A*b^2*c*m*n^3*x*x^m*x^(2*n)*e^m + 12*B*a^2*d*m*n^3*x*x^m*x^(2*n)*e^m + 24*A*a*b*d*m*n^3*x*x^m*x^(2*n)*e^m + B*a^2*c*m^4*x*x^m*x^n*e^m + 2*A*a*b*c*m^4*x*x^m*x^n*e^m + A*a^2*d*m^4*x*x^m*x^n*e^m + 9*B*a^2*c*m^3*n*x*x^m*x^n*e^m + 18*A*a*b*c*m^3*n*x*x^m*x^n*e^m + 9*A*a^2*d*m^3*n*x*x^m*x^n*e^m + 26*B*a^2*c*m^2*n^2*x*x^m*x^n*e^m + 52*A*a*b*c*m^2*n^2*x*x^m*x^n*e^m + 26*A*a^2*d*m^2*n^2*x*x^m*x^n*e^m + 24*B*a^2*c*m*n^3*x*x^m*x^n*e^m + 48*A*a*b*c*m*n^3*x*x^m*x^n*e^m + 24*A*a^2*d*m*n^3*x*x^m*x^n*e^m + A*a^2*c*m^4*x*x^m*x^n*e^m + 10*A*a^2*c*m^3*n*x*x^m*x^n*e^m + 35*A*a^2*c*m^2*n^2*x*x^m*x^n*e^m + 50*A*a^2*c*m*n^3*x*x^m*x^n*e^m + 24*A*a^2*c*n^4*x*x^m*x^n*e^m + 4*B*b^2*d*m^3*x*x^m*x^(4*n)*e^m + 18*B*b^2*d*m^2*n*x*x^m*x^(4*n)*e^m + 22*B*b^2*d*m*n^2*x*x^m*x^(4*n)*e^m + 6*B*b^2*d*n^3*x*x^m*x^(4*n)*e^m + 4*B*b^2*c*m^3*x*x^m*x^(3*n)*e^m + 8*B*a*b*d*m^3*x*x^m*x^(3*n)*e^m + 4*A*b^2*d*m^3*x*x^m*x^(3*n)*e^m + 21*B*b^2*c*m^2*n*x*x^m*x^(3*n)*e^m + 42*B*a*b*d*m^2*n*x*x^m*x^(3*n)*e^m + 21*A*b^2*d*m^2*n*x*x^m*x^(3*n)*e^m + 28*B*b^2*c*m*n^2*x*x^m*x^(3*n)*e^m + 56*B*a*b*d*m*n^2*x*x^m*x^(3*n)*e^m + 28*A*b^2*d*m*n^2*x*x^m*x^(3*n)*e^m + 8*B*b^2*c*n^3*x*x^m*x^(3*n)*e^m + 16*B*a*b*d*n^3*x*x^m*x^(3*n)*e^m + 8*A*b^2*d*n^3*x*x^m*x^(3*n)*e^m + 8*B*a*b*c*m^3*x*x^m*x^(2*n)*e^m + 4*A*b^2*c*m^3*x*x^m*x^(2*n)*e^m + 4*B*a^2*d*m^3*x*x^m*x^(2*n)*e^m + 8*A*a*b*d*m^3*x*x^m*x^(2*n)*e^m + 48*B*a*b*c*m^2*n*x*x^m*x^(2*n)*e^m + 24*A*b^2*c*m^2*n*x*x^m*x^(2*n)*e^m + 24*B*a^2*d*m^2*n*x*x^m*x^(2*n)*e^m + 48*A*a*b*d*m^2*n*x*x^m*x^(2*n)*e^m + 76*B*a*b*c*m*n^2*x*x^m*x^(2*n)*e^m + 38*A*b^2*c*m*n^2*x*x^m*x^(2*n)*e^m + 38*B*a^2*d*m*n^2*x*x^m*x^(2*n)*e^m + 76*A*a*b*d*m*n^2*x*x^m*x^(2*n)*e^m + 24*B*a*b*c*n^3*x*x^m*x^(2*n)*e^m + 12*A*b^2*c*n^3*x*x^m*x^(2*n)*e^m + 12*B*a^2*d*n^3*x*x^m*x^(2*n)*e^m + 24*A*a*b*d*n^3*x*x^m*x^(2*n)*e^m + 4*B*a^2*c*m^3*x*x^m*x^n*e^m + 8*A*a*b*c*m^3*x*x^m*x^n*e^m + 4*A*a^2*d*m^3*x*x^m*x^n*e^m + 27*B*a^2*c*m^2*n*x*x^m*x^n*e^m + 54*A*a*b*c*m^2*n*x*x^m*x^n*e^m + 27*A*a^2*d*m^2*n*x*x^m*x^n*e^m + 52*B*a^2*c*m*n^2*x*x^m*x^n*e^m + 104*A*a*b*c*m*n^2*x*x^m*x^n*e^m + 52*A*a^2*d*m*n^2*x*x^m*x^n*e^m + 24*B*a^2*c*n^3*x*x^m*x^n*e^m + 48*A*a*b*c*n^3*x*x^m*x^n*e^m + 24*A*a^2*d*n^3*x*x^m*x^n*e^m + 4*A*a^2*c*m^3*x*x^m*x^n*e^m + 30*A*a^2*c*m^2*n*x*x^m*x^n*e^m + 70*A*a^2*c*m*n^2*x*x^m*x^n*e^m + 50*A*a^2*c*n^3*x*x^m*x^n*e^m + 6*B*b^2*d*m^2*x*x^m*x^(4*n)*e^m + 18*B*b^2*d*m*n*x*x^m*x^(4*n)*e^m + 11*B*b^2*d*n^2*x*x^m*x^(4*n)*e^m + 6*B*b^2*c*m^2*x*x^m*x^(3*n)*e^m + 12*B*a*b*d*m^2*x*x^m*x^(3*n)*e^m + 6*A*b^2*d*m^2*x*x^m*x^(3*n)*e^m + 21*B*b^2*c*m*n*x*x^m*x^(3*n)*e^m + 42*B*a*b*d*m*n*x*x^m*x^(3*n)*e^m + 21*A*b^2*d*m*n*x*x^m*x^(3*n)*e^m + 14*B*b^2*c*n^2*x*x^m*x^(3*n)*e^m + 28*B*a*b*d*n^2*x*x^m*x^(3*n)*e^m + 14*A*b^2*d*n^2*x*x^m*x^(3*n)*e^m + 12*B*a*b*c*m^2*x*x^m*x^(2*n)*e^m + 6*A*b^2*c*m^2*x*x^m*x^(2*n)*e^m + 6*B*a^2*d*m^2*x*x^m*x^(2*n)*e^m + 12*A*a*b*d*m^2*x*x^m*x^(2*n)*e^m + 48*B*a*b*c*m*n*x*x^m*x^(2*n)*e^m + 24*A*b^2*c*m*n*x*x^m*x^(2*n)*e^m + 24*B*a^2*d*m*n*x*x^m*x^(2*n)*e^m + 48*A*a*b*d*m*n*x*x^m*x^(2*n)*e^m + 38*B*a*b*c*n^2*x*x^m*x^(2*n)*e^m +
```

$$\begin{aligned}
& 19*A*b^2*c*n^2*x*x^m*x^{(2*n)}*e^m + 19*B*a^2*d*n^2*x*x^m*x^{(2*n)}*e^m + 38*A* \\
& a*b*d*n^2*x*x^m*x^{(2*n)}*e^m + 6*B*a^2*c*m^2*x*x^m*x^n*e^m + 12*A*a*b*c*m^2* \\
& x*x^m*x^n*e^m + 6*A*a^2*d*m^2*x*x^m*x^n*e^m + 27*B*a^2*c*m*n*x*x^m*x^n*e^m \\
& + 54*A*a*b*c*m*n*x*x^m*x^n*e^m + 27*A*a^2*d*m*n*x*x^m*x^n*e^m + 26*B*a^2*c* \\
& n^2*x*x^m*x^n*e^m + 52*A*a*b*c*n^2*x*x^m*x^n*e^m + 26*A*a^2*d*n^2*x*x^m*x^n \\
& *e^m + 6*A*a^2*c*m^2*x*x^m*e^m + 30*A*a^2*c*m*n*x*x^m*e^m + 35*A*a^2*c*n^2* \\
& x*x^m*e^m + 4*B*b^2*d*m*x*x^m*x^{(4*n)}*e^m + 6*B*b^2*d*n*x*x^m*x^{(4*n)}*e^m + \\
& 4*B*b^2*c*m*x*x^m*x^{(3*n)}*e^m + 8*B*a*b*d*m*x*x^m*x^{(3*n)}*e^m + 4*A*b^2*d* \\
& m*x*x^m*x^{(3*n)}*e^m + 7*B*b^2*c*n*x*x^m*x^{(3*n)}*e^m + 14*B*a*b*d*n*x*x^m*x^{(3*n)}*e^m \\
& + 7*A*b^2*d*n*x*x^m*x^{(3*n)}*e^m + 8*B*a*b*c*m*x*x^m*x^{(2*n)}*e^m + \\
& 4*A*b^2*c*m*x*x^m*x^{(2*n)}*e^m + 4*B*a^2*d*m*x*x^m*x^{(2*n)}*e^m + 8*A*a*b*d* \\
& m*x*x^m*x^{(2*n)}*e^m + 16*B*a*b*c*n*x*x^m*x^{(2*n)}*e^m + 8*A*b^2*c*n*x*x^m*x^{(2*n)}*e^m \\
& + 8*B*a^2*d*n*x*x^m*x^{(2*n)}*e^m + 16*A*a*b*d*n*x*x^m*x^{(2*n)}*e^m \\
& + 4*B*a^2*c*m*x*x^m*x^n*e^m + 8*A*a*b*c*m*x*x^m*x^n*e^m + 4*A*a^2*d*m*x*x^m \\
& *x^n*e^m + 9*B*a^2*c*n*x*x^m*x^n*e^m + 18*A*a*b*c*n*x*x^m*x^n*e^m + 9*A*a^2 \\
& *d*n*x*x^m*x^n*e^m + 4*A*a^2*c*m*x*x^m*e^m + 10*A*a^2*c*n*x*x^m*e^m + B*b^2 \\
& *d*x*x^m*x^{(4*n)}*e^m + B*b^2*c*x*x^m*x^{(3*n)}*e^m + 2*B*a*b*d*x*x^m*x^{(3*n)}* \\
& e^m + A*b^2*d*x*x^m*x^{(3*n)}*e^m + 2*B*a*b*c*x*x^m*x^{(2*n)}*e^m + A*b^2*c*x*x \\
& ^m*x^{(2*n)}*e^m + B*a^2*d*x*x^m*x^{(2*n)}*e^m + 2*A*a*b*d*x*x^m*x^{(2*n)}*e^m + \\
& B*a^2*c*x*x^m*x^n*e^m + 2*A*a*b*c*x*x^m*x^n*e^m + A*a^2*d*x*x^m*x^n*e^m + A \\
& *a^2*c*x*x^m*e^m)/(m^5 + 10*m^4*n + 35*m^3*n^2 + 50*m^2*n^3 + 24*m*n^4 + 5* \\
& m^4 + 40*m^3*n + 105*m^2*n^2 + 100*m*n^3 + 24*n^4 + 10*m^3 + 60*m^2*n + 105 \\
& *m*n^2 + 50*n^3 + 10*m^2 + 40*m*n + 35*n^2 + 5*m + 10*n + 1)
\end{aligned}$$

**maple [C]** time = 0.14, size = 2410, normalized size = 15.06

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((e*x)^m*(b*x^n+a)^2*(A+B*x^n)*(d*x^n+c),x)`

[Out]  $x*(2*B*a*b*d*m^4*(x^n)^3+7*B*b^2*c*m^3*n*(x^n)^3+14*B*b^2*c*m^2*n^2*(x^n)^3+8*B*b^2*c*m*n^3*(x^n)^3+18*B*b^2*d*m^2*n*(x^n)^4+22*B*b^2*d*m*n^2*(x^n)^4+2*A*a*b*d*m^4*(x^n)^2+2*A*a*b*c*m^4*x^n+6*B*b^2*d*m^3*n*(x^n)^4+11*B*b^2*d*m^2*n^2*(x^n)^4+6*B*b^2*d*m*n^3*(x^n)^4+7*A*b^2*d*m^3*n*(x^n)^3+14*A*b^2*d*m^2*n^2*(x^n)^3+8*A*b^2*d*m*n^3*(x^n)^3+9*A*a^2*d*m^3*n*x^n+26*A*a^2*d*m^2*n^2*x^n+24*A*a^2*d*m*n^3*x^n+8*B*a*b*d*m^3*(x^n)^3+16*B*a*b*d*n^3*(x^n)^3+21*B*b^2*c*m^2*n*(x^n)^3+28*B*b^2*c*m*n^2*(x^n)^3+18*B*b^2*d*m*n*(x^n)^4+a^2*A*c+A*b^2*d*(x^n)^3+B*b^2*c*(x^n)^3+A*b^2*c*(x^n)^2+B*a^2*d*(x^n)^2+A*a^2*d*x^n+B*a^2*c*x^n+b^2*B*d*(x^n)^4+35*A*a^2*c*n^2+A*a^2*c*m^4+4*A*a^2*c*m^3+50*A*a^2*c*n^3+6*A*a^2*c*m^2+24*A*a^2*c*n^4+12*B*a^2*d*m*n^3*(x^n)^2+2*B*a*b*c*m^4*(x^n)^2+19*B*a^2*d*m^2*n^2*(x^n)^2+19*A*b^2*c*m^2*n^2*(x^n)^2+12*A*b^2*c*m*n^3*(x^n)^2+21*A*b^2*d*m^2*n*(x^n)^3+28*A*b^2*d*m*n^2*(x^n)^3+8*B*a^2*d*m^3*n*(x^n)^2+24*B*a^2*c*m*n^3*x^n+24*B*a^2*d*m^2*n*(x^n)^2+38*B*a^2*d*m*n^2*(x^n)^2+8*A*b^2*c*m^3*n*(x^n)^2+24*A*b^2*c*m^2*n*(x^n)^2+38*A*b^2*c*m*n^2*(x^n)^2+21*A*b^2*d*m*n*(x^n)^3+9*B*a^2*c*m^3*n*x^n+26*B*a^2*c*m^2*n^2*x^n+8*A*a*b*d*m^3*(x^n)^2+24*A*a*b*d*n^3*(x^n)^2+12*B*a*b*d*m^2*(x^n)^3+28*B*a*b*d*n^2*(x^n)^3+27*B*a^2*c*m^2*n*x^n+8*B*a*b*c*m^3*(x^n)^2+24*B*a*b*c*n^3*(x^n)^2+52*A*a^2*d*m*n^2*x^n+8*A*a*b*c*m^3*x^n+48*A*a*b*c*n^3*x^n+12*A*a*b*d*m^2*(x^n)^2+38*A*a*b*d*n^2*(x^n)^2+24*A*b^2*c*m*n*(x^n)^2+27*A*a^2*d*m*n*x^n+52*B*a^2*c*m*n^2*x^n+24*B*a^2*d*m*n*(x^n)^2+12*B*a*b*c*m^2*(x^n)^2+21*B*b^2*c*m*n*(x^n)^3+27*A*a^2*d*m^2*n*x^n+38*B*a*b*c*n^2*(x^n)^2+8*B*a*b*d*(x^n)^3+m+14*B*a*b*d*(x^n)^3+n+8*A*a*b*d*(x^n)^2+m+16*A*a*b*d*(x^n)^2+n+27*B*a^2*c*m*n*x^n+8*B*a*b*c*(x^n)^2+m+18*A*a*b*c*x^n+n+12*A*a*b*c*m^2*x^n+52*A*a*b*c*n^2*x^n+8*A*a*b*c*x^n*m+16*B*a*b*c*(x^n)^2*n+4*a^2*A*c*m+10*a^2*A*c*n+4*A*b^2*d*(x^n)^3+m+7*A*b^2*d*(x^n)^3+n+4*B*a^2*c*m^3*x^n+24*B*a^2*c*n^3*x^n+6*B*a^2*d*m^2*(x^n)^2+19*B*a^2*d*n^2*(x^n)^2+4*B*b^2*c*(x^n)^3+m+7*B*b^2*c*(x^n)^3+n+6*A*a^2*d*m^2*x^n+4*A*b^2*d*m^3*(x^n)^3+8*A*b^2*d*n^3*(x^n)^3+4*A*a^2*d*x^n*m+9*A*a^2*d*x^n*n+4*B*a^2*c*x^n*m+9*B*a^2*c*x^n*n+54*A*a*b*c*m*n*x^n+38*A*a*b*d*m^2*n^2*(x^n)^2+24*A*a*b*d*m*n^3*(x^n)^2+16*B*a*b*c*$

$$m^3 n (x^n)^2 + 38 B a b c m^2 n^2 (x^n)^2 + 24 B a b c m n^3 (x^n)^2 + 42 B a b c d m^2 n (x^n)^3 + 76 A a b d m n^2 (x^n)^2 + 48 B a b c m^2 n (x^n)^2 + 76 B a b c m n^2 (x^n)^2 + 42 B a b d m n^2 (x^n)^3 + 54 A a b c m^2 n x^n + 104 A a b c m n^2 x^n + 48 A a b d m n^2 (x^n)^2 + 48 B a b c m n^2 (x^n)^2 + 14 B a b d m^3 n (x^n)^3 + 28 B a b d m^2 n^2 (x^n)^3 + 16 B a b d m n^3 (x^n)^3 + 16 A a b d m^3 n (x^n)^2 + 56 B a b d m n^2 (x^n)^3 + 18 A a b c m^3 n x^n + 52 A a b c m^2 n^2 x^n + 48 A a b c m n^3 x^n + 48 A a b d m^2 n (x^n)^2 + B b^2 d m^4 (x^n)^4 + A b^2 d m^4 (x^n)^3 + B b^2 c m^4 (x^n)^3 + 4 B b^2 d m^3 (x^n)^4 + 6 B b^2 d m^3 (x^n)^4 + A b^2 c m^4 (x^n)^2 + 2 (x^n)^2 B a b c + 2 x^n c a b A + 2 (x^n)^2 A a b d + 30 A a^2 c m^2 n + 70 A a^2 c m n^2 + 30 A a^2 c m n + 2 (x^n)^3 B a b d + 10 A a^2 c m^3 n + 35 A a^2 c m^2 n^2 + 50 A a^2 c m n^3 + 14 B b^2 c n^2 (x^n)^3 + 4 m b^2 B d (x^n)^4 + 6 b^2 B d (x^n)^4 n + 4 A a^2 d m^3 x^n + 24 A a^2 d n^3 x^n + 6 A b^2 c m^2 (x^n)^2 + 19 A b^2 c n^2 (x^n)^2 + 6 A b^2 d m^2 (x^n)^3 + 14 A b^2 d n^2 (x^n)^3 + B a^2 c m^4 x^n + 4 B a^2 d m^3 (x^n)^2 + 12 B a^2 d n^3 (x^n)^2 + 6 B b^2 c m^2 (x^n)^3 + B a^2 d m^4 (x^n)^2 + 4 B b^2 c m^3 (x^n)^3 + 8 B b^2 c n^3 (x^n)^3 + 6 B b^2 d m^2 (x^n)^4 + 11 B b^2 d n^2 (x^n)^4 + A a^2 d m^4 x^n + 4 A b^2 c m^3 (x^n)^2 + 12 A b^2 c n^3 (x^n)^2 + 26 A a^2 d n^2 x^n + 4 A b^2 c (x^n)^2 m + 8 A b^2 c (x^n)^2 n + 6 B a^2 c m^2 x^n + 26 B a^2 c n^2 x^n + 4 B a^2 d (x^n)^2 m + 8 B a^2 d (x^n)^2 n) / (m+1) / (m+n+1) / (m+2n+1) / (m+3n+1) / (1+m+4n) * exp(1/2*m*(-I*Pi*csgn(I*e*x)^3 + I*Pi*csgn(I*e*x)^2*csgn(I*e) + I*Pi*csgn(I*e*x)^2*csgn(I*x) - I*Pi*csgn(I*e*x)*csgn(I*e)*csgn(I*x) + 2*ln(e) + 2*ln(x)))$$

**maxima [B]** time = 0.86, size = 332, normalized size = 2.08

$$\frac{B^2 d m^4 e^{m \log(x) + 4 \log(x)}}{m+4n+1} + \frac{B^2 d m^3 e^{m \log(x) + 3 \log(x)}}{m+3n+1} + \frac{2 B a b d m^2 e^{m \log(x) + 3 \log(x)}}{m+3n+1} + \frac{A^2 d m^2 e^{m \log(x) + 3 \log(x)}}{m+3n+1} + \frac{2 B a b d m e^{m \log(x) + 2 \log(x)}}{m+2n+1} + \frac{A^2 d m e^{m \log(x) + 2 \log(x)}}{m+2n+1} + \frac{B^2 d m^2 e^{m \log(x) + 2 \log(x)}}{m+2n+1} + \frac{2 A a b d m e^{m \log(x) + 2 \log(x)}}{m+2n+1} + \frac{B^2 d m e^{m \log(x) + \log(x)}}{m+n+1} + \frac{2 A a b d m e^{m \log(x) + \log(x)}}{m+n+1} + \frac{A^2 d m e^{m \log(x) + \log(x)}}{m+n+1} + \frac{(e x)^{m+1} A^2 c}{c(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="maxima")

[Out]  $B b^2 d m^4 e^{m \log(x) + 4 n \log(x)} / (m + 4 n + 1) + B b^2 c m^3 e^{m \log(x) + 3 n \log(x)} / (m + 3 n + 1) + 2 B a b d m^2 e^{m \log(x) + 3 n \log(x)} / (m + 3 n + 1) + A b^2 d m^2 e^{m \log(x) + 3 n \log(x)} / (m + 3 n + 1) + 2 B a b c m^2 e^{m \log(x) + 2 n \log(x)} / (m + 2 n + 1) + A b^2 c m^2 e^{m \log(x) + 2 n \log(x)} / (m + 2 n + 1) + B a^2 d m^2 e^{m \log(x) + 2 n \log(x)} / (m + 2 n + 1) + 2 A a b d m^2 e^{m \log(x) + 2 n \log(x)} / (m + 2 n + 1) + B a^2 c m^2 e^{m \log(x) + n \log(x)} / (m + n + 1) + 2 A a b c m^2 e^{m \log(x) + n \log(x)} / (m + n + 1) + A a^2 d m^2 e^{m \log(x) + n \log(x)} / (m + n + 1) + (e x)^{m+1} A^2 c / (e(m+1))$

**mupad [B]** time = 5.23, size = 588, normalized size = 3.68

$$\frac{e^{m \log(x)} (A^2 c - 2 A b d + 2 B a d) (m^2 + 9 n^2 + 19 m n + 30 m + 12 n^2 + 19 n^2 + 8 n + 1)}{m+1} + \frac{A^2 d m^2 e^{m \log(x)}}{m+1} + \frac{2 A a b d m e^{m \log(x) + 2 \log(x)}}{m+2n+1} + \frac{B^2 d m^2 e^{m \log(x) + 2 \log(x)}}{m+2n+1} + \frac{2 A a b d m e^{m \log(x) + 2 \log(x)}}{m+2n+1} + \frac{B^2 d m e^{m \log(x) + \log(x)}}{m+n+1} + \frac{2 A a b d m e^{m \log(x) + \log(x)}}{m+n+1} + \frac{A^2 d m e^{m \log(x) + \log(x)}}{m+n+1} + \frac{(e x)^{m+1} A^2 c}{c(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^2\*(c + d\*x^n),x)

[Out]  $(x x^{(2n)} (e x)^m (A b^2 c + B a^2 d + 2 A a b d + 2 B a b c) (3 m + 8 n + 16 m n + 19 m n^2 + 8 m^2 n + 3 m^2 + m^3 + 19 n^2 + 12 n^3 + 1)) / (4 m + 10 n + 30 m n + 70 m n^2 + 30 m^2 n + 50 m n^3 + 10 m^3 n + 6 m^2 + 4 m^3 + m^4 + 35 n^2 + 50 n^3 + 24 n^4 + 35 m^2 n^2 + 1) + (A a^2 c x^m (e x)^m) / (m + 1) + (a x x^n (e x)^m (A a d + 2 A b c + B a c) (3 m + 9 n + 18 m n + 26 m n^2 + 9 m^2 n + 3 m^2 + m^3 + 26 n^2 + 24 n^3 + 1)) / (4 m + 10 n + 30 m n + 70 m n^2 + 30 m^2 n + 50 m n^3 + 10 m^3 n + 6 m^2 + 4 m^3 + m^4 + 35 n^2 + 50 n^3 + 24 n^4 + 35 m^2 n^2 + 1) + (b x x^n (3 n) (e x)^m (A b d + 2 B a d + B b c) (3 m + 7 n + 14 m n + 14 m n^2 + 7 m^2 n + 3 m^2 + m^3 + 14 n^2 + 8 n^3 + 1)) / (4 m + 10 n + 30 m n + 70 m n^2 + 30 m^2 n + 50 m n^3 + 10 m^3 n + 6 m^2 + 4 m^3 + m^4 + 35 n^2 + 50 n^3 + 24 n^4 + 35 m^2 n^2 + 1) + (B b^2 d x x^{(4n)} (e x)^m (3 m + 6 n + 12 m n + 11 m n^2 + 6 m^2 n + 3 m^2 + m^3 + 11 n^2 + 6 n^3 + 1)) / (4 m + 10 n + 30 m n + 70 m n^2 + 30 m^2 n + 50 m$

```
*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n  
^2 + 1)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(a+b*x**n)**2*(A+B*x**n)*(c+d*x**n),x)
```

```
[Out] Timed out
```



### 3.3 $\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n) dx$

**Optimal.** Leaf size=108

$$\frac{x^{n+1}(ex)^m(aAd + aBc + Abc)}{m + n + 1} + \frac{x^{2n+1}(ex)^m(aBd + Abd + bBc)}{m + 2n + 1} + \frac{aAc(ex)^{m+1}}{e(m + 1)} + \frac{bBdx^{3n+1}(ex)^m}{m + 3n + 1}$$

**Rubi [A]** time = 0.08, antiderivative size = 108, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 3, integrand size = 27,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$ , Rules used = {570, 20, 30}

$$\frac{x^{n+1}(ex)^m(aAd + aBc + Abc)}{m + n + 1} + \frac{x^{2n+1}(ex)^m(aBd + Abd + bBc)}{m + 2n + 1} + \frac{aAc(ex)^{m+1}}{e(m + 1)} + \frac{bBdx^{3n+1}(ex)^m}{m + 3n + 1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n), x]

[Out] ((A\*b\*c + a\*B\*c + a\*A\*d)\*x^(1 + n)\*(e\*x)^m)/(1 + m + n) + ((b\*B\*c + A\*b\*d + a\*B\*d)\*x^(1 + 2\*n)\*(e\*x)^m)/(1 + m + 2\*n) + (b\*B\*d\*x^(1 + 3\*n)\*(e\*x)^m)/(1 + m + 3\*n) + (a\*A\*c\*(e\*x)^(1 + m))/(e\*(1 + m))

#### Rule 20

Int[(u\_)\*((a\_)\*(v\_))^(m\_)\*((b\_)\*(v\_))^(n\_), x\_Symbol] :> Dist[(b^IntPart[n]\*(b\*v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m + n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

#### Rule 30

Int[(x\_)^(m\_), x\_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

#### Rule 570

Int[((g\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_)\*((e\_) + (f\_)\*(x\_)^(n\_))^(r\_), x\_Symbol] :> Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

#### Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n) dx &= \int (aAc(ex)^m + (Abc + aBc + aAd)x^n(ex)^m + (bBc + Abd + aBd)x^{2n}(ex)^m + (bBd)x^{3n}(ex)^m) dx \\ &= \frac{aAc(ex)^{1+m}}{e(1+m)} + (bBd) \int x^{3n}(ex)^m dx + (Abc + aBc + aAd) \int x^n(ex)^m dx \\ &= \frac{aAc(ex)^{1+m}}{e(1+m)} + (bBdx^{-m}(ex)^m) \int x^{m+3n} dx + ((Abc + aBc + aAd)x^{1+n}(ex)^m) \\ &= \frac{(Abc + aBc + aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{(bBc + Abd + aBd)x^{1+2n}(ex)^m}{1+m+2n} + \end{aligned}$$

**Mathematica [A]** time = 0.25, size = 84, normalized size = 0.78

$$x(ex)^m \left( \frac{x^{2n}(aBd + Abd + bBc)}{m + 2n + 1} + \frac{x^n(aAd + aBc + Abc)}{m + n + 1} + \frac{aAc}{m + 1} + \frac{bBdx^{3n}}{m + 3n + 1} \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(e*x)^m*(a + b*x^n)*(A + B*x^n)*(c + d*x^n), x]
```

```
[Out] x*(e*x)^m*((a*A*c)/(1 + m) + ((A*b*c + a*B*c + a*A*d)*x^n)/(1 + m + n) + ((b*B*c + A*b*d + a*B*d)*x^(2*n))/(1 + m + 2*n) + (b*B*d*x^(3*n))/(1 + m + 3*n))
```

**IntegrateAlgebraic** [F] time = 0.11, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n) dx$$

Verification is not applicable to the result.

```
[In] IntegrateAlgebraic[(e*x)^m*(a + b*x^n)*(A + B*x^n)*(c + d*x^n), x]
```

```
[Out] Defer[IntegrateAlgebraic] [(e*x)^m*(a + b*x^n)*(A + B*x^n)*(c + d*x^n), x]
```

**fricas** [B] time = 0.45, size = 562, normalized size = 5.20

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)*(A+B*x^n)*(c+d*x^n), x, algorithm="fricas")
```

```
[Out] ((B*b*d*m^3 + 3*B*b*d*m^2 + 3*B*b*d*m + B*b*d + 2*(B*b*d*m + B*b*d)*n^2 + 3*(B*b*d*m^2 + 2*B*b*d*m + B*b*d)*n)*x*x^(3*n)*e^(m*log(e) + m*log(x)) + ((B*b*c + (B*a + A*b)*d)*m^3 + B*b*c + 3*(B*b*c + (B*a + A*b)*d)*m^2 + 3*(B*b*c + (B*a + A*b)*d + (B*b*c + (B*a + A*b)*d)*m)*n^2 + (B*a + A*b)*d + 3*(B*b*c + (B*a + A*b)*d)*m + 4*(B*b*c + (B*b*c + (B*a + A*b)*d)*m^2 + (B*a + A*b)*d + 2*(B*b*c + (B*a + A*b)*d)*m)*n)*x*x^(2*n)*e^(m*log(e) + m*log(x)) + ((A*a*d + (B*a + A*b)*c)*m^3 + A*a*d + 3*(A*a*d + (B*a + A*b)*c)*m^2 + 6*(A*a*d + (B*a + A*b)*c + (A*a*d + (B*a + A*b)*c)*m)*n^2 + (B*a + A*b)*c + 3*(A*a*d + (B*a + A*b)*c)*m + 5*(A*a*d + (A*a*d + (B*a + A*b)*c)*m^2 + (B*a + A*b)*c + 2*(A*a*d + (B*a + A*b)*c)*m)*n)*x*x^n*e^(m*log(e) + m*log(x)) + (A*a*c*m^3 + 6*A*a*c*n^3 + 3*A*a*c*m^2 + 3*A*a*c*m + A*a*c + 11*(A*a*c*m + A*a*c)*n^2 + 6*(A*a*c*m^2 + 2*A*a*c*m + A*a*c)*n)*x*x^n*e^(m*log(e) + m*log(x)))/(m^4 + 6*(m + 1)*n^3 + 4*m^3 + 11*(m^2 + 2*m + 1)*n^2 + 6*m^2 + 6*(m^3 + 3*m^2 + 3*m + 1)*n + 4*m + 1)
```

**giac** [B] time = 1.80, size = 1290, normalized size = 11.94

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)*(A+B*x^n)*(c+d*x^n), x, algorithm="giac")
```

```
[Out] (B*b*d*m^3*x*x^m*x^(3*n)*e^m + 3*B*b*d*m^2*n*x*x^m*x^(3*n)*e^m + 2*B*b*d*m*n^2*x*x^m*x^(3*n)*e^m + B*b*c*m^3*x*x^m*x^(2*n)*e^m + B*a*d*m^3*x*x^m*x^(2*n)*e^m + A*b*d*m^3*x*x^m*x^(2*n)*e^m + 4*B*b*c*m^2*n*x*x^m*x^(2*n)*e^m + 4*B*a*d*m^2*n*x*x^m*x^(2*n)*e^m + 4*A*b*d*m^2*n*x*x^m*x^(2*n)*e^m + 3*B*b*c*m*n^2*x*x^m*x^(2*n)*e^m + 3*B*a*d*m*n^2*x*x^m*x^(2*n)*e^m + 3*A*b*d*m*n^2*x*x^m*x^(2*n)*e^m + B*a*c*m^3*x*x^m*x^n*e^m + A*b*c*m^3*x*x^m*x^n*e^m + A*a*d*m^3*x*x^m*x^n*e^m + 5*B*a*c*m^2*n*x*x^m*x^n*e^m + 5*A*b*c*m^2*n*x*x^m*x^n*e^m + 5*A*a*d*m^2*n*x*x^m*x^n*e^m + 6*B*a*c*m*n^2*x*x^m*x^n*e^m + 6*A*b*c*m*n^2*x*x^m*x^n*e^m + 6*A*a*d*m*n^2*x*x^m*x^n*e^m + A*a*c*m^3*x*x^m*e^m + 6*A*a*c*m^2*n*x*x^m*e^m + 11*A*a*c*m*n^2*x*x^m*e^m + 6*A*a*c*n^3*x*x^m*e^m + 3*B*b*d*m^2*x*x^m*x^(3*n)*e^m + 6*B*b*d*m*n*x*x^m*x^(3*n)*e^m + 2*B*b*d*n^2*x*x^m*x^(3*n)*e^m + 3*B*b*c*m^2*x*x^m*x^(2*n)*e^m + 3*B*a*d*m^2*x*x^m*x^(2*n)*e^m + 3*A*b*d*m^2*x*x^m*x^(2*n)*e^m + 8*B*b*c*m*n*x*x^m*x^(2*n)*e^m + 8
```

$$\begin{aligned}
& *B*a*d*m*n*x*x^m*x^{(2*n)}*e^m + 8*A*b*d*m*n*x*x^m*x^{(2*n)}*e^m + 3*B*b*c*n^2* \\
& x*x^m*x^{(2*n)}*e^m + 3*B*a*d*n^2*x*x^m*x^{(2*n)}*e^m + 3*A*b*d*n^2*x*x^m*x^{(2* \\
& n)}*e^m + 3*B*a*c*m^2*x*x^m*x^n*e^m + 3*A*b*c*m^2*x*x^m*x^n*e^m + 3*A*a*d*m^ \\
& 2*x*x^m*x^n*e^m + 10*B*a*c*m*n*x*x^m*x^n*e^m + 10*A*b*c*m*n*x*x^m*x^n*e^m + \\
& 10*A*a*d*m*n*x*x^m*x^n*e^m + 6*B*a*c*n^2*x*x^m*x^n*e^m + 6*A*b*c*n^2*x*x^m \\
& *x^n*e^m + 6*A*a*d*n^2*x*x^m*x^n*e^m + 3*A*a*c*m^2*x*x^m*e^m + 12*A*a*c*m*n \\
& *x*x^m*e^m + 11*A*a*c*n^2*x*x^m*e^m + 3*B*b*d*m*x*x^m*x^{(3*n)}*e^m + 3*B*b*d \\
& *n*x*x^m*x^{(3*n)}*e^m + 3*B*b*c*m*x*x^m*x^{(2*n)}*e^m + 3*B*a*d*m*x*x^m*x^{(2*n)} \\
& )*e^m + 3*A*b*d*m*x*x^m*x^{(2*n)}*e^m + 4*B*b*c*n*x*x^m*x^{(2*n)}*e^m + 4*B*a*d \\
& *n*x*x^m*x^{(2*n)}*e^m + 4*A*b*d*n*x*x^m*x^{(2*n)}*e^m + 3*B*a*c*m*x*x^m*x^n*e^ \\
& m + 3*A*b*c*m*x*x^m*x^n*e^m + 3*A*a*d*m*x*x^m*x^n*e^m + 5*B*a*c*n*x*x^m*x^n \\
& *e^m + 5*A*b*c*n*x*x^m*x^n*e^m + 5*A*a*d*n*x*x^m*x^n*e^m + 3*A*a*c*m*x*x^m* \\
& e^m + 6*A*a*c*n*x*x^m*e^m + B*b*d*x*x^m*x^{(3*n)}*e^m + B*b*c*x*x^m*x^{(2*n)}*e \\
& ^m + B*a*d*x*x^m*x^{(2*n)}*e^m + A*b*d*x*x^m*x^{(2*n)}*e^m + B*a*c*x*x^m*x^n*e^ \\
& m + A*b*c*x*x^m*x^n*e^m + A*a*d*x*x^m*x^n*e^m + A*a*c*x*x^m*e^m)/(m^4 + 6*m \\
& ^3*n + 11*m^2*n^2 + 6*m*n^3 + 4*m^3 + 18*m^2*n + 22*m*n^2 + 6*n^3 + 6*m^2 + \\
& 18*m*n + 11*n^2 + 4*m + 6*n + 1)
\end{aligned}$$

**maple [C]** time = 0.11, size = 891, normalized size = 8.25

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(b*x^n+a)*(A+B*x^n)*(d*x^n+c), x)$

[Out]  $x*(a*A*c+B*b*c*(x^n)^2+B*a*d*(x^n)^2+A*b*d*(x^n)^2+b*B*d*(x^n)^3+B*a*c*x^n+A*a*d*x^n+A*b*c*x^n+A*a*c*m^3+3*A*a*c*m^2+11*A*a*c*n^2+6*A*a*c*n^3+6*a*A*c*n+10*A*b*c*m*n*x^n+10*B*a*c*m*n*x^n+10*A*a*d*m*n*x^n+6*B*a*c*m*n^2*x^n+8*B*a*d*m*n*(x^n)^2+8*B*b*c*m*n*(x^n)^2+8*A*b*d*m*n*(x^n)^2+5*B*a*c*m^2*n*x^n+5*A*b*c*m^2*n*x^n+6*A*b*c*m*n^2*x^n+6*A*a*d*m*n^2*x^n+5*A*a*d*m^2*n*x^n+3*B*b*c*m*n^2*(x^n)^2+6*B*b*d*m*n*(x^n)^3+4*B*a*d*m^2*n*(x^n)^2+3*B*a*d*m*n^2*(x^n)^2+4*B*b*c*m^2*n*(x^n)^2+3*A*b*d*m*n^2*(x^n)^2+4*A*b*d*m^2*n*(x^n)^2+3*B*b*d*m^2*n*(x^n)^3+2*B*b*d*m*n^2*(x^n)^3+4*A*(x^n)^2*b*d*n+3*B*(x^n)^2*a*d*m+4*B*(x^n)^2*a*d*n+3*B*(x^n)^2*b*c*m+4*B*(x^n)^2*b*c*n+3*A*x^n*a*d*m+5*A*x^n*a*d*n+3*A*x^n*b*c*m+5*A*x^n*b*c*n+3*B*x^n*a*c*m+5*B*x^n*a*c*n+3*B*(x^n)^3*b*d*m+3*B*(x^n)^3*b*d*n+3*A*(x^n)^2*b*d*m+3*A*a*c*m+6*A*a*c*m^2*n+11*A*a*c*m*n^2+12*A*a*c*m*n+6*A*b*c*n^2*x^n+3*B*a*c*m^2*x^n+6*B*a*c*n^2*x^n+A*a*d*m^3*x^n+A*b*c*m^3*x^n+3*A*b*d*m^2*(x^n)^2+3*A*b*d*n^2*(x^n)^2+B*a*c*m^3*x^n+3*B*a*d*m^2*(x^n)^2+3*B*a*d*n^2*(x^n)^2+3*B*b*c*m^2*(x^n)^2+3*B*b*c*n^2*(x^n)^2+3*A*a*d*m^2*x^n+6*A*a*d*n^2*x^n+3*A*b*c*m^2*x^n+B*b*d*m^3*(x^n)^3+A*b*d*m^3*(x^n)^2+B*a*d*m^3*(x^n)^2+B*b*c*m^3*(x^n)^2+3*B*b*d*m^2*(x^n)^3+2*B*b*d*n^2*(x^n)^3)/(m+1)/(m+n+1)/(m+2*n+1)/(m+3*n+1)*exp(1/2*(-I*Pi*csgn(I*e)*csgn(I*x)*csgn(I*e*x)+I*Pi*csgn(I*e)*csgn(I*e*x)^2+I*Pi*csgn(I*x)*csgn(I*e*x)^2-I*Pi*csgn(I*e*x)^3+2*ln(e)+2*ln(x))*m)$

**maxima [A]** time = 0.70, size = 200, normalized size = 1.85

$$\frac{Bbde^m x e^{(m \log(x) + 3n \log(x))}}{m + 3n + 1} + \frac{Bbce^m x e^{(m \log(x) + 2n \log(x))}}{m + 2n + 1} + \frac{Bade^m x e^{(m \log(x) + 2n \log(x))}}{m + 2n + 1} + \frac{Abde^m x e^{(m \log(x) + 2n \log(x))}}{m + 2n + 1} + \frac{Bace^m x e^{(m \log(x) + n \log(x))}}{m + n + 1} + \frac{Abce^m x e^{(m \log(x) + n \log(x))}}{m + n + 1} + \frac{Aade^m x e^{(m \log(x) + n \log(x))}}{m + n + 1} + \frac{(ex)^{m+1} Aac}{e(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{integrate}((e*x)^m*(a+b*x^n)*(A+B*x^n)*(c+d*x^n), x, \text{algorithm}="maxima")$

[Out]  $B*b*d*e^m*x*e^{(m*\log(x) + 3*n*\log(x))/(m + 3*n + 1)} + B*b*c*e^m*x*e^{(m*\log(x) + 2*n*\log(x))/(m + 2*n + 1)} + B*a*d*e^m*x*e^{(m*\log(x) + 2*n*\log(x))/(m + 2*n + 1)} + A*b*d*e^m*x*e^{(m*\log(x) + 2*n*\log(x))/(m + 2*n + 1)} + B*a*c*e^m*x*e^{(m*\log(x) + n*\log(x))/(m + n + 1)} + A*b*c*e^m*x*e^{(m*\log(x) + n*\log(x))/(m + n + 1)} + A*a*d*e^m*x*e^{(m*\log(x) + n*\log(x))/(m + n + 1)} + (e*x)^{(m + 1)}*A*a*c/(e*(m + 1))$



$< 1$ ),  $(-e^{-(2n)} \text{meijerg}(((), (1, 1)), ((0, 0), ()), x) + e^{-(2n)} \text{meijerg}(((1, 1), ()), (((), (0, 0)), x), \text{True}))/e + B*b*d*\text{Piecewise}((\log(x), \text{Eq}(n, 0)), (-x^{(3n)}/(2*0^{(1/n)}*zoo^{(1/n)}*n*x^{(2n)}*(0^{(1/n)})^{(2n)} - 3*n*x^{(2n)}*(0^{(1/n)})^{(2n)}), \text{Eq}(e, 0^{(1/n)})), (e^{-(2n)}*x^{n/n}, \text{True}))/e$ ,  $\text{Eq}(m, -2n - 1)$ ),  $(A*a*c*\text{Piecewise}((\log(x), \text{Eq}(n, 0)), (-x^{(-n)}*(0^{(1/n)})^{(-n)}/n, \text{Eq}(e, 0^{(1/n)})), (-e^{(-n)}*x^{(-n)}/n, \text{True}))/e + A*a*d*\text{Piecewise}((e^{(-n)}*\log(x), \text{Abs}(x) < 1), (-e^{(-n)}*\log(1/x), 1/\text{Abs}(x) < 1), (-e^{(-n)}* \text{meijerg}(((), (1, 1)), ((0, 0), ()), x) + e^{(-n)}* \text{meijerg}(((1, 1), ()), (((), (0, 0)), x), \text{True}))/e + A*b*c*\text{Piecewise}((e^{(-n)}*\log(x), \text{Abs}(x) < 1), (-e^{(-n)}*\log(1/x), 1/\text{Abs}(x) < 1), (-e^{(-n)}* \text{meijerg}(((), (1, 1)), ((0, 0), ()), x) + e^{(-n)}* \text{meijerg}(((1, 1), ()), (((), (0, 0)), x), \text{True}))/e + A*b*d*\text{Piecewise}((\log(x), \text{Eq}(n, 0)), (-x^{(2n)}/(0^{(1/n)}*zoo^{(1/n)}*n*x^{n*(0^{(1/n)})^{n} - 2*n*x^{n*(0^{(1/n)})^{n}}), \text{Eq}(e, 0^{(1/n)})), (e^{(-n)}*x^{n/n}, \text{True}))/e + B*a*c*\text{Piecewise}((e^{(-n)}*\log(x), \text{Abs}(x) < 1), (-e^{(-n)}*\log(1/x), 1/\text{Abs}(x) < 1), (-e^{(-n)}* \text{meijerg}(((), (1, 1)), ((0, 0), ()), x) + e^{(-n)}* \text{meijerg}(((1, 1), ()), (((), (0, 0)), x), \text{True}))/e + B*a*d*\text{Piecewise}((\log(x), \text{Eq}(n, 0)), (-x^{(2n)}/(0^{(1/n)}*zoo^{(1/n)}*n*x^{n*(0^{(1/n)})^{n} - 2*n*x^{n*(0^{(1/n)})^{n}}), \text{Eq}(e, 0^{(1/n)})), (e^{(-n)}*x^{n/n}, \text{True}))/e + B*b*c*\text{Piecewise}((\log(x), \text{Eq}(n, 0)), (-x^{(2n)}/(0^{(1/n)}*zoo^{(1/n)}*n*x^{n*(0^{(1/n)})^{n} - 2*n*x^{n*(0^{(1/n)})^{n}}), \text{Eq}(e, 0^{(1/n)})), (e^{(-n)}*x^{n/n}, \text{True}))/e + B*b*d*\text{Piecewise}((\log(x), \text{Eq}(n, 0)), (-x^{(3n)}/(0^{(1/n)}*zoo^{(1/n)}*n*x^{n*(0^{(1/n)})^{n} - 3*n*x^{n*(0^{(1/n)})^{n}}), \text{Eq}(e, 0^{(1/n)})), (e^{(-n)}*x^{(2n)}/(2n), \text{True}))/e$ ,  $\text{Eq}(m, -n - 1)$ ),  $(A*a*c*e^{m*m*3*x*x*m}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 6*A*a*c*e^{m*m*2*n*x*x*m}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 3*A*a*c*e^{m*m*2*x*x*m}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 11*A*a*c*e^{m*m*n^{*2}*x*x*m}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 12*A*a*c*e^{m*m*n*x*x*m}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 3*A*a*c*e^{m*m*x*x*m}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 6*A*a*c*e^{m*n^{*3}*x*x*m}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 11*A*a*c*e^{m*n^{*2}*x*x*m}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 6*A*a*c*e^{m*n*x*x*m}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + A*a*c*e^{m*x*x*m}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + A*a*d*e^{m*m*3*x*x*m*x^{*n}}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 5*A*a*d*e^{m*m*2*n*x*x*m*x^{*n}}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 3*A*a*d*e^{m*m*2*x*x*m*x^{*n}}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 10*A*a*d*e^{m*m*n*x*x*m*x^{*n}}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 3*A*a*d*e^{m*m*x*x*m*x^{*n}}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 6*A*a*d*e^{m*n^{*2}*x*x*m*x^{*n}}/(m^{*4} + 6*m^{*3}*n + 4*m^{*3} + 11*m^{*2}*n^{*2} + 18*m^{*2}*n + 6*m^{*2} + 6*m*n^{*3} + 22*m*n^{*2} + 18*m*n + 4*m + 6*n^{*3} + 11*n^{*2} + 6*n + 1) + 5*A*a*d*e^{m*n*x*x*m*x^{*n}}/(m^{*4} + 6*m^{*3}*n + 4*m$

$$\begin{aligned}
& **3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4 \\
& *m + 6*n**3 + 11*n**2 + 6*n + 1) + A*a*d*e**m*x*x**m*x**n/(m**4 + 6*m**3*n \\
& + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m* \\
& n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + A*b*c*e**m*m**3*x*x**m*x**n/(m**4 + \\
& 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n* \\
& *2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 5*A*b*c*e**m*m**2*n*x*x** \\
& m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m* \\
& n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*A*b*c*e** \\
& m*m**2*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6 \\
& *m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + \\
& 6*A*b*c*e**m*m*n**2*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + \\
& 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n** \\
& 2 + 6*n + 1) + 10*A*b*c*e**m*m*n*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11 \\
& *m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n \\
& **3 + 11*n**2 + 6*n + 1) + 3*A*b*c*e**m*m*x*x**m*x**n/(m**4 + 6*m**3*n + 4* \\
& m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + \\
& 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 6*A*b*c*e**m*n**2*x*x**m*x**n/(m**4 + 6 \\
& *m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 \\
& + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 5*A*b*c*e**m*n*x*x**m*x**n/ \\
& (m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + \\
& 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + A*b*c*e**m*x*x**m* \\
& x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n* \\
& *3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + A*b*d*e**m*m* \\
& *3*x*x**m*x**n/(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6 \\
& *m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + \\
& 4*A*b*d*e**m*m**2*n*x*x**m*x**n/(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n* \\
& *2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11 \\
& *n**2 + 6*n + 1) + 3*A*b*d*e**m*m**2*x*x**m*x**n/(2*n)/(m**4 + 6*m**3*n + 4*m \\
& **3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4 \\
& *m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*A*b*d*e**m*m*n**2*x*x**m*x**n/(2*n)/(m** \\
& 4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m \\
& *n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 8*A*b*d*e**m*m*n*x*x** \\
& m*x**n/(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + \\
& 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*A*b*d \\
& *e**m*m*x*x**m*x**n/(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2* \\
& n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + \\
& 1) + 3*A*b*d*e**m*n**2*x*x**m*x**n/(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2 \\
& *n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + \\
& 11*n**2 + 6*n + 1) + 4*A*b*d*e**m*n*x*x**m*x**n/(2*n)/(m**4 + 6*m**3*n + 4*m \\
& **3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4 \\
& *m + 6*n**3 + 11*n**2 + 6*n + 1) + A*b*d*e**m*x*x**m*x**n/(2*n)/(m**4 + 6*m** \\
& 3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 1 \\
& 8*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + B*a*c*e**m*m**3*x*x**m*x**n/(m* \\
& *4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22* \\
& m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 5*B*a*c*e**m*m**2*n*x \\
& *x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + \\
& 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*B*a*c \\
& *e**m*m**2*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n \\
& + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + \\
& 1) + 6*B*a*c*e**m*m*n**2*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n* \\
& *2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11 \\
& *n**2 + 6*n + 1) + 10*B*a*c*e**m*m*n*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 \\
& + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + \\
& 6*n**3 + 11*n**2 + 6*n + 1) + 3*B*a*c*e**m*m*x*x**m*x**n/(m**4 + 6*m**3*n \\
& + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m* \\
& n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 6*B*a*c*e**m*n**2*x*x**m*x**n/(m**4 \\
& + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m* \\
& n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 5*B*a*c*e**m*n*x*x**m*x \\
& **n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**
\end{aligned}$$

$$\begin{aligned}
& 3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + B*a*c*e**m*x*x \\
& **m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6* \\
& m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + B*a*d*e** \\
& m*m**3*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n \\
& + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + \\
& 1) + 4*B*a*d*e**m*m**2*n*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m** \\
& 2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 \\
& + 11*n**2 + 6*n + 1) + 3*B*a*d*e**m*m**2*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + \\
& 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n \\
& + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*B*a*d*e**m*m*n**2*x*x**m*x**(2*n)/ \\
& (m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + \\
& 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 8*B*a*d*e**m*m*n*x \\
& *x**m*x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m** \\
& 2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*B \\
& *a*d*e**m*m*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m \\
& **2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6 \\
& *n + 1) + 3*B*a*d*e**m*n**2*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11* \\
& m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n* \\
& *3 + 11*n**2 + 6*n + 1) + 4*B*a*d*e**m*n*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + \\
& 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n \\
& + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + B*a*d*e**m*x*x**m*x**(2*n)/(m**4 + 6 \\
& *m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 \\
& + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + B*b*c*e**m*m**3*x*x**m*x**( \\
& 2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n* \\
& *3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 4*B*b*c*e**m \\
& m**2*n*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n \\
& + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + \\
& 1) + 3*B*b*c*e**m*m**2*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2* \\
& n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + \\
& 11*n**2 + 6*n + 1) + 3*B*b*c*e**m*m*n**2*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + \\
& 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n \\
& + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 8*B*b*c*e**m*m*n*x*x**m*x**(2*n)/(m \\
& *4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22* \\
& m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*B*b*c*e**m*m*x*x**m \\
& *x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6 \\
& *m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*B*b*c* \\
& e**m*n**2*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m** \\
& 2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n \\
& + 1) + 4*B*b*c*e**m*n*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2* \\
& n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + \\
& 11*n**2 + 6*n + 1) + B*b*c*e**m*x*x**m*x**(2*n)/(m**4 + 6*m**3*n + 4*m**3 + \\
& 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + \\
& 6*n**3 + 11*n**2 + 6*n + 1) + B*b*d*e**m*m**3*x*x**m*x**(3*n)/(m**4 + 6*m** \\
& 3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 1 \\
& 8*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*B*b*d*e**m*m**2*n*x*x**m*x**( \\
& 3*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n* \\
& *3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*B*b*d*e**m \\
& m**2*x*x**m*x**(3*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + \\
& 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) \\
& + 2*B*b*d*e**m*m*n**2*x*x**m*x**(3*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2* \\
& n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + \\
& 11*n**2 + 6*n + 1) + 6*B*b*d*e**m*m*n*x*x**m*x**(3*n)/(m**4 + 6*m**3*n + 4* \\
& m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + \\
& 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*B*b*d*e**m*m*x*x**m*x**(3*n)/(m**4 + \\
& 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n** \\
& 2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 2*B*b*d*e**m*n**2*x*x**m*x \\
& **3*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m \\
& *n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*B*b*d*e* \\
& *m*n*x*x**m*x**(3*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n +
\end{aligned}$$

```
6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1)
+ B*b*d*e**m*x*x**m*x**(3*n)/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18
*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 +
6*n + 1), True))
```



### 3.4 $\int (ex)^m (A + Bx^n) (c + dx^n) dx$

**Optimal.** Leaf size=66

$$\frac{x^{n+1}(ex)^m(Ad + Bc)}{m + n + 1} + \frac{Ac(ex)^{m+1}}{e(m + 1)} + \frac{Bdx^{2n+1}(ex)^m}{m + 2n + 1}$$

**Rubi [A]** time = 0.04, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 20,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$ , Rules used = {448, 20, 30}

$$\frac{x^{n+1}(ex)^m(Ad + Bc)}{m + n + 1} + \frac{Ac(ex)^{m+1}}{e(m + 1)} + \frac{Bdx^{2n+1}(ex)^m}{m + 2n + 1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n), x]

[Out] ((B\*c + A\*d)\*x^(1 + n)\*(e\*x)^m)/(1 + m + n) + (B\*d\*x^(1 + 2\*n)\*(e\*x)^m)/(1 + m + 2\*n) + (A\*c\*(e\*x)^(1 + m))/(e\*(1 + m))

Rule 20

Int[(u\_.)\*((a\_.)\*(v\_.))^(m\_.)\*((b\_.)\*(v\_.))^(n\_.), x\_Symbol] :> Dist[(b^IntPart[n]\*(b\*v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m + n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

Rule 30

Int[(x\_)^(m\_.), x\_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 448

Int[((e\_.)\*(x\_.))^(m\_.)\*((a\_.) + (b\_.)\*(x\_.)^(n\_.))^(p\_.)\*((c\_.) + (d\_.)\*(x\_.)^(n\_.))^(q\_.), x\_Symbol] :> Int[ExpandIntegrand[(e\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[b\*c - a\*d, 0] && IGtQ[p, 0] && IGtQ[q, 0]

Rubi steps

$$\begin{aligned} \int (ex)^m (A + Bx^n) (c + dx^n) dx &= \int (Ac(ex)^m + (Bc + Ad)x^n(ex)^m + Bdx^{2n}(ex)^m) dx \\ &= \frac{Ac(ex)^{1+m}}{e(1+m)} + (Bd) \int x^{2n}(ex)^m dx + (Bc + Ad) \int x^n(ex)^m dx \\ &= \frac{Ac(ex)^{1+m}}{e(1+m)} + (Bdx^{-m}(ex)^m) \int x^{m+2n} dx + ((Bc + Ad)x^{-m}(ex)^m) \int x^{m+n} dx \\ &= \frac{(Bc + Ad)x^{1+n}(ex)^m}{1 + m + n} + \frac{Bdx^{1+2n}(ex)^m}{1 + m + 2n} + \frac{Ac(ex)^{1+m}}{e(1+m)} \end{aligned}$$

**Mathematica [A]** time = 0.07, size = 49, normalized size = 0.74

$$x(ex)^m \left( \frac{x^n(Ad + Bc)}{m + n + 1} + \frac{Ac}{m + 1} + \frac{Bdx^{2n}}{m + 2n + 1} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n), x]

[Out] x\*(e\*x)^m\*((A\*c)/(1 + m) + ((B\*c + A\*d)\*x^n)/(1 + m + n) + (B\*d\*x^(2\*n))/(1 + m + 2\*n))

**IntegrateAlgebraic [F]** time = 0.07, size = 0, normalized size = 0.00

$$\int (ex)^m (A + Bx^n) (c + dx^n) dx$$

Verification is not applicable to the result.

[In] IntegrateAlgebraic[(e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n), x]

[Out] Defer[IntegrateAlgebraic] [(e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n), x]

**fricas [B]** time = 0.44, size = 185, normalized size = 2.80

$$\frac{(Bdm^2 + 2Bdm + Bd + (Bdm + Bd)n)xx^{2n}e^{(m \log(e) + m \log(x))} + ((Bc + Ad)m^2 + Bc + Ad + 2(Bc + Ad)m + 2(Bc + Ad + (Bc + Ad)m)n)xx^ne^{(m \log(e) + m \log(x))} + (Acm^2 + 2Acr^2 + 2Acm + Ac + 3(Acm + Ac)n)xe^{(m \log(e) + m \log(x))}}{m^3 + 2(m + 1)n^2 + 3m^2 + 3(m^2 + 2m + 1)n + 3m + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n), x, algorithm="fricas")

[Out] ((B\*d\*m^2 + 2\*B\*d\*m + B\*d + (B\*d\*m + B\*d)\*n)\*x\*x^(2\*n)\*e^(m\*log(e) + m\*log(x)) + ((B\*c + A\*d)\*m^2 + B\*c + A\*d + 2\*(B\*c + A\*d)\*m + 2\*(B\*c + A\*d + (B\*c + A\*d)\*m)\*n)\*x\*x^n\*e^(m\*log(e) + m\*log(x)) + (A\*c\*m^2 + 2\*A\*c\*n^2 + 2\*A\*c\*m + A\*c + 3\*(A\*c\*m + A\*c)\*n)\*x\*e^(m\*log(e) + m\*log(x))/(m^3 + 2\*(m + 1)\*n^2 + 3\*m^2 + 3\*(m^2 + 2\*m + 1)\*n + 3\*m + 1)

**giac [B]** time = 0.45, size = 327, normalized size = 4.95

$$\frac{Bdm^2x^{2n} + Bdmx^{2n} + Bcm^2x^{2n} + Bdmx^{2n} + Adm^2x^{2n} + 2Bdmx^{2n} + 2Admx^{2n} + Acm^2x^{2n} + 3Acmx^{2n} + 2Acmx^{2n} + 2Bdmx^{2n} + Bdmx^{2n} + 2Bdmx^{2n} + 2Admx^{2n} + 2Bdmx^{2n} + 2Admx^{2n} + 2Acmx^{2n} + 3Acmx^{2n} + Bdmx^{2n} + Bcm^2x^{2n} + Adm^2x^{2n} + Acm^2x^{2n}}{m^3 + 3m^2n + 2m^2 + 6mn + 2n^2 + 3m + 3n + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n), x, algorithm="giac")

[Out] (B\*d\*m^2\*x\*x^m\*x^(2\*n)\*e^m + B\*d\*m\*n\*x\*x^m\*x^(2\*n)\*e^m + B\*c\*m^2\*x\*x^m\*x^n\*e^m + A\*d\*m^2\*x\*x^m\*x^n\*e^m + 2\*B\*c\*m\*n\*x\*x^m\*x^n\*e^m + 2\*A\*d\*m\*n\*x\*x^m\*x^n\*e^m + A\*c\*m^2\*x\*x^m\*e^m + 3\*A\*c\*m\*n\*x\*x^m\*e^m + 2\*A\*c\*n^2\*x\*x^m\*e^m + 2\*B\*d\*m\*x\*x^m\*x^(2\*n)\*e^m + B\*d\*n\*x\*x^m\*x^(2\*n)\*e^m + 2\*B\*c\*m\*x\*x^m\*x^n\*e^m + 2\*A\*d\*m\*x\*x^m\*x^n\*e^m + 2\*B\*c\*n\*x\*x^m\*x^n\*e^m + 2\*A\*d\*n\*x\*x^m\*x^n\*e^m + 2\*A\*c\*m\*x\*x^m\*e^m + 3\*A\*c\*n\*x\*x^m\*e^m + B\*d\*x\*x^m\*x^(2\*n)\*e^m + B\*c\*x\*x^m\*x^n\*e^m + A\*d\*x\*x^m\*x^n\*e^m + A\*c\*x\*x^m\*e^m)/(m^3 + 3\*m^2\*n + 2\*m\*n^2 + 3\*m^2 + 6\*m\*n + 2\*n^2 + 3\*m + 3\*n + 1)

**maple [C]** time = 0.12, size = 262, normalized size = 3.97

$$\frac{(Ad^2x^2 + 2Admx^2 + Bcm^2x^2 + 2Bcmx^2 + Bdm^2x^2 + Bdmx^2 + Acm^2 + 3Acmn + 2Acr^2 + 2Admx^2 + 2Adnx^2 + 2Bcmx^2 + 2Bcnx^2 + 2Bdmx^2 + Bdmx^2 + 2Acm + 3Acm + Adx^2 + Bcx^2 + Bdx^2 + Ac)xe^{(m \log(e) + m \log(x))}}{(m + 1)(m + n + 1)(m + 2n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)\*(d\*x^n+c), x)

[Out] x\*(B\*d\*m^2\*(x^n)^2+B\*d\*m\*n\*(x^n)^2+A\*d\*m^2\*x^n+2\*A\*d\*m\*n\*x^n+B\*c\*m^2\*x^n+2\*B\*c\*m\*n\*x^n+2\*B\*(x^n)^2\*d\*m+B\*(x^n)^2\*d\*n+A\*c\*m^2+3\*A\*c\*m\*n+2\*A\*c\*n^2+2\*A\*x^n\*d\*m+2\*A\*x^n\*d\*n+2\*B\*x^n\*c\*m+2\*B\*x^n\*c\*n+d\*(x^n)^2+B\*2\*A\*c\*m+3\*A\*c\*n+d\*x^n\*A+c\*B\*x^n+A\*c)/(m+1)/(m+n+1)/(m+2\*n+1)\*exp(1/2\*(-I\*Pi\*csgn(I\*e)\*csgn(I\*x)\*csgn(I\*e\*x)+I\*Pi\*csgn(I\*e)\*csgn(I\*e\*x)^2+I\*Pi\*csgn(I\*x)\*csgn(I\*e\*x)^2-I\*Pi\*csgn(I\*e\*x)^3+2\*ln(e)+2\*ln(x))\*m)

**maxima [A]** time = 0.60, size = 91, normalized size = 1.38

$$\frac{Bde^m x e^{(m \log(x) + 2n \log(x))}}{m + 2n + 1} + \frac{Bce^m x e^{(m \log(x) + n \log(x))}}{m + n + 1} + \frac{Ade^m x e^{(m \log(x) + n \log(x))}}{m + n + 1} + \frac{(ex)^{m+1} Ac}{e(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="maxima")

[Out] B\*d\*e^m\*x\*e^(m\*log(x) + 2\*n\*log(x))/(m + 2\*n + 1) + B\*c\*e^m\*x\*e^(m\*log(x) + n\*log(x))/(m + n + 1) + A\*d\*e^m\*x\*e^(m\*log(x) + n\*log(x))/(m + n + 1) + (e\*x)^(m + 1)\*A\*c/(e\*(m + 1))

**mupad [B]** time = 4.83, size = 91, normalized size = 1.38

$$(ex)^m \left( \frac{Acx}{m+1} + \frac{xx^n (Ad + Bc) (m + 2n + 1)}{m^2 + 3mn + 2m + 2n^2 + 3n + 1} + \frac{Bdx x^{2n} (m + n + 1)}{m^2 + 3mn + 2m + 2n^2 + 3n + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n),x)

[Out] (e\*x)^m\*((A\*c\*x)/(m + 1) + (x\*x^n\*(A\*d + B\*c)\*(m + 2\*n + 1))/(2\*m + 3\*n + 3\*m\*n + m^2 + 2\*n^2 + 1) + (B\*d\*x\*x^(2\*n)\*(m + n + 1))/(2\*m + 3\*n + 3\*m\*n + m^2 + 2\*n^2 + 1))

**sympy [A]** time = 29.33, size = 1698, normalized size = 25.73

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)\*(c+d\*x\*\*n),x)

[Out] Piecewise(((A + B)\*(c + d)\*log(x)/e, Eq(m, -1) & Eq(n, 0)), ((A\*c\*log(x) + A\*d\*x\*\*n/n + B\*c\*x\*\*n/n + B\*d\*x\*\*(2\*n)/(2\*n))/e, Eq(m, -1)), (A\*c\*Piecewise((log(x), Eq(n, 0)), (-x\*\*(-2\*n)\*(0\*\*(1/n))\*\*(-2\*n)/(2\*n), Eq(e, 0\*\*(1/n))), (-e\*\*(-2\*n)\*x\*\*(-2\*n)/(2\*n), True))/e + A\*d\*Piecewise((log(x), Eq(n, 0)), (-x\*\*n/(2\*0\*\*(1/n)\*zoo\*\*(1/n)\*n\*x\*\*(2\*n)\*(0\*\*(1/n))\*\*(-2\*n) - n\*x\*\*(2\*n)\*(0\*\*(1/n))\*\*(-2\*n)), Eq(e, 0\*\*(1/n))), (-e\*\*(-2\*n)\*x\*\*(-n)/n, True))/e + B\*c\*Piecewise((log(x), Eq(n, 0)), (-x\*\*n/(2\*0\*\*(1/n)\*zoo\*\*(1/n)\*n\*x\*\*(2\*n)\*(0\*\*(1/n))\*\*(-2\*n) - n\*x\*\*(2\*n)\*(0\*\*(1/n))\*\*(-2\*n)), Eq(e, 0\*\*(1/n))), (-e\*\*(-2\*n)\*x\*\*(-n)/n, True))/e + B\*d\*Piecewise((e\*\*(-2\*n)\*log(x), Abs(x) < 1), (-e\*\*(-2\*n)\*log(1/x), 1/Abs(x) < 1), (-e\*\*(-2\*n)\*meijerg(((), (1, 1)), ((0, 0), ()), x) + e\*\*(-2\*n)\*meijerg(((1, 1), ()), (((), (0, 0)), x), True))/e, Eq(m, -2\*n - 1)), (A\*c\*Piecewise((log(x), Eq(n, 0)), (-x\*\*(-n)\*(0\*\*(1/n))\*\*(-n)/n, Eq(e, 0\*\*(1/n))), (-e\*\*(-n)\*x\*\*(-n)/n, True))/e + A\*d\*Piecewise((e\*\*(-n)\*log(x), Abs(x) < 1), (-e\*\*(-n)\*log(1/x), 1/Abs(x) < 1), (-e\*\*(-n)\*meijerg(((), (1, 1)), ((0, 0), ()), x) + e\*\*(-n)\*meijerg(((1, 1), ()), (((), (0, 0)), x), True))/e + B\*c\*Piecewise((e\*\*(-n)\*log(x), Abs(x) < 1), (-e\*\*(-n)\*log(1/x), 1/Abs(x) < 1), (-e\*\*(-n)\*meijerg(((), (1, 1)), ((0, 0), ()), x) + e\*\*(-n)\*meijerg(((1, 1), ()), (((), (0, 0)), x), True))/e + B\*d\*Piecewise((log(x), Eq(n, 0)), (-x\*\*(2\*n)/(0\*\*(1/n)\*zoo\*\*(1/n)\*n\*x\*\*n\*(0\*\*(1/n))\*\*n - 2\*n\*x\*\*n\*(0\*\*(1/n))\*\*n), Eq(e, 0\*\*(1/n))), (e\*\*(-n)\*x\*\*n/n, True))/e, Eq(m, -n - 1)), (A\*c\*e\*\*m\*m\*\*2\*x\*x\*\*m/(m\*\*3 + 3\*m\*\*2\*n + 3\*m\*\*2 + 2\*m\*n\*\*2 + 6\*m\*n + 3\*m + 2\*n\*\*2 + 3\*n + 1) + 3\*A\*c\*e\*\*m\*m\*n\*x\*x\*\*m/(m\*\*3 + 3\*m\*\*2\*n + 3\*m\*\*2 + 2\*m\*n\*\*2 + 6\*m\*n + 3\*m + 2\*n\*\*2 + 3\*n + 1) + 2\*A\*c\*e\*\*m\*m\*x\*x\*\*m/(m\*\*3 + 3\*m\*\*2\*n + 3\*m\*\*2 + 2\*m\*n\*\*2 + 6\*m\*n + 3\*m + 2\*n\*\*2 + 3\*n + 1) + 2\*A\*c\*e\*\*m\*n\*\*2\*x\*x\*\*m/(m\*\*3 + 3\*m\*\*2\*n + 3\*m\*\*2 + 2\*m\*n\*\*2 + 6\*m\*n + 3\*m + 2\*n\*\*2 + 3\*n + 1) + 3\*A\*c\*e\*\*m\*n\*x\*x\*\*m/(m\*\*3 + 3\*m\*\*2\*n + 3\*m\*\*2 + 2\*m\*n\*\*2 + 6\*m\*n + 3\*m + 2\*n\*\*2 + 3\*n + 1) + A\*c\*e\*\*m\*x\*x\*\*m/(m\*\*3 + 3\*m\*\*2\*n + 3\*m\*\*2 + 2\*m\*n\*\*2 + 6\*m\*n + 3\*m + 2\*n\*\*2 + 3\*n + 1) + A\*d\*e\*\*m\*m\*\*2\*x\*x\*\*m\*x\*\*n/(m\*\*3 +

```

3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + 2*A*d*e**m
*m*n*x*x**m*x**n/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**
2 + 3*n + 1) + 2*A*d*e**m*m*x*x**m*x**n/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**
2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + 2*A*d*e**m*n*x*x**m*x**n/(m**3 + 3*m
**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + A*d*e**m*x*x**
m*x**n/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n +
1) + B*c*e**m*m**2*x*x**m*x**n/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n
+ 3*m + 2*n**2 + 3*n + 1) + 2*B*c*e**m*m*n*x*x**m*x**n/(m**3 + 3*m**2*n +
3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + 2*B*c*e**m*m*x*x**m*x
**n/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1)
+ 2*B*c*e**m*n*x*x**m*x**n/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3
*m + 2*n**2 + 3*n + 1) + B*c*e**m*x*x**m*x**n/(m**3 + 3*m**2*n + 3*m**2 + 2
*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + B*d*e**m*m**2*x*x**m*x**(2*n)/(
m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + B*d
*e**m*m*n*x*x**m*x**(2*n)/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*
m + 2*n**2 + 3*n + 1) + 2*B*d*e**m*m*x*x**m*x**(2*n)/(m**3 + 3*m**2*n + 3*m
**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + B*d*e**m*n*x*x**m*x**(2*
n)/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) +
B*d*e**m*x*x**m*x**(2*n)/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*
m + 2*n**2 + 3*n + 1), True))

```

### 3.5 $\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^2 dx$

**Optimal.** Leaf size=318

$$\frac{a^3 Ac^2 (ex)^{m+1}}{e(m+1)} + \frac{ax^{2n+1} (ex)^m (A(a^2 d^2 + 6abcd + 3b^2 c^2) + aBc(2ad + 3bc))}{m+2n+1} + \frac{x^{3n+1} (ex)^m (Ab(3a^2 d^2 + 6abcd + 3b^2 c^2) + a^2 Bc^2)}{m+3n+1}$$

**Rubi [A]** time = 0.41, antiderivative size = 318, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {570, 20, 30}

$$\frac{ax^{2n+1}(ex)^m(A(a^2d^2+6abcd+3b^2c^2)+aBc(2ad+3bc))}{m+2n+1} + \frac{x^{3n+1}(ex)^m(Ab(3a^2d^2+6abcd+3b^2c^2)+a^2Bc^2)}{m+3n+1} + \frac{bx^{4n+1}(ex)^m(3a^2Bd^2+3abB(Ad+2Bc)+B^2c(2Ad+Bc))}{m+4n+1} + \frac{a^3Ac^2(ex)^{m+1}}{e(m+1)} + \frac{b^3Bd^2(ex)^{m+1}}{m+5n+1} + \frac{b^3Bd^2e^{m+1}(ex)^m}{m+6n+1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] (a^2\*c\*(3\*A\*b\*c + a\*B\*c + 2\*a\*A\*d)\*x^(1 + n)\*(e\*x)^m/(1 + m + n) + (a\*(a\*B\*c\*(3\*b\*c + 2\*a\*d) + A\*(3\*b^2\*c^2 + 6\*a\*b\*c\*d + a^2\*d^2))\*x^(1 + 2\*n)\*(e\*x)^m/(1 + m + 2\*n) + ((a\*B\*(3\*b^2\*c^2 + 6\*a\*b\*c\*d + a^2\*d^2) + A\*b\*(b^2\*c^2 + 6\*a\*b\*c\*d + 3\*a^2\*d^2))\*x^(1 + 3\*n)\*(e\*x)^m/(1 + m + 3\*n) + (b\*(3\*a^2\*B\*d^2 + 3\*a\*b\*d\*(2\*B\*c + A\*d) + b^2\*c\*(B\*c + 2\*A\*d))\*x^(1 + 4\*n)\*(e\*x)^m/(1 + m + 4\*n) + (b^2\*d\*(2\*b\*B\*c + A\*b\*d + 3\*a\*B\*d))\*x^(1 + 5\*n)\*(e\*x)^m/(1 + m + 5\*n) + (b^3\*B\*d^2\*x^(1 + 6\*n)\*(e\*x)^m)/(1 + m + 6\*n) + (a^3\*A\*c^2\*(e\*x)^(1 + m))/(e\*(1 + m))

#### Rule 20

Int[(u\_.)\*((a\_.)\*(v\_.))^(m\_.)\*((b\_.)\*(v\_.))^(n\_.), x\_Symbol] := Dist[(b^IntPart[n]\*(b\*v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

#### Rule 30

Int[(x\_)^(m\_.), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]

#### Rule 570

Int[((g\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_))^(q\_.)\*((e\_) + (f\_.)\*(x\_)^(n\_))^(r\_.), x\_Symbol] := Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

#### Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^2 dx &= \int (a^3 Ac^2 (ex)^m + a^2 c(3Abc + aBc + 2aAd)x^n (ex)^m + a(aBc(3bc + 2ad) + A(3a^2 d^2 + 6abcd + 3b^2 c^2))x^{2n} (ex)^m \\ &\quad + (b^3 Bd^2)x^{3n} (ex)^m + (a^2 c(3Abc + aBc + 2aAd) + a(aBc(3bc + 2ad) + A(3a^2 d^2 + 6abcd + 3b^2 c^2)))x^{4n} (ex)^m \\ &\quad + (b^3 Bd^2)x^{5n} (ex)^m + (a^2 c(3Abc + aBc + 2aAd) + a(aBc(3bc + 2ad) + A(3a^2 d^2 + 6abcd + 3b^2 c^2)))x^{6n} (ex)^m \\ &= \frac{a^3 Ac^2 (ex)^{1+m}}{e(1+m)} + (b^3 Bd^2) \int x^{6n} (ex)^m dx + (a^2 c(3Abc + aBc + 2aAd) + a(aBc(3bc + 2ad) + A(3a^2 d^2 + 6abcd + 3b^2 c^2))) \int x^{m+6n} dx \\ &= \frac{a^3 Ac^2 (ex)^{1+m}}{e(1+m)} + (b^3 Bd^2 x^{-m} (ex)^m) \int x^{m+6n} dx + (a^2 c(3Abc + aBc + 2aAd) + a(aBc(3bc + 2ad) + A(3a^2 d^2 + 6abcd + 3b^2 c^2))) \int x^{m+6n} dx \\ &= \frac{a^2 c(3Abc + aBc + 2aAd)x^{1+n} (ex)^m}{1+m+n} + \frac{a(aBc(3bc + 2ad) + A(3a^2 d^2 + 6abcd + 3b^2 c^2))x^{1+m}}{1+m+n} \end{aligned}$$

**Mathematica [A]** time = 1.48, size = 273, normalized size = 0.86

$$x^{(m)} \left( \frac{a^2 A c^2}{m+1} + \frac{a x^{2n} (A (a^2 d^2 + 6abcd + 3b^2 c^2) + aBc(2ad + 3bc))}{m+2n+1} + \frac{x^{3n} (Ab (3a^2 d^2 + 6abcd + b^2 c^2) + aB (a^2 d^2 + 6abcd + 3b^2 c^2))}{m+3n+1} + \frac{b x^{4n} (3a^2 B d^2 + 3abd(Ad + 2Bc) + b^2 c(2Ad + Bc))}{m+4n+1} + \frac{a^2 c x^{2n} (2nAd + aBc + 3Abc)}{m+n+1} + \frac{b^2 d x^{3n} (3aBd + Abd + 2Bbc)}{m+5n+1} + \frac{b^3 B d^2 x^{6n}}{m+6n+1} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] x\*(e\*x)^m\*((a^3\*A\*c^2)/(1 + m) + (a^2\*c\*(3\*A\*b\*c + a\*B\*c + 2\*a\*A\*d)\*x^n)/(1 + m + n) + (a\*(a\*B\*c\*(3\*b\*c + 2\*a\*d) + A\*(3\*b^2\*c^2 + 6\*a\*b\*c\*d + a^2\*d^2))\*x^(2\*n))/(1 + m + 2\*n) + ((a\*B\*(3\*b^2\*c^2 + 6\*a\*b\*c\*d + a^2\*d^2) + A\*b\*(b^2\*c^2 + 6\*a\*b\*c\*d + 3\*a^2\*d^2))\*x^(3\*n))/(1 + m + 3\*n) + (b\*(3\*a^2\*B\*d^2 + 3\*a\*b\*d\*(2\*B\*c + A\*d) + b^2\*c\*(B\*c + 2\*A\*d))\*x^(4\*n))/(1 + m + 4\*n) + (b^2\*d\*(2\*b\*B\*c + A\*b\*d + 3\*a\*B\*d)\*x^(5\*n))/(1 + m + 5\*n) + (b^3\*B\*d^2\*x^(6\*n))/(1 + m + 6\*n))

**IntegrateAlgebraic [F]** time = 0.86, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^2 dx$$

Verification is not applicable to the result.

[In] IntegrateAlgebraic[(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] Defer[IntegrateAlgebraic] [(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n)^2, x]

**fricas [B]** time = 0.58, size = 6638, normalized size = 20.87

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="fricas")

[Out] ((B\*b^3\*d^2\*m^6 + 6\*B\*b^3\*d^2\*m^5 + 15\*B\*b^3\*d^2\*m^4 + 20\*B\*b^3\*d^2\*m^3 + 15\*B\*b^3\*d^2\*m^2 + 6\*B\*b^3\*d^2\*m + B\*b^3\*d^2 + 120\*(B\*b^3\*d^2\*m + B\*b^3\*d^2)\*n^5 + 274\*(B\*b^3\*d^2\*m^2 + 2\*B\*b^3\*d^2\*m + B\*b^3\*d^2)\*n^4 + 225\*(B\*b^3\*d^2\*m^3 + 3\*B\*b^3\*d^2\*m^2 + 3\*B\*b^3\*d^2\*m + B\*b^3\*d^2)\*n^3 + 85\*(B\*b^3\*d^2\*m^4 + 4\*B\*b^3\*d^2\*m^3 + 6\*B\*b^3\*d^2\*m^2 + 4\*B\*b^3\*d^2\*m + B\*b^3\*d^2)\*n^2 + 15\*(B\*b^3\*d^2\*m^5 + 5\*B\*b^3\*d^2\*m^4 + 10\*B\*b^3\*d^2\*m^3 + 10\*B\*b^3\*d^2\*m^2 + 5\*B\*b^3\*d^2\*m + B\*b^3\*d^2)\*n)\*x\*x^(6\*n)\*e^(m\*log(e) + m\*log(x)) + ((2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^6 + 2\*B\*b^3\*c\*d + 6\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^5 + 144\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2 + (2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m)\*n^5 + 15\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^4 + 324\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2 + (2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^2 + 2\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m)\*n^4 + 20\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^3 + 260\*(2\*B\*b^3\*c\*d + (2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^3 + (3\*B\*a\*b^2 + A\*b^3)\*d^2 + 3\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^2 + 3\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m)\*n^3 + (3\*B\*a\*b^2 + A\*b^3)\*d^2 + 15\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^2 + 95\*(2\*B\*b^3\*c\*d + (2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^4 + 4\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^3 + (3\*B\*a\*b^2 + A\*b^3)\*d^2 + 6\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^2 + 4\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m)\*n^2 + 6\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m + 16\*(2\*B\*b^3\*c\*d + (2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^5 + 5\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^4 + 10\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^3 + (3\*B\*a\*b^2 + A\*b^3)\*d^2 + 10\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m^2 + 5\*(2\*B\*b^3\*c\*d + (3\*B\*a\*b^2 + A\*b^3)\*d^2)\*m)\*n)\*x\*x^(5\*n)\*e^(m\*log(e) + m\*log(x)) + ((B\*b^3\*c^2 + 2\*(3\*B\*a\*b^2 + A\*b^3)\*c\*d + 3\*(B\*a^2\*b + A\*a\*b^2)\*d^2)\*m^6 + B\*b^3\*c^2 + 6\*(B\*b^3\*c^2 + 2\*(3\*B\*a\*b^2 + A\*b^3)\*c\*d + 3\*(B\*a^2\*b + A\*a\*b^2)\*d^2)\*m^5 + 180\*(B\*b^3\*c^2 + 2\*(3\*B\*a\*b^2 + A\*b^3)\*c\*d + 3\*(B\*a^2\*b + A\*a\*b^2)\*d^2)\*m^4 + 180\*(B\*b^3\*c^2 + 2\*(3\*B\*a\*b^2 + A\*b^3)\*c\*d + 3\*(B\*a^2\*b + A\*a\*b^2)\*d^2)\*m^3 + 180\*(B\*b^3\*c^2 + 2\*(3\*B\*a\*b^2 + A\*b^3)\*c\*d + 3\*(B\*a^2\*b + A\*a\*b^2)\*d^2)\*m^2 + 180\*(B\*b^3\*c^2 + 2\*(3\*B\*a\*b^2 + A\*b^3)\*c\*d + 3\*(B\*a^2\*b + A\*a\*b^2)\*d^2)\*m + 180\*(B\*b^3\*c^2 + 2\*(3\*B\*a\*b^2 + A\*b^3)\*c\*d + 3\*(B\*a^2\*b + A\*a\*b^2)\*d^2))



$$\begin{aligned}
& 0*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d + (A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m)*n^5 + 15 \\
& *(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m^4 + 702*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d + (A \\
& *a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m^2 + 2*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m)*n^4 + \\
& 20*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m^3 + 461*(A*a^3*d^2 + (A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A \\
& *a^2*b)*c*d)*m^3 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d + 3*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m^2 + \\
& 3*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m)*n^3 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d + 15*(A*a^3*d^2 \\
& + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m^2 + 137*(A*a^3*d^2 \\
& ^2 + (A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m^4 + 4*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m \\
& ^3 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d + 6*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m^2 + 4*(A*a^3*d^2 \\
& + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m)*n^2 + 6*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m + 19*(A*a^3*d^2 \\
& + (A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m^5 + 5*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)* \\
& m^4 + 10*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d) \\
& )*m^3 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d + 10*(A*a^3*d^2 \\
& ^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m^2 + 5*(A*a^3*d^2 + 3*(B*a^2*b + A*a*b^2)*c^2 + 2*(B*a^3 + 3*A*a^2*b)*c*d)*m)*n)*x*x^(2*n) \\
& )*e^(m*log(e) + m*log(x)) + ((2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m^6 + 2*A*a^3*c*d + 6*(2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m^5 + 720*(2*A*a^3*c \\
& *d + (B*a^3 + 3*A*a^2*b)*c^2 + (2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m)* \\
& n^5 + 15*(2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m^4 + 1044*(2*A*a^3*c*d + \\
& (B*a^3 + 3*A*a^2*b)*c^2 + (2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m^2 + 2*( \\
& 2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m)*n^4 + 20*(2*A*a^3*c*d + (B*a^3 + \\
& 3*A*a^2*b)*c^2)*m^3 + 580*(2*A*a^3*c*d + (2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b) \\
& )*c^2)*m^3 + (B*a^3 + 3*A*a^2*b)*c^2 + 3*(2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)* \\
& )*c^2)*m^2 + 3*(2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m)*n^3 + (B*a^3 + 3*A* \\
& )*a^2*b)*c^2 + 15*(2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m^2 + 155*(2*A*a^3*c \\
& *d + (2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m^4 + 4*(2*A*a^3*c*d + (B*a^3 \\
& + 3*A*a^2*b)*c^2)*m^3 + (B*a^3 + 3*A*a^2*b)*c^2 + 6*(2*A*a^3*c*d + (B*a^3 \\
& + 3*A*a^2*b)*c^2)*m^2 + 4*(2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m)*n^2 + \\
& 6*(2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m + 20*(2*A*a^3*c*d + (2*A*a^3*c* \\
& )*d + (B*a^3 + 3*A*a^2*b)*c^2)*m^5 + 5*(2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2 \\
& )*m^4 + 10*(2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m^3 + (B*a^3 + 3*A*a^2*b) \\
& )*c^2 + 10*(2*A*a^3*c*d + (B*a^3 + 3*A*a^2*b)*c^2)*m^2 + 5*(2*A*a^3*c*d + ( \\
& )*B*a^3 + 3*A*a^2*b)*c^2)*m)*n)*x*x^n*e^(m*log(e) + m*log(x)) + (A*a^3*c^2*m^6 \\
& + 720*A*a^3*c^2*n^6 + 6*A*a^3*c^2*m^5 + 15*A*a^3*c^2*m^4 + 20*A*a^3*c^2*m \\
& ^3 + 15*A*a^3*c^2*m^2 + 6*A*a^3*c^2*m + A*a^3*c^2 + 1764*(A*a^3*c^2*m + A*a \\
& ^3*c^2)*n^5 + 1624*(A*a^3*c^2*m^2 + 2*A*a^3*c^2*m + A*a^3*c^2)*n^4 + 735*(A \\
& )*a^3*c^2*m^3 + 3*A*a^3*c^2*m^2 + 3*A*a^3*c^2*m + A*a^3*c^2)*n^3 + 175*(A*a^ \\
& )*3*c^2*m^4 + 4*A*a^3*c^2*m^3 + 6*A*a^3*c^2*m^2 + 4*A*a^3*c^2*m + A*a^3*c^2)* \\
& n^2 + 21*(A*a^3*c^2*m^5 + 5*A*a^3*c^2*m^4 + 10*A*a^3*c^2*m^3 + 10*A*a^3*c^2 \\
& )*m^2 + 5*A*a^3*c^2*m + A*a^3*c^2)*n)*x*x^n*e^(m*log(e) + m*log(x)))/(m^7 + 720* \\
& (m + 1)*n^6 + 7*m^6 + 1764*(m^2 + 2*m + 1)*n^5 + 21*m^5 + 1624*(m^3 + 3*m^2 \\
& + 3*m + 1)*n^4 + 35*m^4 + 735*(m^4 + 4*m^3 + 6*m^2 + 4*m + 1)*n^3 + 35*m^3 \\
& + 175*(m^5 + 5*m^4 + 10*m^3 + 10*m^2 + 5*m + 1)*n^2 + 21*m^2 + 21*(m^6 + 6 \\
& )*m^5 + 15*m^4 + 20*m^3 + 15*m^2 + 6*m + 1)*n + 7*m + 1)
\end{aligned}$$

**giac [B]** time = 2.01, size = 15358, normalized size = 48.30

result too large to display

Verification of antiderivative is not currently implemented for this CAS.



[In] integrate((e\*x)^(m\*(a+b\*x^n))^3\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="giac")

[Out]  $(B*b^3*d^2*m^6*x*x^m*x^{(6*n)}*e^m + 15*B*b^3*d^2*m^5*n*x*x^m*x^{(6*n)}*e^m + 8*5*B*b^3*d^2*m^4*n^2*x*x^m*x^{(6*n)}*e^m + 225*B*b^3*d^2*m^3*n^3*x*x^m*x^{(6*n)}*e^m + 274*B*b^3*d^2*m^2*n^4*x*x^m*x^{(6*n)}*e^m + 120*B*b^3*d^2*m*n^5*x*x^m*x^{(6*n)}*e^m + 2*B*b^3*c*d*m^6*x*x^m*x^{(5*n)}*e^m + 3*B*a*b^2*d^2*m^6*x*x^m*x^{(5*n)}*e^m + A*b^3*d^2*m^6*x*x^m*x^{(5*n)}*e^m + 32*B*b^3*c*d*m^5*n*x*x^m*x^{(5*n)}*e^m + 48*B*a*b^2*d^2*m^5*n*x*x^m*x^{(5*n)}*e^m + 16*A*b^3*d^2*m^5*n*x*x^m*x^{(5*n)}*e^m + 190*B*b^3*c*d*m^4*n^2*x*x^m*x^{(5*n)}*e^m + 285*B*a*b^2*d^2*m^4*n^2*x*x^m*x^{(5*n)}*e^m + 95*A*b^3*d^2*m^4*n^2*x*x^m*x^{(5*n)}*e^m + 520*B*b^3*c*d*m^3*n^3*x*x^m*x^{(5*n)}*e^m + 780*B*a*b^2*d^2*m^3*n^3*x*x^m*x^{(5*n)}*e^m + 260*A*b^3*d^2*m^3*n^3*x*x^m*x^{(5*n)}*e^m + 648*B*b^3*c*d*m^2*n^4*x*x^m*x^{(5*n)}*e^m + 972*B*a*b^2*d^2*m^2*n^4*x*x^m*x^{(5*n)}*e^m + 324*A*b^3*d^2*m^2*n^4*x*x^m*x^{(5*n)}*e^m + 288*B*b^3*c*d*m*n^5*x*x^m*x^{(5*n)}*e^m + 432*B*a*b^2*d^2*m*n^5*x*x^m*x^{(5*n)}*e^m + 144*A*b^3*d^2*m*n^5*x*x^m*x^{(5*n)}*e^m + B*b^3*c^2*m^6*x*x^m*x^{(4*n)}*e^m + 6*B*a*b^2*c*d*m^6*x*x^m*x^{(4*n)}*e^m + 2*A*b^3*c*d*m^6*x*x^m*x^{(4*n)}*e^m + 3*B*a^2*b*d^2*m^6*x*x^m*x^{(4*n)}*e^m + 3*A*a*b^2*d^2*m^6*x*x^m*x^{(4*n)}*e^m + 17*B*b^3*c^2*m^5*n*x*x^m*x^{(4*n)}*e^m + 102*B*a*b^2*c*d*m^5*n*x*x^m*x^{(4*n)}*e^m + 34*A*b^3*c*d*m^5*n*x*x^m*x^{(4*n)}*e^m + 51*B*a^2*b*d^2*m^5*n*x*x^m*x^{(4*n)}*e^m + 51*A*a*b^2*d^2*m^5*n*x*x^m*x^{(4*n)}*e^m + 107*B*b^3*c^2*m^4*n^2*x*x^m*x^{(4*n)}*e^m + 642*B*a*b^2*c*d*m^4*n^2*x*x^m*x^{(4*n)}*e^m + 214*A*b^3*c*d*m^4*n^2*x*x^m*x^{(4*n)}*e^m + 321*B*a^2*b*d^2*m^4*n^2*x*x^m*x^{(4*n)}*e^m + 321*A*a*b^2*d^2*m^4*n^2*x*x^m*x^{(4*n)}*e^m + 307*B*b^3*c^2*m^3*n^3*x*x^m*x^{(4*n)}*e^m + 1842*B*a*b^2*c*d*m^3*n^3*x*x^m*x^{(4*n)}*e^m + 614*A*b^3*c*d*m^3*n^3*x*x^m*x^{(4*n)}*e^m + 921*B*a^2*b*d^2*m^3*n^3*x*x^m*x^{(4*n)}*e^m + 921*A*a*b^2*d^2*m^3*n^3*x*x^m*x^{(4*n)}*e^m + 396*B*b^3*c^2*m^2*n^4*x*x^m*x^{(4*n)}*e^m + 2376*B*a*b^2*c*d*m^2*n^4*x*x^m*x^{(4*n)}*e^m + 792*A*b^3*c*d*m^2*n^4*x*x^m*x^{(4*n)}*e^m + 1188*B*a^2*b*d^2*m^2*n^4*x*x^m*x^{(4*n)}*e^m + 1188*A*a*b^2*d^2*m^2*n^4*x*x^m*x^{(4*n)}*e^m + 180*B*b^3*c^2*m*n^5*x*x^m*x^{(4*n)}*e^m + 1080*B*a*b^2*c*d*m*n^5*x*x^m*x^{(4*n)}*e^m + 360*A*b^3*c*d*m*n^5*x*x^m*x^{(4*n)}*e^m + 540*B*a^2*b*d^2*m*n^5*x*x^m*x^{(4*n)}*e^m + 540*A*a*b^2*d^2*m*n^5*x*x^m*x^{(4*n)}*e^m + 3*B*a*b^2*c^2*m^6*x*x^m*x^{(3*n)}*e^m + A*b^3*c^2*m^6*x*x^m*x^{(3*n)}*e^m + 6*B*a^2*b*c*d*m^6*x*x^m*x^{(3*n)}*e^m + 6*A*a*b^2*c*d*m^6*x*x^m*x^{(3*n)}*e^m + B*a^3*d^2*m^6*x*x^m*x^{(3*n)}*e^m + 3*A*a^2*b*d^2*m^6*x*x^m*x^{(3*n)}*e^m + 54*B*a*b^2*c^2*m^5*n*x*x^m*x^{(3*n)}*e^m + 18*A*b^3*c^2*m^5*n*x*x^m*x^{(3*n)}*e^m + 108*B*a^2*b*c*d*m^5*n*x*x^m*x^{(3*n)}*e^m + 108*A*a*b^2*c*d*m^5*n*x*x^m*x^{(3*n)}*e^m + 18*B*a^3*d^2*m^5*n*x*x^m*x^{(3*n)}*e^m + 54*A*a^2*b*d^2*m^5*n*x*x^m*x^{(3*n)}*e^m + 363*B*a*b^2*c^2*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 121*A*b^3*c^2*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 726*B*a^2*b*c*d*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 726*A*a*b^2*c*d*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 121*B*a^3*d^2*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 363*A*a^2*b*d^2*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 1116*B*a*b^2*c^2*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 372*A*b^3*c^2*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 2232*B*a^2*b*c*d*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 2232*A*a*b^2*c*d*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 372*B*a^3*d^2*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 1116*A*a^2*b*d^2*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 1524*B*a*b^2*c^2*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 508*A*b^3*c^2*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 3048*B*a^2*b*c*d*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 3048*A*a*b^2*c*d*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 508*B*a^3*d^2*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 1524*A*a^2*b*d^2*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 720*B*a*b^2*c^2*m*n^5*x*x^m*x^{(3*n)}*e^m + 240*A*b^3*c^2*m*n^5*x*x^m*x^{(3*n)}*e^m + 1440*B*a^2*b*c*d*m*n^5*x*x^m*x^{(3*n)}*e^m + 1440*A*a*b^2*c*d*m*n^5*x*x^m*x^{(3*n)}*e^m + 240*B*a^3*d^2*m*n^5*x*x^m*x^{(3*n)}*e^m + 720*A*a^2*b*d^2*m*n^5*x*x^m*x^{(3*n)}*e^m + 3*B*a^2*b*c^2*m^6*x*x^m*x^{(2*n)}*e^m + 3*A*a*b^2*c^2*m^6*x*x^m*x^{(2*n)}*e^m + 2*B*a^3*c*d*m^6*x*x^m*x^{(2*n)}*e^m + 6*A*a^2*b*c*d*m^6*x*x^m*x^{(2*n)}*e^m + A*a^3*d^2*m^6*x*x^m*x^{(2*n)}*e^m + 57*B*a^2*b*c^2*m^5*n*x*x^m*x^{(2*n)}*e^m + 57*A*a*b^2*c^2*m^5*n*x*x^m*x^{(2*n)}*e^m + 38*B*a^3*c*d*m^5*n*x*x^m*x^{(2*n)}*e^m + 114*A*a^2*b*c*d*m^5*n*x*x^m*x^{(2*n)}*e^m + 19*A*a^3*d^2*m^5*n*x*x^m*x^{(2*n)}*e^m + 411*B*a^2*b*c^2*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 411*A*a*b^2*c^2*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 274*B*a^3*c*d*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 822*A*a^2*b*c*d*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 137*A*a^3*d^2*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 1383*B*a^2*b*c^2*m^3*n^3*x*x^m$

$x^{(2n)}e^m + 1383A^2ab^2c^2m^3n^3xxx^m x^{(2n)}e^m + 922B^3a^3c^2d^3n^3xxx^m x^{(2n)}e^m + 2766A^2a^2b^2c^2d^3n^3xxx^m x^{(2n)}e^m + 461$   
 $A^3a^3d^2m^3n^3xxx^m x^{(2n)}e^m + 2106B^2a^2b^2c^2m^2n^4xxx^m x^{(2n)}e^m + 2106A^2ab^2c^2m^2n^4xxx^m x^{(2n)}e^m + 1404B^3a^3c^2d^2n^4$   
 $xxx^m x^{(2n)}e^m + 4212A^2a^2b^2c^2d^2n^4xxx^m x^{(2n)}e^m + 702A^3a^3d^2m^2n^4xxx^m x^{(2n)}e^m + 1080B^2a^2b^2c^2m^2n^5xxx^m x^{(2n)}e^m$   
 $+ 1080A^2ab^2c^2m^2n^5xxx^m x^{(2n)}e^m + 720B^3a^3c^2d^2m^2n^5xxx^m x^{(2n)}e^m + 2160A^2a^2b^2c^2d^2m^2n^5xxx^m x^{(2n)}e^m + 360A^3a^3d^2m^2n^5xxx^m$   
 $x^{(2n)}e^m + B^3a^3c^2m^6xxx^m x^{(2n)}e^m + 3A^2a^2b^2c^2m^6xxx^m x^{(2n)}e^m + 2A^3a^3c^2d^2m^6xxx^m x^{(2n)}e^m + 20B^2a^2b^2c^2m^5n^2xxx^m x^{(2n)}e^m + 6$   
 $0A^2a^2b^2c^2m^5n^2xxx^m x^{(2n)}e^m + 40A^3a^3c^2d^2m^5n^2xxx^m x^{(2n)}e^m + 155B^3a^3c^2m^4n^2xxx^m x^{(2n)}e^m + 465A^2a^2b^2c^2m^4n^2xxx^m x^{(2n)}e^m + 3$   
 $10A^3a^3c^2d^2m^4n^2xxx^m x^{(2n)}e^m + 580B^2a^2b^2c^2m^3n^3xxx^m x^{(2n)}e^m + 1740A^2a^2b^2c^2m^3n^3xxx^m x^{(2n)}e^m + 1160A^3a^3c^2d^2m^3n^3xxx^m x^{(2n)}e^m$   
 $+ 1044B^3a^3c^2m^2n^4xxx^m x^{(2n)}e^m + 3132A^2a^2b^2c^2m^2n^4xxx^m x^{(2n)}e^m + 2088A^3a^3c^2d^2m^2n^4xxx^m x^{(2n)}e^m + 720B^2a^2b^2c^2m^2n^5xxx^m x^{(2n)}e^m$   
 $+ 2160A^2a^2b^2c^2m^2n^5xxx^m x^{(2n)}e^m + 1440A^3a^3c^2d^2m^2n^5xxx^m x^{(2n)}e^m + A^3a^3c^2m^6xxx^m x^{(2n)}e^m + 21A^2a^2b^2c^2m^5n^2xxx^m x^{(2n)}e^m + 175A^3a^3c^2$   
 $m^4n^2xxx^m x^{(2n)}e^m + 735A^2a^2b^2c^2m^3n^3xxx^m x^{(2n)}e^m + 1624A^3a^3c^2m^2n^4xxx^m x^{(2n)}e^m + 1764A^2a^2b^2c^2m^2n^5xxx^m x^{(2n)}e^m + 720A^3a^3c^2n^6xxx^m$   
 $x^{(2n)}e^m + 6B^3b^3d^2m^5xxx^m x^{(6n)}e^m + 75B^2b^3d^2m^4n^2xxx^m x^{(6n)}e^m + 340B^3b^3d^2m^3n^2xxx^m x^{(6n)}e^m + 675B^2b^3d^2m^2n^3xxx^m x^{(6n)}e^m$   
 $+ 548B^3b^3d^2m^2n^4xxx^m x^{(6n)}e^m + 120B^2b^3d^2m^2n^5xxx^m x^{(6n)}e^m + 12B^3b^3c^2d^2m^5xxx^m x^{(5n)}e^m + 18B^2a^2b^2d^2m^5xxx^m x^{(5n)}e^m + 6A^2b^3d^2m^5xxx^m x^{(5n)}e^m$   
 $+ 160B^3b^3c^2d^2m^4n^2xxx^m x^{(5n)}e^m + 240B^2a^2b^2d^2m^4n^2xxx^m x^{(5n)}e^m + 80A^2b^3d^2m^4n^2xxx^m x^{(5n)}e^m + 760B^3b^3c^2d^2m^3n^2xxx^m x^{(5n)}e^m + 1140$   
 $B^2a^2b^2d^2m^3n^2xxx^m x^{(5n)}e^m + 380A^2b^3d^2m^3n^2xxx^m x^{(5n)}e^m + 1560B^3b^3c^2d^2m^2n^3xxx^m x^{(5n)}e^m + 2340B^2a^2b^2d^2m^2n^3xxx^m x^{(5n)}e^m + 780A^2b^3d^2m^2n^3xxx^m x^{(5n)}e^m$   
 $+ 1296B^3b^3c^2d^2m^2n^4xxx^m x^{(5n)}e^m + 1944B^2a^2b^2d^2m^2n^4xxx^m x^{(5n)}e^m + 648A^2b^3d^2m^2n^4xxx^m x^{(5n)}e^m + 288B^3b^3c^2d^2n^5xxx^m x^{(5n)}e^m + 432B^2a^2b^2d^2n^5xxx^m x^{(5n)}e^m + 144A^2b^3d^2n^5xxx^m x^{(5n)}e^m$   
 $+ 6B^3b^3c^2m^5xxx^m x^{(4n)}e^m + 36B^2a^2b^2c^2d^2m^5xxx^m x^{(4n)}e^m + 12A^2b^3c^2d^2m^5xxx^m x^{(4n)}e^m + 18B^2a^2b^2d^2m^5xxx^m x^{(4n)}e^m + 18A^2a^2b^2d^2m^5xxx^m x^{(4n)}e^m + 85B^3b^3c^2m^4n^2xxx^m x^{(4n)}e^m$   
 $+ 510B^2a^2b^2c^2d^2m^4n^2xxx^m x^{(4n)}e^m + 170A^2b^3c^2d^2m^4n^2xxx^m x^{(4n)}e^m + 255B^3a^3d^2m^4n^2xxx^m x^{(4n)}e^m + 255A^2a^2b^2d^2m^4n^2xxx^m x^{(4n)}e^m + 428B^3b^3c^2m^3n^2xxx^m x^{(4n)}e^m + 2568B^2a^2b^2$   
 $c^2d^2m^3n^2xxx^m x^{(4n)}e^m + 856A^2b^3c^2d^2m^3n^2xxx^m x^{(4n)}e^m + 1284B^2a^2b^2d^2m^3n^2xxx^m x^{(4n)}e^m + 1284A^2a^2b^2d^2m^3n^2xxx^m x^{(4n)}e^m + 921B^3b^3c^2m^2n^3xxx^m x^{(4n)}e^m + 5526B^2a^2b^2c^2d^2m^2n^3xxx^m x^{(4n)}e^m$   
 $+ 1842A^2b^3c^2d^2m^2n^3xxx^m x^{(4n)}e^m + 2763B^2a^2b^2d^2m^2n^3xxx^m x^{(4n)}e^m + 792B^3b^3c^2m^2n^4xxx^m x^{(4n)}e^m + 4752B^2a^2b^2c^2d^2m^2n^4xxx^m x^{(4n)}e^m + 1584A^2b^3c^2d^2m^2n^4xxx^m x^{(4n)}e^m + 2376B^3a^3d^2m^2n^4xxx^m x^{(4n)}e^m$   
 $+ 2376A^2a^2b^2d^2m^2n^4xxx^m x^{(4n)}e^m + 180B^3b^3c^2n^5xxx^m x^{(4n)}e^m + 1080B^2a^2b^2c^2d^2n^5xxx^m x^{(4n)}e^m + 360A^2b^3c^2d^2n^5xxx^m x^{(4n)}e^m + 540B^2a^2b^2d^2n^5xxx^m x^{(4n)}e^m + 18B^2a^2b^2c^2m^5xxx^m x^{(3n)}e^m$   
 $+ 6A^2b^3c^2m^5xxx^m x^{(3n)}e^m + 36B^2a^2b^2c^2d^2m^5xxx^m x^{(3n)}e^m + 36A^2a^2b^2c^2d^2m^5xxx^m x^{(3n)}e^m + 6B^3a^3d^2m^5xxx^m x^{(3n)}e^m + 18A^2a^2b^2d^2m^5xxx^m x^{(3n)}e^m + 270B^2a^2b^2c^2m^4n^2xxx^m x^{(3n)}e^m$   
 $+ 90A^2b^3c^2m^4n^2xxx^m x^{(3n)}e^m + 540B^2a^2b^2c^2d^2m^4n^2xxx^m x^{(3n)}e^m + 540A^2a^2b^2c^2d^2m^4n^2xxx^m x^{(3n)}e^m + 90B^3a^3d^2m^4n^2xxx^m x^{(3n)}e^m + 270A^2a^2b^2d^2m^4n^2xxx^m x^{(3n)}e^m + 1452B^2a^2b^2c^2m^3n^2xxx^m x^{(3n)}e^m$   
 $+ 484A^2b^3c^2m^3n^2xxx^m x^{(3n)}e^m + 2904B^2a^2b^2c^2d^2m^3n^2xxx^m x^{(3n)}e^m + 2904A^2a^2b^2c^2d^2m^3n^2xxx^m x^{(3n)}e^m + 484B^3a^3d^2m^3n^2xxx^m x^{(3n)}e^m + 1452A^2a^2b^2$

$$\begin{aligned}
& d^2 m^3 n^2 x x^m x^{(3n)} e^m + 3348 B a^2 b^2 c^2 m^2 n^3 x x^m x^{(3n)} e^m \\
& + 1116 A a^3 b^3 c^2 m^2 n^3 x x^m x^{(3n)} e^m + 6696 B a^2 b^2 c^2 m^2 n^3 x x^m x^{(3n)} e^m \\
& + 6696 A a^2 b^2 c^2 m^2 n^3 x x^m x^{(3n)} e^m + 1116 B a^3 d^2 m^2 n^3 x x^m x^{(3n)} e^m \\
& + 3348 A a^2 b^2 d^2 m^2 n^3 x x^m x^{(3n)} e^m + 3048 B a^2 b^2 c^2 m^2 n^4 x x^m x^{(3n)} e^m \\
& + 1016 A a^3 b^3 c^2 m^2 n^4 x x^m x^{(3n)} e^m + 6096 B a^2 b^2 c^2 m^2 n^4 x x^m x^{(3n)} e^m \\
& + 6096 A a^2 b^2 c^2 m^2 n^4 x x^m x^{(3n)} e^m + 1016 B a^3 d^2 m^2 n^4 x x^m x^{(3n)} e^m \\
& + 3048 A a^2 b^2 d^2 m^2 n^4 x x^m x^{(3n)} e^m + 720 B a^2 b^2 c^2 m^2 n^5 x x^m x^{(3n)} e^m \\
& + 240 A a^3 b^3 c^2 m^2 n^5 x x^m x^{(3n)} e^m + 1440 B a^2 b^2 c^2 m^2 n^5 x x^m x^{(3n)} e^m \\
& + 1440 A a^2 b^2 c^2 m^2 n^5 x x^m x^{(3n)} e^m + 240 B a^3 d^2 m^2 n^5 x x^m x^{(3n)} e^m \\
& + 720 A a^2 b^2 d^2 m^2 n^5 x x^m x^{(3n)} e^m + 18 B a^2 b^2 c^2 m^5 x x^m x^{(2n)} e^m \\
& + 18 A a^2 b^2 c^2 m^5 x x^m x^{(2n)} e^m + 12 B a^3 c^2 m^5 x x^m x^{(2n)} e^m \\
& + 36 A a^2 b^2 c^2 m^5 x x^m x^{(2n)} e^m + 6 A a^3 d^2 m^5 x x^m x^{(2n)} e^m \\
& + 285 B a^2 b^2 c^2 m^4 n x x^m x^{(2n)} e^m + 285 A a^2 b^2 c^2 m^4 n x x^m x^{(2n)} e^m \\
& + 190 B a^3 c^2 m^4 n x x^m x^{(2n)} e^m + 570 A a^2 b^2 c^2 m^4 n x x^m x^{(2n)} e^m \\
& + 95 A a^3 d^2 m^4 n x x^m x^{(2n)} e^m + 1644 B a^2 b^2 c^2 m^3 n^2 x x^m x^{(2n)} e^m \\
& + 1644 A a^2 b^2 c^2 m^3 n^2 x x^m x^{(2n)} e^m + 1096 B a^3 c^2 m^3 n^2 x x^m x^{(2n)} e^m \\
& + 3288 A a^2 b^2 c^2 m^3 n^2 x x^m x^{(2n)} e^m + 548 A a^3 d^2 m^3 n^2 x x^m x^{(2n)} e^m \\
& + 4149 B a^2 b^2 c^2 m^2 n^3 x x^m x^{(2n)} e^m + 4149 A a^2 b^2 c^2 m^2 n^3 x x^m x^{(2n)} e^m \\
& + 2766 B a^3 c^2 m^2 n^3 x x^m x^{(2n)} e^m + 8298 A a^2 b^2 c^2 m^2 n^3 x x^m x^{(2n)} e^m \\
& + 1383 A a^3 d^2 m^2 n^3 x x^m x^{(2n)} e^m + 4212 B a^2 b^2 c^2 m^2 n^4 x x^m x^{(2n)} e^m \\
& + 4212 A a^2 b^2 c^2 m^2 n^4 x x^m x^{(2n)} e^m + 2808 B a^3 c^2 m^2 n^4 x x^m x^{(2n)} e^m \\
& + 8424 A a^2 b^2 c^2 m^2 n^4 x x^m x^{(2n)} e^m + 1404 A a^3 d^2 m^2 n^4 x x^m x^{(2n)} e^m \\
& + 1080 B a^2 b^2 c^2 m^2 n^5 x x^m x^{(2n)} e^m + 1080 A a^2 b^2 c^2 m^2 n^5 x x^m x^{(2n)} e^m \\
& + 720 B a^3 c^2 m^2 n^5 x x^m x^{(2n)} e^m + 360 A a^3 d^2 m^2 n^5 x x^m x^{(2n)} e^m \\
& + 6 B a^3 c^2 m^5 x x^m x^{2n} e^m + 18 A a^2 b^2 c^2 m^5 x x^m x^{2n} e^m \\
& + 12 A a^3 c^2 m^5 x x^m x^{2n} e^m + 100 B a^3 c^2 m^4 n x x^m x^{2n} e^m + 300 A a^2 b^2 c^2 m^4 n x x^m x^{2n} e^m \\
& + 200 A a^3 c^2 m^4 n x x^m x^{2n} e^m + 620 B a^3 c^2 m^3 n^2 x x^m x^{2n} e^m + 1860 A a^2 b^2 c^2 m^3 n^2 x x^m x^{2n} e^m \\
& + 1240 A a^3 c^2 m^3 n^2 x x^m x^{2n} e^m + 1740 B a^3 c^2 m^2 n^3 x x^m x^{2n} e^m \\
& + 5220 A a^2 b^2 c^2 m^2 n^3 x x^m x^{2n} e^m + 3480 A a^3 c^2 m^2 n^3 x x^m x^{2n} e^m \\
& + 2088 B a^3 c^2 m^2 n^4 x x^m x^{2n} e^m + 6264 A a^2 b^2 c^2 m^2 n^4 x x^m x^{2n} e^m \\
& + 4176 A a^3 c^2 m^2 n^4 x x^m x^{2n} e^m + 720 B a^3 c^2 m^2 n^5 x x^m x^{2n} e^m \\
& + 2160 A a^2 b^2 c^2 m^2 n^5 x x^m x^{2n} e^m + 1440 A a^3 c^2 m^2 n^5 x x^m x^{2n} e^m \\
& + 6 A a^3 c^2 m^5 x x^m e^m + 105 A a^3 c^2 m^4 n x x^m e^m + 700 A a^3 c^2 m^3 n^2 x x^m e^m \\
& + 2205 A a^3 c^2 m^2 n^3 x x^m e^m + 3248 A a^3 c^2 m^2 n^4 x x^m e^m + 1764 A a^3 c^2 m^2 n^5 x x^m e^m \\
& + 15 B b^3 d^2 m^4 x x^m x^{(6n)} e^m + 150 B b^3 d^2 m^3 n x x^m x^{(6n)} e^m + 510 B b^3 d^2 m^2 n^2 x x^m x^{(6n)} e^m \\
& + 675 B b^3 d^2 m^2 n^3 x x^m x^{(6n)} e^m + 274 B b^3 d^2 m^2 n^4 x x^m x^{(6n)} e^m \\
& + 30 B b^3 c^2 d^2 m^4 x x^m x^{(5n)} e^m + 45 B a^2 b^2 d^2 m^4 x x^m x^{(5n)} e^m \\
& + 15 A b^3 d^2 m^4 x x^m x^{(5n)} e^m + 320 B b^3 c^2 d^2 m^3 n x x^m x^{(5n)} e^m \\
& + 480 B a^2 b^2 d^2 m^3 n x x^m x^{(5n)} e^m + 160 A b^3 d^2 m^3 n x x^m x^{(5n)} e^m \\
& + 1140 B b^3 c^2 d^2 m^2 n^2 x x^m x^{(5n)} e^m + 1710 B a^2 b^2 d^2 m^2 n^2 x x^m x^{(5n)} e^m \\
& + 570 A b^3 d^2 m^2 n^2 x x^m x^{(5n)} e^m + 1560 B b^3 c^2 d^2 m^2 n^3 x x^m x^{(5n)} e^m \\
& + 2340 B a^2 b^2 d^2 m^2 n^3 x x^m x^{(5n)} e^m + 780 A b^3 d^2 m^2 n^3 x x^m x^{(5n)} e^m \\
& + 648 B b^3 c^2 d^2 m^4 x x^m x^{(5n)} e^m + 972 B a^2 b^2 d^2 m^4 x x^m x^{(5n)} e^m \\
& + 324 A b^3 d^2 m^4 x x^m x^{(5n)} e^m + 15 B b^3 c^2 m^4 x x^m x^{(4n)} e^m + 90 B a^2 b^2 c^2 d^2 m^4 x x^m x^{(4n)} e^m \\
& + 30 A b^3 c^2 d^2 m^4 x x^m x^{(4n)} e^m + 45 B a^2 b^2 d^2 m^4 x x^m x^{(4n)} e^m \\
& + 45 A a^2 b^2 d^2 m^4 x x^m x^{(4n)} e^m + 170 B b^3 c^2 m^3 n x x^m x^{(4n)} e^m \\
& + 1020 B a^2 b^2 c^2 d^2 m^3 n x x^m x^{(4n)} e^m + 340 A b^3 c^2 d^2 m^3 n x x^m x^{(4n)} e^m \\
& + 510 B a^2 b^2 d^2 m^3 n x x^m x^{(4n)} e^m + 642 B b^3 c^2 m^2 n^2 x x^m x^{(4n)} e^m \\
& + 3852 B a^2 b^2 c^2 d^2 m^2 n^2 x x^m x^{(4n)} e^m + 1284 A b^3 c^2 d^2 m^2 n^2 x x^m x^{(4n)} e^m \\
& + 1926 B a^2 b^2 d^2 m^2 n^2 x x^m x^{(4n)} e^m + 1926 A a^2 b^2 d^2 m^2 n^2 x x^m x^{(4n)} e^m \\
& + 921 B b^3 c^2 m^2 n^3 x x^m x^{(4n)} e^m + 5526 B a^2 b^2 c^2 d^2 m^2 n^3 x x^m x^{(4n)} e^m \\
& + 1842 A b^3 c^2 d^2 m^2 n^3 x x^m x^{(4n)} e^m
\end{aligned}$$

$$\begin{aligned}
& x^{(4n)}e^m + 2763B^2a^2bd^2m^3x^m x^{(4n)}e^m + 2763A^2ab^2d^2m^3x^m x^{(4n)}e^m + 2763A^2ab^2d^2m^3x^m x^{(4n)}e^m + 2763A^2ab^2d^2m^3x^m x^{(4n)}e^m \\
& + 396B^2b^3c^2n^4x^m x^{(4n)}e^m + 2376B^2ab^2c^2d^2n^4x^m x^{(4n)}e^m + 792A^2b^3c^2d^2n^4x^m x^{(4n)}e^m + 1188B^2a^2b^2d^2n^4x^m x^{(4n)}e^m + 1188A^2ab^2d^2n^4x^m x^{(4n)}e^m + 4 \\
& + 5B^2ab^2c^2m^4x^m x^{(3n)}e^m + 15A^2b^3c^2m^4x^m x^{(3n)}e^m + 90B^2a^2b^2c^2d^2m^4x^m x^{(3n)}e^m + 90A^2ab^2c^2d^2m^4x^m x^{(3n)}e^m \\
& + 15B^2a^3d^2m^4x^m x^{(3n)}e^m + 45A^2a^2bd^2m^4x^m x^{(3n)}e^m + 540B^2ab^2c^2m^3n^3x^m x^{(3n)}e^m + 180A^2b^3c^2m^3n^3x^m x^{(3n)}e^m \\
& + 1080B^2a^2b^2c^2d^2m^3n^3x^m x^{(3n)}e^m + 1080A^2ab^2c^2d^2m^3n^3x^m x^{(3n)}e^m + 180B^2a^3d^2m^3n^3x^m x^{(3n)}e^m + 540A^2a^2bd^2m^3n^3x^m x^{(3n)}e^m \\
& + 2178B^2ab^2c^2m^2n^2x^m x^{(3n)}e^m + 726A^2b^3c^2m^2n^2x^m x^{(3n)}e^m + 4356B^2a^2b^2c^2d^2m^2n^2x^m x^{(3n)}e^m + 4356A^2ab^2c^2d^2m^2n^2x^m x^{(3n)}e^m \\
& + 726B^2a^3d^2m^2n^2x^m x^{(3n)}e^m + 2178A^2a^2bd^2m^2n^2x^m x^{(3n)}e^m + 3348B^2ab^2c^2m^2n^3x^m x^{(3n)}e^m + 1116A^2b^3c^2m^2n^3x^m x^{(3n)}e^m \\
& + 6696B^2a^2b^2c^2d^2m^2n^3x^m x^{(3n)}e^m + 6696A^2ab^2c^2d^2m^2n^3x^m x^{(3n)}e^m + 1116B^2a^3d^2m^2n^3x^m x^{(3n)}e^m + 3348A^2a^2bd^2m^2n^3x^m x^{(3n)}e^m \\
& + 1524B^2ab^2c^2n^4x^m x^{(3n)}e^m + 508A^2b^3c^2n^4x^m x^{(3n)}e^m + 3048B^2a^2b^2c^2d^2n^4x^m x^{(3n)}e^m + 3048A^2ab^2c^2d^2n^4x^m x^{(3n)}e^m \\
& + 508B^2a^3d^2n^4x^m x^{(3n)}e^m + 1524A^2a^2bd^2n^4x^m x^{(3n)}e^m + 45B^2a^2b^2c^2m^4x^m x^{(2n)}e^m + 45A^2ab^2c^2m^4x^m x^{(2n)}e^m \\
& + 30B^2a^3c^2d^2m^4x^m x^{(2n)}e^m + 90A^2a^2b^2c^2d^2m^4x^m x^{(2n)}e^m + 15A^2a^3d^2m^4x^m x^{(2n)}e^m + 570B^2a^2b^2c^2m^3n^3x^m x^{(2n)}e^m \\
& + 570A^2ab^2c^2m^3n^3x^m x^{(2n)}e^m + 380B^2a^3c^2d^2m^3n^3x^m x^{(2n)}e^m + 1140A^2a^2b^2c^2d^2m^3n^3x^m x^{(2n)}e^m + 190A^2a^3d^2m^3n^3x^m x^{(2n)}e^m \\
& + 2466B^2a^2b^2c^2m^2n^2x^m x^{(2n)}e^m + 2466A^2ab^2c^2m^2n^2x^m x^{(2n)}e^m + 1644B^2a^3c^2d^2m^2n^2x^m x^{(2n)}e^m + 4932A^2a^2b^2c^2d^2m^2n^2x^m x^{(2n)}e^m \\
& + 822A^2a^3d^2m^2n^2x^m x^{(2n)}e^m + 4149B^2a^2b^2c^2m^2n^3x^m x^{(2n)}e^m + 4149A^2ab^2c^2m^2n^3x^m x^{(2n)}e^m + 2766B^2a^3c^2d^2m^2n^3x^m x^{(2n)}e^m \\
& + 8298A^2a^2b^2c^2d^2m^2n^3x^m x^{(2n)}e^m + 1383A^2a^3d^2m^2n^3x^m x^{(2n)}e^m + 2106B^2a^2b^2c^2n^4x^m x^{(2n)}e^m + 2106A^2ab^2c^2n^4x^m x^{(2n)}e^m \\
& + 1404B^2a^3c^2d^2n^4x^m x^{(2n)}e^m + 4212A^2a^2b^2c^2d^2n^4x^m x^{(2n)}e^m + 702A^2a^3d^2n^4x^m x^{(2n)}e^m + 15B^2a^3c^2m^4x^m x^{(n)}e^m \\
& + 45A^2a^2b^2c^2m^4x^m x^{(n)}e^m + 30A^2a^3c^2d^2m^4x^m x^{(n)}e^m + 200B^2a^3c^2m^3n^3x^m x^{(n)}e^m + 600A^2a^2b^2c^2m^3n^3x^m x^{(n)}e^m \\
& + 400A^2a^3c^2d^2m^3n^3x^m x^{(n)}e^m + 930B^2a^3c^2m^2n^2x^m x^{(n)}e^m + 2790A^2a^2b^2c^2m^2n^2x^m x^{(n)}e^m + 1860A^2a^3c^2d^2m^2n^2x^m x^{(n)}e^m \\
& + 1740B^2a^3c^2m^2n^3x^m x^{(n)}e^m + 5220A^2a^2b^2c^2m^2n^3x^m x^{(n)}e^m + 3480A^2a^3c^2d^2m^2n^3x^m x^{(n)}e^m + 1044B^2a^3c^2n^4x^m x^{(n)}e^m \\
& + 3132A^2a^2b^2c^2n^4x^m x^{(n)}e^m + 2088A^2a^3c^2d^2n^4x^m x^{(n)}e^m + 15A^2a^3c^2m^4x^m x^{(n)}e^m + 210A^2a^3c^2m^3n^3x^m x^{(n)}e^m \\
& + 1050A^2a^3c^2m^2n^2x^m x^{(n)}e^m + 2205A^2a^3c^2m^2n^3x^m x^{(n)}e^m + 1624A^2a^3c^2n^4x^m x^{(n)}e^m + 20B^2b^3d^2m^3x^m x^{(6n)}e^m \\
& + 150B^2b^3d^2m^2n^3x^m x^{(6n)}e^m + 340B^2b^3d^2m^2n^2x^m x^{(6n)}e^m + 225B^2b^3d^2n^3x^m x^{(6n)}e^m + 40B^2b^3c^2d^2m^3x^m x^{(5n)}e^m \\
& + 60B^2ab^2d^2m^3x^m x^{(5n)}e^m + 20A^2b^3d^2m^3x^m x^{(5n)}e^m + 320B^2b^3c^2d^2m^2n^3x^m x^{(5n)}e^m + 480B^2ab^2d^2m^2n^3x^m x^{(5n)}e^m \\
& + 160A^2b^3d^2m^2n^3x^m x^{(5n)}e^m + 760B^2b^3c^2d^2m^2n^2x^m x^{(5n)}e^m + 1140B^2ab^2d^2m^2n^2x^m x^{(5n)}e^m + 380A^2b^3d^2m^2n^2x^m x^{(5n)}e^m \\
& + 520B^2b^3c^2d^2n^3x^m x^{(5n)}e^m + 780B^2ab^2d^2n^3x^m x^{(5n)}e^m + 260A^2b^3d^2n^3x^m x^{(5n)}e^m + 20B^2b^3c^2m^3x^m x^{(4n)}e^m \\
& + 120B^2ab^2c^2d^2m^3x^m x^{(4n)}e^m + 40A^2b^3c^2d^2m^3x^m x^{(4n)}e^m + 60B^2a^2bd^2m^3x^m x^{(4n)}e^m + 60A^2ab^2d^2m^3x^m x^{(4n)}e^m \\
& + 170B^2b^3c^2m^2n^3x^m x^{(4n)}e^m + 1020B^2ab^2c^2d^2m^2n^3x^m x^{(4n)}e^m + 340A^2b^3c^2d^2m^2n^3x^m x^{(4n)}e^m + 510B^2a^2bd^2m^2n^3x^m x^{(4n)}e^m \\
& + 510A^2ab^2d^2m^2n^3x^m x^{(4n)}e^m + 428B^2b^3c^2m^2n^2x^m x^{(4n)}e^m + 2568B^2ab^2c^2d^2m^2n^2x^m x^{(4n)}e^m + 856A^2b^3c^2d^2m^2n^2x^m x^{(4n)}e^m +
\end{aligned}$$

$$\begin{aligned}
& 1284*B*a^2*b*d^2*m*n^2*x*x^m*x^{(4*n)}*e^m + 1284*A*a*b^2*d^2*m*n^2*x*x^m*x^{(4*n)}*e^m + 307*B*b^3*c^2*n^3*x*x^m*x^{(4*n)}*e^m + 1842*B*a*b^2*c*d*n^3*x*x^m*x^{(4*n)}*e^m + 614*A*b^3*c*d*n^3*x*x^m*x^{(4*n)}*e^m + 921*B*a^2*b*d^2*n^3*x*x^m*x^{(4*n)}*e^m + 921*A*a*b^2*d^2*n^3*x*x^m*x^{(4*n)}*e^m + 60*B*a*b^2*c^2*m^3*x*x^m*x^{(3*n)}*e^m + 20*A*b^3*c^2*m^3*x*x^m*x^{(3*n)}*e^m + 120*B*a^2*b*c*d*m^3*x*x^m*x^{(3*n)}*e^m + 120*A*a*b^2*c*d*m^3*x*x^m*x^{(3*n)}*e^m + 20*B*a^3*d^2*m^3*x*x^m*x^{(3*n)}*e^m + 60*A*a^2*b*d^2*m^3*x*x^m*x^{(3*n)}*e^m + 540*B*a*b^2*c^2*m^2*n*x*x^m*x^{(3*n)}*e^m + 180*A*b^3*c^2*m^2*n*x*x^m*x^{(3*n)}*e^m + 1080*B*a^2*b*c*d*m^2*n*x*x^m*x^{(3*n)}*e^m + 1080*A*a*b^2*c*d*m^2*n*x*x^m*x^{(3*n)}*e^m + 180*B*a^3*d^2*m^2*n*x*x^m*x^{(3*n)}*e^m + 540*A*a^2*b*d^2*m^2*n*x*x^m*x^{(3*n)}*e^m + 1452*B*a*b^2*c^2*m*n^2*x*x^m*x^{(3*n)}*e^m + 484*A*b^3*c^2*m*n^2*x*x^m*x^{(3*n)}*e^m + 2904*B*a^2*b*c*d*m*n^2*x*x^m*x^{(3*n)}*e^m + 2904*A*a*b^2*c*d*m*n^2*x*x^m*x^{(3*n)}*e^m + 484*B*a^3*d^2*m*n^2*x*x^m*x^{(3*n)}*e^m + 1452*A*a^2*b*d^2*m*n^2*x*x^m*x^{(3*n)}*e^m + 1116*B*a*b^2*c^2*n^3*x*x^m*x^{(3*n)}*e^m + 372*A*b^3*c^2*n^3*x*x^m*x^{(3*n)}*e^m + 2232*B*a^2*b*c*d*n^3*x*x^m*x^{(3*n)}*e^m + 2232*A*a*b^2*c*d*n^3*x*x^m*x^{(3*n)}*e^m + 372*B*a^3*d^2*n^3*x*x^m*x^{(3*n)}*e^m + 1116*A*a^2*b*d^2*n^3*x*x^m*x^{(3*n)}*e^m + 60*B*a^2*b*c^2*m^3*x*x^m*x^{(2*n)}*e^m + 60*A*a*b^2*c^2*m^3*x*x^m*x^{(2*n)}*e^m + 40*B*a^3*c*d*m^3*x*x^m*x^{(2*n)}*e^m + 120*A*a^2*b*c*d*m^3*x*x^m*x^{(2*n)}*e^m + 20*A*a^3*d^2*m^3*x*x^m*x^{(2*n)}*e^m + 570*B*a^2*b*c^2*m^2*n*x*x^m*x^{(2*n)}*e^m + 570*A*a*b^2*c^2*m^2*n*x*x^m*x^{(2*n)}*e^m + 380*B*a^3*c*d*m^2*n*x*x^m*x^{(2*n)}*e^m + 1140*A*a^2*b*c*d*m^2*n*x*x^m*x^{(2*n)}*e^m + 190*A*a^3*d^2*m^2*n*x*x^m*x^{(2*n)}*e^m + 1644*B*a^2*b*c^2*m*n^2*x*x^m*x^{(2*n)}*e^m + 1644*A*a*b^2*c^2*m*n^2*x*x^m*x^{(2*n)}*e^m + 1096*B*a^3*c*d*m*n^2*x*x^m*x^{(2*n)}*e^m + 3288*A*a^2*b*c*d*m*n^2*x*x^m*x^{(2*n)}*e^m + 548*A*a^3*d^2*m*n^2*x*x^m*x^{(2*n)}*e^m + 1383*B*a^2*b*c^2*n^3*x*x^m*x^{(2*n)}*e^m + 1383*A*a*b^2*c^2*n^3*x*x^m*x^{(2*n)}*e^m + 922*B*a^3*c*d*n^3*x*x^m*x^{(2*n)}*e^m + 2766*A*a^2*b*c*d*n^3*x*x^m*x^{(2*n)}*e^m + 461*A*a^3*d^2*n^3*x*x^m*x^{(2*n)}*e^m + 20*B*a^3*c^2*m^3*x*x^m*x^n*e^m + 60*A*a^2*b*c^2*m^3*x*x^m*x^n*e^m + 40*A*a^3*c*d*m^3*x*x^m*x^n*e^m + 200*B*a^3*c^2*m^2*n*x*x^m*x^n*e^m + 600*A*a^2*b*c^2*m^2*n*x*x^m*x^n*e^m + 400*A*a^3*c*d*m^2*n*x*x^m*x^n*e^m + 620*B*a^3*c^2*m*n^2*x*x^m*x^n*e^m + 1860*A*a^2*b*c^2*m*n^2*x*x^m*x^n*e^m + 1240*A*a^3*c*d*m*n^2*x*x^m*x^n*e^m + 580*B*a^3*c^2*n^3*x*x^m*x^n*e^m + 1740*A*a^2*b*c^2*n^3*x*x^m*x^n*e^m + 1160*A*a^3*c*d*n^3*x*x^m*x^n*e^m + 20*A*a^3*c^2*m^3*x*x^m*e^m + 210*A*a^3*c^2*m^2*n*x*x^m*e^m + 700*A*a^3*c^2*m*n^2*x*x^m*e^m + 735*A*a^3*c^2*n^3*x*x^m*e^m + 15*B*b^3*d^2*m^2*x*x^m*x^{(6*n)}*e^m + 75*B*b^3*d^2*m*n*x*x^m*x^{(6*n)}*e^m + 85*B*b^3*d^2*n^2*x*x^m*x^{(6*n)}*e^m + 30*B*b^3*c*d*m^2*x*x^m*x^{(5*n)}*e^m + 45*B*a*b^2*d^2*m^2*x*x^m*x^{(5*n)}*e^m + 15*A*b^3*d^2*m^2*x*x^m*x^{(5*n)}*e^m + 160*B*b^3*c*d*m*n*x*x^m*x^{(5*n)}*e^m + 240*B*a*b^2*d^2*m*n*x*x^m*x^{(5*n)}*e^m + 80*A*b^3*d^2*m*n*x*x^m*x^{(5*n)}*e^m + 190*B*b^3*c*d*n^2*x*x^m*x^{(5*n)}*e^m + 285*B*a*b^2*d^2*n^2*x*x^m*x^{(5*n)}*e^m + 95*A*b^3*d^2*n^2*x*x^m*x^{(5*n)}*e^m + 15*B*b^3*c^2*m^2*x*x^m*x^{(4*n)}*e^m + 90*B*a*b^2*c*d*m^2*x*x^m*x^{(4*n)}*e^m + 30*A*b^3*c*d*m^2*x*x^m*x^{(4*n)}*e^m + 45*B*a^2*b*d^2*m^2*x*x^m*x^{(4*n)}*e^m + 45*A*a*b^2*d^2*m^2*x*x^m*x^{(4*n)}*e^m + 85*B*b^3*c^2*m*n*x*x^m*x^{(4*n)}*e^m + 510*B*a*b^2*c*d*m*n*x*x^m*x^{(4*n)}*e^m + 170*A*b^3*c*d*m*n*x*x^m*x^{(4*n)}*e^m + 255*B*a^2*b*d^2*m*n*x*x^m*x^{(4*n)}*e^m + 255*A*a*b^2*d^2*m*n*x*x^m*x^{(4*n)}*e^m + 107*B*b^3*c^2*n^2*x*x^m*x^{(4*n)}*e^m + 642*B*a*b^2*c*d*n^2*x*x^m*x^{(4*n)}*e^m + 214*A*b^3*c*d*n^2*x*x^m*x^{(4*n)}*e^m + 321*B*a^2*b*d^2*n^2*x*x^m*x^{(4*n)}*e^m + 321*A*a*b^2*d^2*n^2*x*x^m*x^{(4*n)}*e^m + 45*B*a*b^2*c^2*m^2*x*x^m*x^{(3*n)}*e^m + 15*A*b^3*c^2*m^2*x*x^m*x^{(3*n)}*e^m + 90*B*a^2*b*c*d*m^2*x*x^m*x^{(3*n)}*e^m + 90*A*a*b^2*c*d*m^2*x*x^m*x^{(3*n)}*e^m + 15*B*a^3*d^2*m^2*x*x^m*x^{(3*n)}*e^m + 45*A*a^2*b*d^2*m^2*x*x^m*x^{(3*n)}*e^m + 270*B*a*b^2*c^2*m*n*x*x^m*x^{(3*n)}*e^m + 90*A*b^3*c^2*m*n*x*x^m*x^{(3*n)}*e^m + 540*B*a^2*b*c*d*m*n*x*x^m*x^{(3*n)}*e^m + 540*A*a*b^2*c*d*m*n*x*x^m*x^{(3*n)}*e^m + 90*B*a^3*d^2*m*n*x*x^m*x^{(3*n)}*e^m + 270*A*a^2*b*d^2*m*n*x*x^m*x^{(3*n)}*e^m + 363*B*a*b^2*c^2*n^2*x*x^m*x^{(3*n)}*e^m + 121*A*b^3*c^2*n^2*x*x^m*x^{(3*n)}*e^m + 726*B*a^2*b*c*d*n^2*x*x^m*x^{(3*n)}*e^m + 726*A*a*b^2*c*d*n^2*x*x^m*x^{(3*n)}*e^m + 121*B*a^3*d^2*n^2*x*x^m*x^{(3*n)}*e^m + 363*A*a^2*b*d^2*n^2*x*x^m*x^{(3*n)}*e^m + 45*B*a^2*b*c^2*m^2*x*x^m*x^{(2*n)}*e^m + 45*A*a*b^2*c^2*m^2*x*x^m*x^{(2*n)}*e^m
\end{aligned}$$

$$\begin{aligned}
& *e^m + 30*B*a^3*c*d*m^2*x*x^m*x^{(2*n)}*e^m + 90*A*a^2*b*c*d*m^2*x*x^m*x^{(2*n)} \\
& )*e^m + 15*A*a^3*d^2*m^2*x*x^m*x^{(2*n)}*e^m + 285*B*a^2*b*c^2*m*n*x*x^m*x^{(2 \\
& *n)}*e^m + 285*A*a*b^2*c^2*m*n*x*x^m*x^{(2*n)}*e^m + 190*B*a^3*c*d*m*n*x*x^m*x \\
& ^{(2*n)}*e^m + 570*A*a^2*b*c*d*m*n*x*x^m*x^{(2*n)}*e^m + 95*A*a^3*d^2*m*n*x*x^m \\
& *x^{(2*n)}*e^m + 411*B*a^2*b*c^2*n^2*x*x^m*x^{(2*n)}*e^m + 411*A*a*b^2*c^2*n^2* \\
& x*x^m*x^{(2*n)}*e^m + 274*B*a^3*c*d*n^2*x*x^m*x^{(2*n)}*e^m + 822*A*a^2*b*c*d*n \\
& ^2*x*x^m*x^{(2*n)}*e^m + 137*A*a^3*d^2*n^2*x*x^m*x^{(2*n)}*e^m + 15*B*a^3*c^2*m \\
& ^2*x*x^m*x^n*e^m + 45*A*a^2*b*c^2*m^2*x*x^m*x^n*e^m + 30*A*a^3*c*d*m^2*x*x^ \\
& m*x^n*e^m + 100*B*a^3*c^2*m*n*x*x^m*x^n*e^m + 300*A*a^2*b*c^2*m*n*x*x^m*x^n \\
& *e^m + 200*A*a^3*c*d*m*n*x*x^m*x^n*e^m + 155*B*a^3*c^2*n^2*x*x^m*x^n*e^m + \\
& 465*A*a^2*b*c^2*n^2*x*x^m*x^n*e^m + 310*A*a^3*c*d*n^2*x*x^m*x^n*e^m + 15*A* \\
& a^3*c^2*m^2*x*x^m*e^m + 105*A*a^3*c^2*m*n*x*x^m*e^m + 175*A*a^3*c^2*n^2*x*x \\
& ^m*e^m + 6*B*b^3*d^2*m*x*x^m*x^{(6*n)}*e^m + 15*B*b^3*d^2*n*x*x^m*x^{(6*n)}*e^m \\
& + 12*B*b^3*c*d*m*x*x^m*x^{(5*n)}*e^m + 18*B*a*b^2*d^2*m*x*x^m*x^{(5*n)}*e^m + \\
& 6*A*b^3*d^2*m*x*x^m*x^{(5*n)}*e^m + 32*B*b^3*c*d*n*x*x^m*x^{(5*n)}*e^m + 48*B*a \\
& *b^2*d^2*n*x*x^m*x^{(5*n)}*e^m + 16*A*b^3*d^2*n*x*x^m*x^{(5*n)}*e^m + 6*B*b^3*c \\
& ^2*m*x*x^m*x^{(4*n)}*e^m + 36*B*a*b^2*c*d*m*x*x^m*x^{(4*n)}*e^m + 12*A*b^3*c*d* \\
& m*x*x^m*x^{(4*n)}*e^m + 18*B*a^2*b*d^2*m*x*x^m*x^{(4*n)}*e^m + 18*A*a*b^2*d^2*m \\
& *x*x^m*x^{(4*n)}*e^m + 17*B*b^3*c^2*n*x*x^m*x^{(4*n)}*e^m + 102*B*a*b^2*c*d*n*x \\
& *x^m*x^{(4*n)}*e^m + 34*A*b^3*c*d*n*x*x^m*x^{(4*n)}*e^m + 51*B*a^2*b*d^2*n*x*x^ \\
& m*x^{(4*n)}*e^m + 51*A*a*b^2*d^2*n*x*x^m*x^{(4*n)}*e^m + 18*B*a*b^2*c^2*m*x*x^m \\
& *x^{(3*n)}*e^m + 6*A*b^3*c^2*m*x*x^m*x^{(3*n)}*e^m + 36*B*a^2*b*c*d*m*x*x^m*x^{( \\
& 3*n)}*e^m + 36*A*a*b^2*c*d*m*x*x^m*x^{(3*n)}*e^m + 6*B*a^3*d^2*m*x*x^m*x^{(3*n)} \\
& *e^m + 18*A*a^2*b*d^2*m*x*x^m*x^{(3*n)}*e^m + 54*B*a*b^2*c^2*n*x*x^m*x^{(3*n)}* \\
& e^m + 18*A*b^3*c^2*n*x*x^m*x^{(3*n)}*e^m + 108*B*a^2*b*c*d*n*x*x^m*x^{(3*n)}*e^ \\
& m + 108*A*a*b^2*c*d*n*x*x^m*x^{(3*n)}*e^m + 18*B*a^3*d^2*n*x*x^m*x^{(3*n)}*e^m \\
& + 54*A*a^2*b*d^2*n*x*x^m*x^{(3*n)}*e^m + 18*B*a^2*b*c^2*m*x*x^m*x^{(2*n)}*e^m + \\
& 18*A*a*b^2*c^2*m*x*x^m*x^{(2*n)}*e^m + 12*B*a^3*c*d*m*x*x^m*x^{(2*n)}*e^m + 36 \\
& *A*a^2*b*c*d*m*x*x^m*x^{(2*n)}*e^m + 6*A*a^3*d^2*m*x*x^m*x^{(2*n)}*e^m + 57*B*a \\
& ^2*b*c^2*n*x*x^m*x^{(2*n)}*e^m + 57*A*a*b^2*c^2*n*x*x^m*x^{(2*n)}*e^m + 38*B*a^ \\
& 3*c*d*n*x*x^m*x^{(2*n)}*e^m + 114*A*a^2*b*c*d*n*x*x^m*x^{(2*n)}*e^m + 19*A*a^3* \\
& d^2*n*x*x^m*x^{(2*n)}*e^m + 6*B*a^3*c^2*m*x*x^m*x^n*e^m + 18*A*a^2*b*c^2*m*x* \\
& x^m*x^n*e^m + 12*A*a^3*c*d*m*x*x^m*x^n*e^m + 20*B*a^3*c^2*n*x*x^m*x^n*e^m + \\
& 60*A*a^2*b*c^2*n*x*x^m*x^n*e^m + 40*A*a^3*c*d*n*x*x^m*x^n*e^m + 6*A*a^3*c^ \\
& 2*m*x*x^m*e^m + 21*A*a^3*c^2*n*x*x^m*e^m + B*b^3*d^2*x*x^m*x^{(6*n)}*e^m + 2* \\
& B*b^3*c*d*x*x^m*x^{(5*n)}*e^m + 3*B*a*b^2*d^2*x*x^m*x^{(5*n)}*e^m + A*b^3*d^2*x \\
& *x^m*x^{(5*n)}*e^m + B*b^3*c^2*x*x^m*x^{(4*n)}*e^m + 6*B*a*b^2*c*d*x*x^m*x^{(4*n)} \\
& )*e^m + 2*A*b^3*c*d*x*x^m*x^{(4*n)}*e^m + 3*B*a^2*b*d^2*x*x^m*x^{(4*n)}*e^m + 3 \\
& *A*a*b^2*d^2*x*x^m*x^{(4*n)}*e^m + 3*B*a*b^2*c^2*x*x^m*x^{(3*n)}*e^m + A*b^3*c^ \\
& 2*x*x^m*x^{(3*n)}*e^m + 6*B*a^2*b*c*d*x*x^m*x^{(3*n)}*e^m + 6*A*a*b^2*c*d*x*x^m \\
& *x^{(3*n)}*e^m + B*a^3*d^2*x*x^m*x^{(3*n)}*e^m + 3*A*a^2*b*d^2*x*x^m*x^{(3*n)}*e^ \\
& m + 3*B*a^2*b*c^2*x*x^m*x^{(2*n)}*e^m + 3*A*a*b^2*c^2*x*x^m*x^{(2*n)}*e^m + 2*B \\
& *a^3*c*d*x*x^m*x^{(2*n)}*e^m + 6*A*a^2*b*c*d*x*x^m*x^{(2*n)}*e^m + A*a^3*d^2*x* \\
& x^m*x^{(2*n)}*e^m + B*a^3*c^2*x*x^m*x^n*e^m + 3*A*a^2*b*c^2*x*x^m*x^n*e^m + 2 \\
& *A*a^3*c*d*x*x^m*x^n*e^m + A*a^3*c^2*x*x^m*e^m)/(m^7 + 21*m^6*n + 175*m^5*n \\
& ^2 + 735*m^4*n^3 + 1624*m^3*n^4 + 1764*m^2*n^5 + 720*m*n^6 + 7*m^6 + 126*m^ \\
& 5*n + 875*m^4*n^2 + 2940*m^3*n^3 + 4872*m^2*n^4 + 3528*m*n^5 + 720*n^6 + 21 \\
& *m^5 + 315*m^4*n + 1750*m^3*n^2 + 4410*m^2*n^3 + 4872*m*n^4 + 1764*n^5 + 35 \\
& *m^4 + 420*m^3*n + 1750*m^2*n^2 + 2940*m*n^3 + 1624*n^4 + 35*m^3 + 315*m^2* \\
& n + 875*m*n^2 + 735*n^3 + 21*m^2 + 126*m*n + 175*n^2 + 7*m + 21*n + 1)
\end{aligned}$$

**maple [C]** time = 0.23, size = 11389, normalized size = 35.81

output too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((e*x)^m*(b*x^n+a)^3*(B*x^n+A)*(d*x^n+c)^2,x)`

[Out] result too large to display

**maxima [B]** time = 1.12, size = 748, normalized size = 2.35

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="maxima")

[Out]  $B*b^3*d^2*e^{m*x}*e^{(m*\log(x) + 6*n*\log(x))/(m + 6*n + 1)} + 2*B*b^3*c*d*e^{m*x}*e^{(m*\log(x) + 5*n*\log(x))/(m + 5*n + 1)} + 3*B*a*b^2*d^2*e^{m*x}*e^{(m*\log(x) + 5*n*\log(x))/(m + 5*n + 1)} + A*b^3*d^2*e^{m*x}*e^{(m*\log(x) + 5*n*\log(x))/(m + 5*n + 1)} + B*b^3*c^2*e^{m*x}*e^{(m*\log(x) + 4*n*\log(x))/(m + 4*n + 1)} + 6*B*a*b^2*c*d*e^{m*x}*e^{(m*\log(x) + 4*n*\log(x))/(m + 4*n + 1)} + 2*A*b^3*c*d*e^{m*x}*e^{(m*\log(x) + 4*n*\log(x))/(m + 4*n + 1)} + 3*B*a^2*b*d^2*e^{m*x}*e^{(m*\log(x) + 4*n*\log(x))/(m + 4*n + 1)} + 3*A*a*b^2*d^2*e^{m*x}*e^{(m*\log(x) + 4*n*\log(x))/(m + 4*n + 1)} + 3*B*a*b^2*c^2*e^{m*x}*e^{(m*\log(x) + 3*n*\log(x))/(m + 3*n + 1)} + A*b^3*c^2*e^{m*x}*e^{(m*\log(x) + 3*n*\log(x))/(m + 3*n + 1)} + 6*B*a^2*b*c*d*e^{m*x}*e^{(m*\log(x) + 3*n*\log(x))/(m + 3*n + 1)} + 6*A*a*b^2*c*d*e^{m*x}*e^{(m*\log(x) + 3*n*\log(x))/(m + 3*n + 1)} + B*a^3*d^2*e^{m*x}*e^{(m*\log(x) + 3*n*\log(x))/(m + 3*n + 1)} + 3*A*a^2*b*d^2*e^{m*x}*e^{(m*\log(x) + 3*n*\log(x))/(m + 3*n + 1)} + 3*B*a^2*b*c^2*e^{m*x}*e^{(m*\log(x) + 2*n*\log(x))/(m + 2*n + 1)} + 3*A*a*b^2*c^2*e^{m*x}*e^{(m*\log(x) + 2*n*\log(x))/(m + 2*n + 1)} + 2*B*a^3*c*d*e^{m*x}*e^{(m*\log(x) + 2*n*\log(x))/(m + 2*n + 1)} + 6*A*a^2*b*c*d*e^{m*x}*e^{(m*\log(x) + 2*n*\log(x))/(m + 2*n + 1)} + A*a^3*d^2*e^{m*x}*e^{(m*\log(x) + 2*n*\log(x))/(m + 2*n + 1)} + B*a^3*c^2*e^{m*x}*e^{(m*\log(x) + n*\log(x))/(m + n + 1)} + 3*A*a^2*b*c^2*e^{m*x}*e^{(m*\log(x) + n*\log(x))/(m + n + 1)} + 2*A*a^3*c*d*e^{m*x}*e^{(m*\log(x) + n*\log(x))/(m + n + 1)} + (e*x)^{(m + 1)}*A*a^3*c^2/(e*(m + 1))$

**mupad [B]** time = 6.35, size = 1882, normalized size = 5.92

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^3\*(c + d\*x^n)^2,x)

[Out]  $(x*x^{(3*n)}*(e*x)^m*(A*b^3*c^2 + B*a^3*d^2 + 3*A*a^2*b*d^2 + 3*B*a*b^2*c^2 + 6*A*a*b^2*c*d + 6*B*a^2*b*c*d)*(5*m + 18*n + 72*m*n + 363*m*n^2 + 108*m^2*n + 744*m*n^3 + 72*m^3*n + 508*m*n^4 + 18*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 121*n^2 + 372*n^3 + 508*n^4 + 240*n^5 + 363*m^2*n^2 + 372*m^2*n^3 + 121*m^3*n^2 + 1))/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (A*a^3*c^2*x*(e*x)^m)/(m + 1) + (a*x*x^{(2*n)}*(e*x)^m*(A*a^2*d^2 + 3*A*b^2*c^2 + 3*B*a*b*c^2 + 2*B*a^2*c*d + 6*A*a*b*c*d)*(5*m + 19*n + 76*m*n + 411*m*n^2 + 114*m^2*n + 922*m*n^3 + 76*m^3*n + 702*m*n^4 + 19*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 137*n^2 + 461*n^3 + 702*n^4 + 360*n^5 + 411*m^2*n^2 + 461*m^2*n^3 + 137*m^3*n^2 + 1))/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (b*x*x^{(4*n)}*(e*x)^m*(3*B*a^2*d^2 + B*b^2*c^2 + 3*A*a*b*d^2 + 2*A*b^2*c*d + 6*B*a*b*c*d)*(5*m + 17*n + 68*m*n + 321*m*n^2 + 102*m^2*n + 614*m*n^3 + 68*m^3*n + 396*m*n^4 + 17*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 107*n^2 + 307*n^3 + 396*n^4 + 180*n^5 + 321*m^2*n^2 + 307*m^2*n^3 + 107*m^3*n^2 + 1))/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (a^2*c*x*x^n*(e*x)^m*(2*A*a*d + 3*A*b*c + B*a*c)*(5*m + 20*n + 80*m*n + 465*m*n$

$$\begin{aligned} &^2 + 120*m^2*n + 1160*m*n^3 + 80*m^3*n + 1044*m*n^4 + 20*m^4*n + 10*m^2 + 1 \\ &0*m^3 + 5*m^4 + m^5 + 155*n^2 + 580*n^3 + 1044*n^4 + 720*n^5 + 465*m^2*n^2 \\ &+ 580*m^2*n^3 + 155*m^3*n^2 + 1) / (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m \\ &^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^ \\ &5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 \\ &+ 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^ \\ &2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (b^2*d*x*x^(5*n))*(e*x)^m*(A*b*d + \\ &3*B*a*d + 2*B*b*c)*(5*m + 16*n + 64*m*n + 285*m*n^2 + 96*m^2*n + 520*m*n^3 \\ &+ 64*m^3*n + 324*m*n^4 + 16*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 95*n^2 \\ &+ 260*n^3 + 324*n^4 + 144*n^5 + 285*m^2*n^2 + 260*m^2*n^3 + 95*m^3*n^2 + 1) \\ &)/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + \\ &3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + \\ &6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2 \\ &*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^ \\ &2 + 1) + (B*b^3*d^2*x*x^(6*n))*(e*x)^m*(5*m + 15*n + 60*m*n + 255*m*n^2 + 90 \\ &*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5* \\ &m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^ \\ &3 + 85*m^3*n^2 + 1) / (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m \\ &*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 \\ &+ 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + \\ &720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m \\ &^3*n^3 + 175*m^4*n^2 + 1) \end{aligned}$$

**sympy** [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*3\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*2,x)

[Out] Timed out



### 3.6 $\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^2 dx$

**Optimal.** Leaf size=237

$$\frac{x^{2n+1}(ex)^m \left( A(a^2d^2 + 4abcd + b^2c^2) + 2aBc(ad + bc) \right)}{m + 2n + 1} + \frac{x^{3n+1}(ex)^m \left( a^2Bd^2 + 2abd(Ad + 2Bc) + b^2c(2Ad + Bc) \right)}{m + 3n + 1}$$

**Rubi [A]** time = 0.31, antiderivative size = 237, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {570, 20, 30}

$$\frac{x^{2n+1}(ex)^m \left( A(a^2d^2 + 4abcd + b^2c^2) + 2aBc(ad + bc) \right)}{m + 2n + 1} + \frac{x^{3n+1}(ex)^m \left( a^2Bd^2 + 2abd(Ad + 2Bc) + b^2c(2Ad + Bc) \right)}{m + 3n + 1} + \frac{a^2Ac^2(ex)^{m+1}}{c(m+1)} + \frac{acx^{n+1}(ex)^m(2A(ad + bc) + aBc)}{m + n + 1} + \frac{bdx^{4n+1}(ex)^m(2aBd + Abd + 2bBc)}{m + 4n + 1} + \frac{b^2Bd^2x^{5n+1}(ex)^m}{m + 5n + 1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] (a\*c\*(a\*B\*c + 2\*A\*(b\*c + a\*d))\*x^(1 + n)\*(e\*x)^m/(1 + m + n) + ((2\*a\*B\*c\*(b\*c + a\*d) + A\*(b^2\*c^2 + 4\*a\*b\*c\*d + a^2\*d^2))\*x^(1 + 2\*n)\*(e\*x)^m/(1 + m + 2\*n) + ((a^2\*B\*d^2 + 2\*a\*b\*d\*(2\*B\*c + A\*d) + b^2\*c\*(B\*c + 2\*A\*d))\*x^(1 + 3\*n)\*(e\*x)^m/(1 + m + 3\*n) + (b\*d\*(2\*b\*B\*c + A\*b\*d + 2\*a\*B\*d))\*x^(1 + 4\*n)\*(e\*x)^m/(1 + m + 4\*n) + (b^2\*B\*d^2\*x^(1 + 5\*n)\*(e\*x)^m)/(1 + m + 5\*n) + (a^2\*A\*c^2\*(e\*x)^(1 + m))/(e\*(1 + m))

#### Rule 20

Int[(u\_)\*((a\_)\*(v\_))^(m\_)\*((b\_)\*(v\_))^(n\_), x\_Symbol] := Dist[(b^IntPart[n]\*((a\*v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m + n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

#### Rule 30

Int[(x\_)^(m\_), x\_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

#### Rule 570

Int[((g\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_)\*((e\_) + (f\_)\*(x\_)^(n\_))^(r\_), x\_Symbol] := Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

#### Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^2 dx &= \int \left( a^2Ac^2(ex)^m + ac(aBc + 2A(bc + ad))x^n(ex)^m + (2aBc(bc + ad) + A(b^2c^2 + 4abcd + b^2d^2))x^{2n}(ex)^m \right) dx \\ &= \frac{a^2Ac^2(ex)^{1+m}}{e(1+m)} + (b^2Bd^2) \int x^{5n}(ex)^m dx + (bd(2bBc + Abd + 2aBd)) \int x^{m+5n} dx \\ &= \frac{a^2Ac^2(ex)^{1+m}}{e(1+m)} + (b^2Bd^2x^{-m}(ex)^m) \int x^{m+5n} dx + (bd(2bBc + Abd + 2aBd)) \int x^{m+5n} dx \\ &= \frac{ac(aBc + 2A(bc + ad))x^{1+n}(ex)^m}{1+m+n} + \frac{(2aBc(bc + ad) + A(b^2c^2 + 4abcd + b^2d^2))x^{m+5n+1}(ex)^m}{1+m} \end{aligned}$$

**Mathematica [A]** time = 0.60, size = 199, normalized size = 0.84

$$x(ex)^m \left( \frac{x^{2n} \left( A(a^2d^2 + 4abcd + b^2c^2) + 2aBc(ad + bc) \right)}{m + 2n + 1} + \frac{x^{3n} \left( a^2Bd^2 + 2abd(Ad + 2Bc) + b^2c(2Ad + Bc) \right)}{m + 3n + 1} + \frac{a^2Ac^2}{m + 1} + \frac{bdx^{4n}(2aBd + Abd + 2bBc)}{m + 4n + 1} + \frac{acx^n(2A(ad + bc) + aBc)}{m + n + 1} + \frac{b^2Bd^2x^{5n}}{m + 5n + 1} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] x\*(e\*x)^m\*((a^2\*A\*c^2)/(1 + m) + (a\*c\*(a\*B\*c + 2\*A\*(b\*c + a\*d))\*x^n)/(1 + m + n) + ((2\*a\*B\*c\*(b\*c + a\*d) + A\*(b^2\*c^2 + 4\*a\*b\*c\*d + a^2\*d^2))\*x^(2\*n))/(1 + m + 2\*n) + ((a^2\*B\*d^2 + 2\*a\*b\*d\*(2\*B\*c + A\*d) + b^2\*c\*(B\*c + 2\*A\*d))\*x^(3\*n))/(1 + m + 3\*n) + (b\*d\*(2\*b\*B\*c + A\*b\*d + 2\*a\*B\*d)\*x^(4\*n))/(1 + m + 4\*n) + (b^2\*B\*d^2\*x^(5\*n))/(1 + m + 5\*n))

IntegrateAlgebraic [F] time = 0.30, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^2 dx$$

Verification is not applicable to the result.

[In] IntegrateAlgebraic[(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] Defer[IntegrateAlgebraic] [(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n)^2, x]

fricas [B] time = 0.51, size = 3515, normalized size = 14.83

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="fricas")

[Out] ((B\*b^2\*d^2\*m^5 + 5\*B\*b^2\*d^2\*m^4 + 10\*B\*b^2\*d^2\*m^3 + 10\*B\*b^2\*d^2\*m^2 + 5\*B\*b^2\*d^2\*m + B\*b^2\*d^2 + 24\*(B\*b^2\*d^2\*m + B\*b^2\*d^2)\*n^4 + 50\*(B\*b^2\*d^2\*m^2 + 2\*B\*b^2\*d^2\*m + B\*b^2\*d^2)\*n^3 + 35\*(B\*b^2\*d^2\*m^3 + 3\*B\*b^2\*d^2\*m^2 + 3\*B\*b^2\*d^2\*m + B\*b^2\*d^2)\*n^2 + 10\*(B\*b^2\*d^2\*m^4 + 4\*B\*b^2\*d^2\*m^3 + 6\*B\*b^2\*d^2\*m^2 + 4\*B\*b^2\*d^2\*m + B\*b^2\*d^2)\*n)\*x\*x^(5\*n)\*e^(m\*log(e) + m\*log(x)) + ((2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m^5 + 2\*B\*b^2\*c\*d + 5\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m^4 + 30\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2 + (2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m)\*n^4 + 10\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m^3 + 61\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2 + (2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m)\*n^2 + 2\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m)\*n^3 + (2\*B\*a\*b + A\*b^2)\*d^2 + 10\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m^2 + 41\*(2\*B\*b^2\*c\*d + (2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m^3 + (2\*B\*a\*b + A\*b^2)\*d^2 + 3\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m^2 + 3\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m)\*n^2 + 5\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m + 11\*(2\*B\*b^2\*c\*d + (2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m^4 + 4\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m^3 + (2\*B\*a\*b + A\*b^2)\*d^2 + 6\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m^2 + 4\*(2\*B\*b^2\*c\*d + (2\*B\*a\*b + A\*b^2)\*d^2)\*m)\*n)\*x\*x^(4\*n)\*e^(m\*log(e) + m\*log(x)) + ((B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m^5 + B\*b^2\*c^2 + 5\*(B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m^4 + 40\*(B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2 + (B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m)\*n^4 + 10\*(B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m^3 + 78\*(B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2 + (B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m)\*n^2 + 2\*(B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m)\*n^3 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2 + 10\*(B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m^2 + 49\*(B\*b^2\*c^2 + (B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m^3 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2 + 3\*(B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m^2 + 3\*(B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m)\*n^2 + 5\*(B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m + 12\*(B\*b^2\*c^2 + (B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B\*a^2 + 2\*A\*a\*b)\*d^2)\*m^4 + 4\*(B\*b^2\*c^2 + 2\*(2\*B\*a\*b + A\*b^2)\*c\*d + (B

$$\begin{aligned}
& a^2 + 2Aab)d^2)m^3 + 2*(2Bab + Ab^2)*cd + (Ba^2 + 2Aab)d^2 + \\
& 6*(Bb^2*c^2 + 2*(2Bab + Ab^2)*cd + (Ba^2 + 2Aab)d^2)m^2 + 4*(B \\
& *b^2*c^2 + 2*(2Bab + Ab^2)*cd + (Ba^2 + 2Aab)d^2)m)*n)*x^{3n} \\
& *e^{(m*\log(e) + m*\log(x))} + ((Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + \\
& 2Aab)*cd)*m^5 + Aa^2*d^2 + 5*(Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*( \\
& Ba^2 + 2Aab)*cd)*m^4 + 60*(Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 \\
& + 2Aab)*cd + (Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab) \\
& *cd)*m)*n^4 + 10*(Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab)* \\
& cd)*m^3 + 107*(Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab)*cd \\
& + (Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab)*cd)*m^2 + 2*(A \\
& a^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab)*cd)*m)*n^3 + (2Bab \\
& + Ab^2)*c^2 + 2*(Ba^2 + 2Aab)*cd + 10*(Aa^2*d^2 + (2Bab + Ab^2) \\
& *c^2 + 2*(Ba^2 + 2Aab)*cd)*m^2 + 59*(Aa^2*d^2 + (Aa^2*d^2 + (2Bab \\
& + Ab^2)*c^2 + 2*(Ba^2 + 2Aab)*cd)*m^3 + (2Bab + Ab^2)*c^2 + 2* \\
& (Ba^2 + 2Aab)*cd + 3*(Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2 \\
& Aab)*cd)*m^2 + 3*(Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab \\
& b)*cd)*m)*n^2 + 5*(Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab) \\
& *cd)*m + 13*(Aa^2*d^2 + (Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2 \\
& Aab)*cd)*m^4 + 4*(Aa^2*d^2 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab \\
& b)*cd)*m^3 + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab)*cd + 6*(Aa^2*d^2 \\
& + (2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab)*cd)*m^2 + 4*(Aa^2*d^2 + ( \\
& 2Bab + Ab^2)*c^2 + 2*(Ba^2 + 2Aab)*cd)*m)*n)*x^{2n}*e^{(m*\log(e) \\
& + m*\log(x))} + ((2Aa^2*c*d + (Ba^2 + 2Aab)*c^2)*m^5 + 2Aa^2*c*d + 5 \\
& *(2Aa^2*c*d + (Ba^2 + 2Aab)*c^2)*m^4 + 120*(2Aa^2*c*d + (Ba^2 + 2* \\
& Aab)*c^2 + (2Aa^2*c*d + (Ba^2 + 2Aab)*c^2)*m)*n^4 + 10*(2Aa^2*c*d \\
& + (Ba^2 + 2Aab)*c^2)*m^3 + 154*(2Aa^2*c*d + (Ba^2 + 2Aab)*c^2 + \\
& (2Aa^2*c*d + (Ba^2 + 2Aab)*c^2)*m^2 + 2*(2Aa^2*c*d + (Ba^2 + 2Aab \\
& *b)*c^2)*m)*n^3 + (Ba^2 + 2Aab)*c^2 + 10*(2Aa^2*c*d + (Ba^2 + 2Aab \\
& b)*c^2)*m^2 + 71*(2Aa^2*c*d + (2Aa^2*c*d + (Ba^2 + 2Aab)*c^2)*m^3 + \\
& (Ba^2 + 2Aab)*c^2 + 3*(2Aa^2*c*d + (Ba^2 + 2Aab)*c^2)*m^2 + 3*(2 \\
& Aa^2*c*d + (Ba^2 + 2Aab)*c^2)*m)*n^2 + 5*(2Aa^2*c*d + (Ba^2 + 2Aab \\
& *b)*c^2)*m + 14*(2Aa^2*c*d + (2Aa^2*c*d + (Ba^2 + 2Aab)*c^2)*m^4 + \\
& 4*(2Aa^2*c*d + (Ba^2 + 2Aab)*c^2)*m^3 + (Ba^2 + 2Aab)*c^2 + 6*(2 \\
& Aa^2*c*d + (Ba^2 + 2Aab)*c^2)*m^2 + 4*(2Aa^2*c*d + (Ba^2 + 2Aab) \\
& )*c^2)*m)*n)*x^n*e^{(m*\log(e) + m*\log(x))} + (Aa^2*c^2*m^5 + 120*Aa^2*c^2 \\
& *n^5 + 5Aa^2*c^2*m^4 + 10Aa^2*c^2*m^3 + 10Aa^2*c^2*m^2 + 5Aa^2*c^2* \\
& m + Aa^2*c^2 + 274*(Aa^2*c^2*m + Aa^2*c^2)*n^4 + 225*(Aa^2*c^2*m^2 + 2* \\
& Aa^2*c^2*m + Aa^2*c^2)*n^3 + 85*(Aa^2*c^2*m^3 + 3Aa^2*c^2*m^2 + 3Aa^2 \\
& *c^2*m + Aa^2*c^2)*n^2 + 15*(Aa^2*c^2*m^4 + 4Aa^2*c^2*m^3 + 6Aa^2*c^2 \\
& *m^2 + 4Aa^2*c^2*m + Aa^2*c^2)*n)*x*e^{(m*\log(e) + m*\log(x))}/(m^6 + 120 \\
& *(m + 1)*n^5 + 6*m^5 + 274*(m^2 + 2*m + 1)*n^4 + 15*m^4 + 225*(m^3 + 3*m^2 \\
& + 3*m + 1)*n^3 + 20*m^3 + 85*(m^4 + 4*m^3 + 6*m^2 + 4*m + 1)*n^2 + 15*m^2 + \\
& 15*(m^5 + 5*m^4 + 10*m^3 + 10*m^2 + 5*m + 1)*n + 6*m + 1)
\end{aligned}$$

**giac** [B] time = 2.01, size = 8103, normalized size = 34.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="giac")

[Out] (B\*b^2\*d^2\*m^5\*x\*x^m\*x^(5\*n)\*e^m + 10\*B\*b^2\*d^2\*m^4\*n\*x\*x^m\*x^(5\*n)\*e^m + 3  
5\*B\*b^2\*d^2\*m^3\*n^2\*x\*x^m\*x^(5\*n)\*e^m + 50\*B\*b^2\*d^2\*m^2\*n^3\*x\*x^m\*x^(5\*n)\*  
e^m + 24\*B\*b^2\*d^2\*m\*n^4\*x\*x^m\*x^(5\*n)\*e^m + 2\*B\*b^2\*c\*d\*m^5\*x\*x^m\*x^(4\*n)\*  
e^m + 2\*B\*a\*b\*d^2\*m^5\*x\*x^m\*x^(4\*n)\*e^m + A\*b^2\*d^2\*m^5\*x\*x^m\*x^(4\*n)\*e^m +  
22\*B\*b^2\*c\*d\*m^4\*n\*x\*x^m\*x^(4\*n)\*e^m + 22\*B\*a\*b\*d^2\*m^4\*n\*x\*x^m\*x^(4\*n)\*e^  
m + 11\*A\*b^2\*d^2\*m^4\*n\*x\*x^m\*x^(4\*n)\*e^m + 82\*B\*b^2\*c\*d\*m^3\*n^2\*x\*x^m\*x^(4\*  
n)\*e^m + 82\*B\*a\*b\*d^2\*m^3\*n^2\*x\*x^m\*x^(4\*n)\*e^m + 41\*A\*b^2\*d^2\*m^3\*n^2\*x\*x^  
m\*x^(4\*n)\*e^m + 122\*B\*b^2\*c\*d\*m^2\*n^3\*x\*x^m\*x^(4\*n)\*e^m + 122\*B\*a\*b\*d^2\*m^2  
\*n^3\*x\*x^m\*x^(4\*n)\*e^m + 61\*A\*b^2\*d^2\*m^2\*n^3\*x\*x^m\*x^(4\*n)\*e^m + 60\*B\*b^2\*

$$\begin{aligned}
& c*d*m^n^4*x*x^m*x^(4*n)*e^m + 60*B*a*b*d^2*m^n^4*x*x^m*x^(4*n)*e^m + 30*A*b^2*d^2*m^n^4*x*x^m*x^(4*n)*e^m + B*b^2*c^2*m^5*x*x^m*x^(3*n)*e^m + 4*B*a*b*c*d*m^5*x*x^m*x^(3*n)*e^m + 2*A*b^2*c*d*m^5*x*x^m*x^(3*n)*e^m + B*a^2*d^2*m^5*x*x^m*x^(3*n)*e^m + 2*A*a*b*d^2*m^5*x*x^m*x^(3*n)*e^m + 12*B*b^2*c^2*m^4*n*x*x^m*x^(3*n)*e^m + 48*B*a*b*c*d*m^4*n*x*x^m*x^(3*n)*e^m + 24*A*b^2*c*d*m^4*n*x*x^m*x^(3*n)*e^m + 12*B*a^2*d^2*m^4*n*x*x^m*x^(3*n)*e^m + 24*A*a*b*d^2*m^4*n*x*x^m*x^(3*n)*e^m + 49*B*b^2*c^2*m^3*n^2*x*x^m*x^(3*n)*e^m + 196*B*a*b*c*d*m^3*n^2*x*x^m*x^(3*n)*e^m + 98*A*b^2*c*d*m^3*n^2*x*x^m*x^(3*n)*e^m + 49*B*a^2*d^2*m^3*n^2*x*x^m*x^(3*n)*e^m + 98*A*a*b*d^2*m^3*n^2*x*x^m*x^(3*n)*e^m + 78*B*b^2*c^2*m^2*n^3*x*x^m*x^(3*n)*e^m + 312*B*a*b*c*d*m^2*n^3*x*x^m*x^(3*n)*e^m + 156*A*b^2*c*d*m^2*n^3*x*x^m*x^(3*n)*e^m + 78*B*a^2*d^2*m^2*n^3*x*x^m*x^(3*n)*e^m + 156*A*a*b*d^2*m^2*n^3*x*x^m*x^(3*n)*e^m + 40*B*b^2*c^2*m^n^4*x*x^m*x^(3*n)*e^m + 160*B*a*b*c*d*m^n^4*x*x^m*x^(3*n)*e^m + 80*A*b^2*c*d*m^n^4*x*x^m*x^(3*n)*e^m + 40*B*a^2*d^2*m^n^4*x*x^m*x^(3*n)*e^m + 80*A*a*b*d^2*m^n^4*x*x^m*x^(3*n)*e^m + 2*B*a*b*c^2*m^5*x*x^m*x^(2*n)*e^m + A*b^2*c^2*m^5*x*x^m*x^(2*n)*e^m + 2*B*a^2*c*d*m^5*x*x^m*x^(2*n)*e^m + 4*A*a*b*c*d*m^5*x*x^m*x^(2*n)*e^m + A*a^2*d^2*m^5*x*x^m*x^(2*n)*e^m + 26*B*a*b*c^2*m^4*n*x*x^m*x^(2*n)*e^m + 13*A*b^2*c^2*m^4*n*x*x^m*x^(2*n)*e^m + 26*B*a^2*c*d*m^4*n*x*x^m*x^(2*n)*e^m + 52*A*a*b*c*d*m^4*n*x*x^m*x^(2*n)*e^m + 13*A*a^2*d^2*m^4*n*x*x^m*x^(2*n)*e^m + 118*B*a*b*c^2*m^3*n^2*x*x^m*x^(2*n)*e^m + 59*A*b^2*c^2*m^3*n^2*x*x^m*x^(2*n)*e^m + 118*B*a^2*c*d*m^3*n^2*x*x^m*x^(2*n)*e^m + 236*A*a*b*c*d*m^3*n^2*x*x^m*x^(2*n)*e^m + 59*A*a^2*d^2*m^3*n^2*x*x^m*x^(2*n)*e^m + 214*B*a*b*c^2*m^2*n^3*x*x^m*x^(2*n)*e^m + 107*A*b^2*c^2*m^2*n^3*x*x^m*x^(2*n)*e^m + 214*B*a^2*c*d*m^2*n^3*x*x^m*x^(2*n)*e^m + 428*A*a*b*c*d*m^2*n^3*x*x^m*x^(2*n)*e^m + 107*A*a^2*d^2*m^2*n^3*x*x^m*x^(2*n)*e^m + 120*B*a*b*c^2*m^n^4*x*x^m*x^(2*n)*e^m + 60*A*b^2*c^2*m^n^4*x*x^m*x^(2*n)*e^m + 120*B*a^2*c*d*m^n^4*x*x^m*x^(2*n)*e^m + 240*A*a*b*c*d*m^n^4*x*x^m*x^(2*n)*e^m + 60*A*a^2*d^2*m^n^4*x*x^m*x^(2*n)*e^m + B*a^2*c^2*m^5*x*x^m*x^n*e^m + 2*A*a*b*c^2*m^5*x*x^m*x^n*e^m + 2*A*a^2*c*d*m^5*x*x^m*x^n*e^m + 14*B*a^2*c^2*m^4*n*x*x^m*x^n*e^m + 28*A*a*b*c^2*m^4*n*x*x^m*x^n*e^m + 28*A*a^2*c*d*m^4*n*x*x^m*x^n*e^m + 71*B*a^2*c^2*m^3*n^2*x*x^m*x^n*e^m + 142*A*a*b*c^2*m^3*n^2*x*x^m*x^n*e^m + 142*A*a^2*c*d*m^3*n^2*x*x^m*x^n*e^m + 154*B*a^2*c^2*m^2*n^3*x*x^m*x^n*e^m + 308*A*a*b*c^2*m^2*n^3*x*x^m*x^n*e^m + 308*A*a^2*c*d*m^2*n^3*x*x^m*x^n*e^m + 120*B*a^2*c^2*m^n^4*x*x^m*x^n*e^m + 240*A*a*b*c^2*m^n^4*x*x^m*x^n*e^m + 240*A*a^2*c*d*m^n^4*x*x^m*x^n*e^m + A*a^2*c^2*m^5*x*x^m*e^m + 15*A*a^2*c^2*m^4*n*x*x^m*e^m + 85*A*a^2*c^2*m^3*n^2*x*x^m*e^m + 225*A*a^2*c^2*m^2*n^3*x*x^m*e^m + 274*A*a^2*c^2*m^n^4*x*x^m*e^m + 120*A*a^2*c^2*n^5*x*x^m*e^m + 5*B*b^2*d^2*m^4*x*x^m*x^(5*n)*e^m + 40*B*b^2*d^2*m^3*n*x*x^m*x^(5*n)*e^m + 105*B*b^2*d^2*m^2*n^2*x*x^m*x^(5*n)*e^m + 100*B*b^2*d^2*m^n^3*x*x^m*x^(5*n)*e^m + 24*B*b^2*d^2*n^4*x*x^m*x^(5*n)*e^m + 10*B*b^2*c*d*m^4*x*x^m*x^(4*n)*e^m + 10*B*a*b*d^2*m^4*x*x^m*x^(4*n)*e^m + 5*A*b^2*d^2*m^4*x*x^m*x^(4*n)*e^m + 88*B*b^2*c*d*m^3*n*x*x^m*x^(4*n)*e^m + 88*B*a*b*d^2*m^3*n*x*x^m*x^(4*n)*e^m + 44*A*b^2*d^2*m^3*n*x*x^m*x^(4*n)*e^m + 246*B*b^2*c*d*m^2*n^2*x*x^m*x^(4*n)*e^m + 246*B*a*b*d^2*m^2*n^2*x*x^m*x^(4*n)*e^m + 123*A*b^2*d^2*m^2*n^2*x*x^m*x^(4*n)*e^m + 244*B*b^2*c*d*m^n^3*x*x^m*x^(4*n)*e^m + 244*B*a*b*d^2*m^n^3*x*x^m*x^(4*n)*e^m + 122*A*b^2*d^2*m^n^3*x*x^m*x^(4*n)*e^m + 60*B*b^2*c*d*n^4*x*x^m*x^(4*n)*e^m + 60*B*a*b*d^2*n^4*x*x^m*x^(4*n)*e^m + 30*A*b^2*d^2*n^4*x*x^m*x^(4*n)*e^m + 5*B*b^2*c^2*m^4*x*x^m*x^(3*n)*e^m + 20*B*a*b*c*d*m^4*x*x^m*x^(3*n)*e^m + 10*A*b^2*c*d*m^4*x*x^m*x^(3*n)*e^m + 5*B*a^2*d^2*m^4*x*x^m*x^(3*n)*e^m + 10*A*a*b*d^2*m^4*x*x^m*x^(3*n)*e^m + 48*B*b^2*c^2*m^3*n*x*x^m*x^(3*n)*e^m + 192*B*a*b*c*d*m^3*n*x*x^m*x^(3*n)*e^m + 96*A*b^2*c*d*m^3*n*x*x^m*x^(3*n)*e^m + 48*B*a^2*d^2*m^3*n*x*x^m*x^(3*n)*e^m + 96*A*a*b*d^2*m^3*n*x*x^m*x^(3*n)*e^m + 147*B*b^2*c^2*m^2*n^2*x*x^m*x^(3*n)*e^m + 588*B*a*b*c*d*m^2*n^2*x*x^m*x^(3*n)*e^m + 294*A*b^2*c*d*m^2*n^2*x*x^m*x^(3*n)*e^m + 147*B*a^2*d^2*m^2*n^2*x*x^m*x^(3*n)*e^m + 294*A*a*b*d^2*m^2*n^2*x*x^m*x^(3*n)*e^m + 156*B*b^2*c^2*m^n^3*x*x^m*x^(3*n)*e^m + 624*B*a*b*c*d*m^n^3*x*x^m*x^(3*n)*e^m + 312*A*b^2*c*d*m^n^3*x*x^m*x^(3*n)*e^m + 156*B*a^2*d^2*m^n^3*x*x^m*x^(3*n)*e^m + 312*A*a*b*d^2*m^n^3*x*x^m*x^(3*n)*e^m + 40*B*b^2*c^2*n^4*x*x^m*x^(3*n)*e^m + 160*B*a*b*c*d*n^4*x*x^m*x
\end{aligned}$$



$$\begin{aligned}
& 5*A*a^2*c^2*m*n^2*x*x^m*e^m + 225*A*a^2*c^2*n^3*x*x^m*e^m + 10*B*b^2*d^2*m^2 \\
& 2*x*x^m*x^(5*n)*e^m + 40*B*b^2*d^2*m*n*x*x^m*x^(5*n)*e^m + 35*B*b^2*d^2*n^2 \\
& *x*x^m*x^(5*n)*e^m + 20*B*b^2*c*d*m^2*x*x^m*x^(4*n)*e^m + 20*B*a*b*d^2*m^2* \\
& x*x^m*x^(4*n)*e^m + 10*A*b^2*d^2*m^2*x*x^m*x^(4*n)*e^m + 88*B*b^2*c*d*m*n*x \\
& *x^m*x^(4*n)*e^m + 88*B*a*b*d^2*m*n*x*x^m*x^(4*n)*e^m + 44*A*b^2*d^2*m*n*x \\
& x^m*x^(4*n)*e^m + 82*B*b^2*c*d*n^2*x*x^m*x^(4*n)*e^m + 82*B*a*b*d^2*n^2*x*x \\
& ^m*x^(4*n)*e^m + 41*A*b^2*d^2*n^2*x*x^m*x^(4*n)*e^m + 10*B*b^2*c^2*m^2*x*x^ \\
& m*x^(3*n)*e^m + 40*B*a*b*c*d*m^2*x*x^m*x^(3*n)*e^m + 20*A*b^2*c*d*m^2*x*x^m \\
& *x^(3*n)*e^m + 10*B*a^2*d^2*m^2*x*x^m*x^(3*n)*e^m + 20*A*a*b*d^2*m^2*x*x^m* \\
& x^(3*n)*e^m + 48*B*b^2*c^2*m*n*x*x^m*x^(3*n)*e^m + 192*B*a*b*c*d*m*n*x*x^m* \\
& x^(3*n)*e^m + 96*A*b^2*c*d*m*n*x*x^m*x^(3*n)*e^m + 48*B*a^2*d^2*m*n*x*x^m*x \\
& ^3(n)*e^m + 96*A*a*b*d^2*m*n*x*x^m*x^(3*n)*e^m + 49*B*b^2*c^2*n^2*x*x^m*x^ \\
& (3*n)*e^m + 196*B*a*b*c*d*n^2*x*x^m*x^(3*n)*e^m + 98*A*b^2*c*d*n^2*x*x^m*x^ \\
& (3*n)*e^m + 49*B*a^2*d^2*n^2*x*x^m*x^(3*n)*e^m + 98*A*a*b*d^2*n^2*x*x^m*x^ \\
& (3*n)*e^m + 20*B*a*b*c^2*m^2*x*x^m*x^(2*n)*e^m + 10*A*b^2*c^2*m^2*x*x^m*x^(2 \\
& *n)*e^m + 20*B*a^2*c*d*m^2*x*x^m*x^(2*n)*e^m + 40*A*a*b*c*d*m^2*x*x^m*x^(2* \\
& n)*e^m + 10*A*a^2*d^2*m^2*x*x^m*x^(2*n)*e^m + 104*B*a*b*c^2*m*n*x*x^m*x^(2* \\
& n)*e^m + 52*A*b^2*c^2*m*n*x*x^m*x^(2*n)*e^m + 104*B*a^2*c*d*m*n*x*x^m*x^(2* \\
& n)*e^m + 208*A*a*b*c*d*m*n*x*x^m*x^(2*n)*e^m + 52*A*a^2*d^2*m*n*x*x^m*x^(2* \\
& n)*e^m + 118*B*a*b*c^2*n^2*x*x^m*x^(2*n)*e^m + 59*A*b^2*c^2*n^2*x*x^m*x^(2* \\
& n)*e^m + 118*B*a^2*c*d*n^2*x*x^m*x^(2*n)*e^m + 236*A*a*b*c*d*n^2*x*x^m*x^(2 \\
& *n)*e^m + 59*A*a^2*d^2*n^2*x*x^m*x^(2*n)*e^m + 10*B*a^2*c^2*m^2*x*x^m*x^n*e \\
& ^m + 20*A*a*b*c^2*m^2*x*x^m*x^n*e^m + 20*A*a^2*c*d*m^2*x*x^m*x^n*e^m + 56*B \\
& *a^2*c^2*m*n*x*x^m*x^n*e^m + 112*A*a*b*c^2*m*n*x*x^m*x^n*e^m + 112*A*a^2*c* \\
& d*m*n*x*x^m*x^n*e^m + 71*B*a^2*c^2*n^2*x*x^m*x^n*e^m + 142*A*a*b*c^2*n^2*x* \\
& x^m*x^n*e^m + 142*A*a^2*c*d*n^2*x*x^m*x^n*e^m + 10*A*a^2*c^2*m^2*x*x^m*e^m \\
& + 60*A*a^2*c^2*m*n*x*x^m*e^m + 85*A*a^2*c^2*n^2*x*x^m*e^m + 5*B*b^2*d^2*m*x \\
& *x^m*x^(5*n)*e^m + 10*B*b^2*d^2*n*x*x^m*x^(5*n)*e^m + 10*B*b^2*c*d*m*x*x^m* \\
& x^(4*n)*e^m + 10*B*a*b*d^2*m*x*x^m*x^(4*n)*e^m + 5*A*b^2*d^2*m*x*x^m*x^(4*n \\
& )*e^m + 22*B*b^2*c*d*n*x*x^m*x^(4*n)*e^m + 22*B*a*b*d^2*n*x*x^m*x^(4*n)*e^m \\
& + 11*A*b^2*d^2*n*x*x^m*x^(4*n)*e^m + 5*B*b^2*c^2*m*x*x^m*x^(3*n)*e^m + 20* \\
& B*a*b*c*d*m*x*x^m*x^(3*n)*e^m + 10*A*b^2*c*d*m*x*x^m*x^(3*n)*e^m + 5*B*a^2* \\
& d^2*m*x*x^m*x^(3*n)*e^m + 10*A*a*b*d^2*m*x*x^m*x^(3*n)*e^m + 12*B*b^2*c^2*n \\
& *x*x^m*x^(3*n)*e^m + 48*B*a*b*c*d*n*x*x^m*x^(3*n)*e^m + 24*A*b^2*c*d*n*x*x^ \\
& m*x^(3*n)*e^m + 12*B*a^2*d^2*n*x*x^m*x^(3*n)*e^m + 24*A*a*b*d^2*n*x*x^m*x^( \\
& 3*n)*e^m + 10*B*a*b*c^2*m*x*x^m*x^(2*n)*e^m + 5*A*b^2*c^2*m*x*x^m*x^(2*n)*e \\
& ^m + 10*B*a^2*c*d*m*x*x^m*x^(2*n)*e^m + 20*A*a*b*c*d*m*x*x^m*x^(2*n)*e^m + \\
& 5*A*a^2*d^2*m*x*x^m*x^(2*n)*e^m + 26*B*a*b*c^2*n*x*x^m*x^(2*n)*e^m + 13*A*b \\
& ^2*c^2*n*x*x^m*x^(2*n)*e^m + 26*B*a^2*c*d*n*x*x^m*x^(2*n)*e^m + 52*A*a*b*c* \\
& d*n*x*x^m*x^(2*n)*e^m + 13*A*a^2*d^2*n*x*x^m*x^(2*n)*e^m + 5*B*a^2*c^2*m*x* \\
& x^m*x^n*e^m + 10*A*a*b*c^2*m*x*x^m*x^n*e^m + 10*A*a^2*c*d*m*x*x^m*x^n*e^m + \\
& 14*B*a^2*c^2*n*x*x^m*x^n*e^m + 28*A*a*b*c^2*n*x*x^m*x^n*e^m + 28*A*a^2*c*d \\
& *n*x*x^m*x^n*e^m + 5*A*a^2*c^2*m*x*x^m*e^m + 15*A*a^2*c^2*n*x*x^m*e^m + B*b \\
& ^2*d^2*x*x^m*x^(5*n)*e^m + 2*B*b^2*c*d*x*x^m*x^(4*n)*e^m + 2*B*a*b*d^2*x*x^ \\
& m*x^(4*n)*e^m + A*b^2*d^2*x*x^m*x^(4*n)*e^m + B*b^2*c^2*x*x^m*x^(3*n)*e^m + \\
& 4*B*a*b*c*d*x*x^m*x^(3*n)*e^m + 2*A*b^2*c*d*x*x^m*x^(3*n)*e^m + B*a^2*d^2* \\
& x*x^m*x^(3*n)*e^m + 2*A*a*b*d^2*x*x^m*x^(3*n)*e^m + 2*B*a*b*c^2*x*x^m*x^(2* \\
& n)*e^m + A*b^2*c^2*x*x^m*x^(2*n)*e^m + 2*B*a^2*c*d*x*x^m*x^(2*n)*e^m + 4*A* \\
& a*b*c*d*x*x^m*x^(2*n)*e^m + A*a^2*d^2*x*x^m*x^(2*n)*e^m + B*a^2*c^2*x*x^m*x \\
& ^n*e^m + 2*A*a*b*c^2*x*x^m*x^n*e^m + 2*A*a^2*c*d*x*x^m*x^n*e^m + A*a^2*c^2* \\
& x*x^m*e^m)/(m^6 + 15*m^5*n + 85*m^4*n^2 + 225*m^3*n^3 + 274*m^2*n^4 + 120*m \\
& *n^5 + 6*m^5 + 75*m^4*n + 340*m^3*n^2 + 675*m^2*n^3 + 548*m*n^4 + 120*n^5 + \\
& 15*m^4 + 150*m^3*n + 510*m^2*n^2 + 675*m*n^3 + 274*n^4 + 20*m^3 + 150*m^2* \\
& n + 340*m*n^2 + 225*n^3 + 15*m^2 + 75*m*n + 85*n^2 + 6*m + 15*n + 1)
\end{aligned}$$

**maple [C]** time = 0.17, size = 5908, normalized size = 24.93

output too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e^x)^m \cdot (b \cdot x^n + a)^2 \cdot (B \cdot x^n + A) \cdot (d \cdot x^n + c)^2, x)$

[Out] result too large to display

**maxima** [B] time = 0.91, size = 540, normalized size = 2.28

---

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{integrate}((e^x)^m \cdot (a + b \cdot x^n)^2 \cdot (A + B \cdot x^n) \cdot (c + d \cdot x^n)^2, x, \text{algorithm} = \text{"maxima"})$

[Out]  $B \cdot b^2 \cdot d^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+5n) \cdot \log(x)} / (m+5n+1) + 2 \cdot B \cdot b^2 \cdot c \cdot d \cdot e^{m \cdot \log(x)} \cdot e^{(m+4n) \cdot \log(x)} / (m+4n+1) + 2 \cdot B \cdot a \cdot b \cdot d^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+4n) \cdot \log(x)} / (m+4n+1) + A \cdot b^2 \cdot d^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+4n) \cdot \log(x)} / (m+4n+1) + B \cdot b^2 \cdot c^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+3n) \cdot \log(x)} / (m+3n+1) + 4 \cdot B \cdot a \cdot b \cdot c \cdot d \cdot e^{m \cdot \log(x)} \cdot e^{(m+3n) \cdot \log(x)} / (m+3n+1) + 2 \cdot A \cdot b^2 \cdot c \cdot d \cdot e^{m \cdot \log(x)} \cdot e^{(m+3n) \cdot \log(x)} / (m+3n+1) + B \cdot a^2 \cdot d^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+3n) \cdot \log(x)} / (m+3n+1) + 2 \cdot A \cdot a \cdot b \cdot d^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+3n) \cdot \log(x)} / (m+3n+1) + 2 \cdot B \cdot a \cdot b \cdot c^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+2n) \cdot \log(x)} / (m+2n+1) + A \cdot b^2 \cdot c^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+2n) \cdot \log(x)} / (m+2n+1) + 2 \cdot B \cdot a^2 \cdot c \cdot d \cdot e^{m \cdot \log(x)} \cdot e^{(m+2n) \cdot \log(x)} / (m+2n+1) + 4 \cdot A \cdot a \cdot b \cdot c \cdot d \cdot e^{m \cdot \log(x)} \cdot e^{(m+2n) \cdot \log(x)} / (m+2n+1) + A \cdot a^2 \cdot d^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+2n) \cdot \log(x)} / (m+2n+1) + B \cdot a^2 \cdot c^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+n) \cdot \log(x)} / (m+n+1) + 2 \cdot A \cdot a \cdot b \cdot c^2 \cdot e^{m \cdot \log(x)} \cdot e^{(m+n) \cdot \log(x)} / (m+n+1) + 2 \cdot A \cdot a^2 \cdot c \cdot d \cdot e^{m \cdot \log(x)} \cdot e^{(m+n) \cdot \log(x)} / (m+n+1) + (e^x)^{m+1} \cdot A \cdot a^2 \cdot c^2 / (e^{m+1})$

**mupad** [B] time = 5.59, size = 1119, normalized size = 4.72

---

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e^x)^m \cdot (A + B \cdot x^n) \cdot (a + b \cdot x^n)^2 \cdot (c + d \cdot x^n)^2, x)$

[Out]  $(x \cdot x^{2n}) \cdot (e^x)^m \cdot (A \cdot a^2 \cdot d^2 + A \cdot b^2 \cdot c^2 + 2 \cdot B \cdot a \cdot b \cdot c^2 + 2 \cdot B \cdot a^2 \cdot c \cdot d + 4 \cdot A \cdot a \cdot b \cdot c \cdot d) \cdot (4m + 13n + 39m \cdot n + 118m \cdot n^2 + 39m^2 \cdot n + 107m \cdot n^3 + 13m^3 \cdot n + 6m^2 + 4m^3 + m^4 + 59n^2 + 107n^3 + 60n^4 + 59m^2 \cdot n^2 + 1) / (5m + 15n + 60m \cdot n + 255m \cdot n^2 + 90m^2 \cdot n + 450m \cdot n^3 + 60m^3 \cdot n + 274m \cdot n^4 + 15m^4 \cdot n + 10m^2 + 10m^3 + 5m^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2 \cdot n^2 + 225m^2 \cdot n^3 + 85m^3 \cdot n^2 + 1) + (x \cdot x^{3n}) \cdot (e^x)^m \cdot (B \cdot a^2 \cdot d^2 + B \cdot b^2 \cdot c^2 + 2 \cdot A \cdot a \cdot b \cdot d^2 + 2 \cdot A \cdot b^2 \cdot c \cdot d + 4 \cdot B \cdot a \cdot b \cdot c \cdot d) \cdot (4m + 12n + 36m \cdot n + 98m \cdot n^2 + 36m^2 \cdot n + 78m \cdot n^3 + 12m^3 \cdot n + 6m^2 + 4m^3 + m^4 + 49n^2 + 78n^3 + 40n^4 + 49m^2 \cdot n^2 + 1) / (5m + 15n + 60m \cdot n + 255m \cdot n^2 + 90m^2 \cdot n + 450m \cdot n^3 + 60m^3 \cdot n + 274m \cdot n^4 + 15m^4 \cdot n + 10m^2 + 10m^3 + 5m^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2 \cdot n^2 + 225m^2 \cdot n^3 + 85m^3 \cdot n^2 + 1) + (A \cdot a^2 \cdot c^2 \cdot x \cdot (e^x)^m) / (m+1) + (b \cdot d \cdot x \cdot x^{4n}) \cdot (e^x)^m \cdot (A \cdot b \cdot d + 2 \cdot B \cdot a \cdot d + 2 \cdot B \cdot b \cdot c) \cdot (4m + 11n + 33m \cdot n + 82m \cdot n^2 + 33m^2 \cdot n + 61m \cdot n^3 + 11m^3 \cdot n + 6m^2 + 4m^3 + m^4 + 41n^2 + 61n^3 + 30n^4 + 41m^2 \cdot n^2 + 1) / (5m + 15n + 60m \cdot n + 255m \cdot n^2 + 90m^2 \cdot n + 450m \cdot n^3 + 60m^3 \cdot n + 274m \cdot n^4 + 15m^4 \cdot n + 10m^2 + 10m^3 + 5m^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2 \cdot n^2 + 225m^2 \cdot n^3 + 85m^3 \cdot n^2 + 1) + (B \cdot b^2 \cdot d^2 \cdot x \cdot x^{5n}) \cdot (e^x)^m \cdot (4m + 10n + 30m \cdot n + 70m \cdot n^2 + 30m^2 \cdot n + 50m \cdot n^3 + 10m^3 \cdot n + 6m^2 + 4m^3 + m^4 + 35n^2 + 50n^3 + 24n^4 + 35m^2 \cdot n^2 + 1) / (5m + 15n + 60m \cdot n + 255m \cdot n^2 + 90m^2 \cdot n + 450m \cdot n^3 + 60m^3 \cdot n + 274m \cdot n^4 + 15m^4 \cdot n + 10m^2 + 10m^3 + 5m^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2 \cdot n^2 + 225m^2 \cdot n^3 + 85m^3 \cdot n^2 + 1) + (a \cdot c \cdot x \cdot x^n) \cdot (e^x)^m \cdot (2 \cdot A \cdot a \cdot d + 2 \cdot A \cdot b \cdot c + B \cdot a \cdot c) \cdot (4m + 14n + 42m \cdot n + 142m \cdot n^2 + 42m^2 \cdot n + 154m \cdot n^3 + 14m^3 \cdot n + 6m^2 + 4m^3 + m^4 + 71n^2 + 154n^3 + 120n^4 + 71m^2 \cdot n^2 + 1) / (5m + 15n + 60m \cdot n + 255m \cdot n^2 + 90m^2 \cdot n + 450m \cdot n^3 + 60m^3 \cdot n + 274m \cdot n^4 + 15m^4 \cdot n + 10m^2 + 10m^3 + 5m^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2 \cdot n^2 + 225m^2 \cdot n^3 + 85m^3 \cdot n^2 + 1)$

$n^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2n^2 + 225m^2n^3 + 85m^3n^2 + 1)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*2\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*2,x)

[Out] Timed out



### 3.7 $\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^2 dx$

**Optimal.** Leaf size=160

$$\frac{cx^{n+1}(ex)^m(2aAd + aBc + Abc)}{m + n + 1} + \frac{x^{2n+1}(ex)^m(ad(Ad + 2Bc) + bc(2Ad + Bc))}{m + 2n + 1} + \frac{dx^{3n+1}(ex)^m(aBd + Abd + 2bBc)}{m + 3n + 1}$$

**Rubi [A]** time = 0.17, antiderivative size = 160, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ , Rules used = {570, 20, 30}

$$\frac{cx^{n+1}(ex)^m(2aAd + aBc + Abc)}{m + n + 1} + \frac{x^{2n+1}(ex)^m(ad(Ad + 2Bc) + bc(2Ad + Bc))}{m + 2n + 1} + \frac{dx^{3n+1}(ex)^m(aBd + Abd + 2bBc)}{m + 3n + 1} + \frac{aAc^2(ex)^{m+1}}{e(m+1)} + \frac{bBd^2x^{4n+1}(ex)^m}{m + 4n + 1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] (c\*(A\*b\*c + a\*B\*c + 2\*a\*A\*d)\*x^(1 + n)\*(e\*x)^m)/(1 + m + n) + ((a\*d\*(2\*B\*c + A\*d) + b\*c\*(B\*c + 2\*A\*d))\*x^(1 + 2\*n)\*(e\*x)^m)/(1 + m + 2\*n) + (d\*(2\*b\*B\*c + A\*b\*d + a\*B\*d)\*x^(1 + 3\*n)\*(e\*x)^m)/(1 + m + 3\*n) + (b\*B\*d^2\*x^(1 + 4\*n)\*(e\*x)^m)/(1 + m + 4\*n) + (a\*A\*c^2\*(e\*x)^(1 + m))/(e\*(1 + m))

#### Rule 20

Int[(u\_.)\*((a\_.)\*(v\_.))^(m\_.)\*((b\_.)\*(v\_.))^(n\_.), x\_Symbol] :> Dist[(b^IntPart[n]\*(v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m + n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

#### Rule 30

Int[(x\_)^(m\_.), x\_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

#### Rule 570

Int[((g\_.)\*(x\_.))^(m\_.)\*((a\_.) + (b\_.)\*(x\_.)^(n\_.))^(p\_.)\*((c\_.) + (d\_.)\*(x\_.)^(n\_.))^(q\_.)\*((e\_.) + (f\_.)\*(x\_.)^(n\_.))^(r\_.), x\_Symbol] :> Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

#### Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^2 dx &= \int (aAc^2(ex)^m + c(abc + aBc + 2aAd)x^n(ex)^m + (ad(2Bc + Ad) - \\ &= \frac{aAc^2(ex)^{1+m}}{e(1+m)} + (bBd^2) \int x^{4n}(ex)^m dx + (c(abc + aBc + 2aAd)) \\ &= \frac{aAc^2(ex)^{1+m}}{e(1+m)} + (bBd^2x^{-m}(ex)^m) \int x^{m+4n} dx + (c(abc + aBc + 2aAd)) \\ &= \frac{c(abc + aBc + 2aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{(ad(2Bc + Ad) + bc(Bc + 2aAd))x^{4n+1}(ex)^m}{1+m+2n} \end{aligned}$$

**Mathematica [A]** time = 0.31, size = 129, normalized size = 0.81

$$x(ex)^m \left( \frac{x^{2n}(ad(Ad + 2Bc) + bc(2Ad + Bc))}{m + 2n + 1} + \frac{dx^{3n}(aBd + Abd + 2bBc)}{m + 3n + 1} + \frac{cx^n(2aAd + aBc + Abc)}{m + n + 1} + \frac{aAc^2}{m + 1} + \frac{bBd^2x^{4n}}{m + 4n + 1} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] x\*(e\*x)^m\*((a\*A\*c^2)/(1 + m) + (c\*(A\*b\*c + a\*B\*c + 2\*a\*A\*d)\*x^n)/(1 + m + n) + ((a\*d\*(2\*B\*c + A\*d) + b\*c\*(B\*c + 2\*A\*d))\*x^(2\*n))/(1 + m + 2\*n) + (d\*(2\*b\*B\*c + A\*b\*d + a\*B\*d)\*x^(3\*n))/(1 + m + 3\*n) + (b\*B\*d^2\*x^(4\*n))/(1 + m + 4\*n))

**IntegrateAlgebraic** [F] time = 0.16, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n)(A + Bx^n)(c + dx^n)^2 dx$$

Verification is not applicable to the result.

[In] IntegrateAlgebraic[(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] Defer[IntegrateAlgebraic] [(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n)^2, x]

**fricas** [B] time = 0.48, size = 1426, normalized size = 8.91

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="fricas")

[Out] ((B\*b\*d^2\*m^4 + 4\*B\*b\*d^2\*m^3 + 6\*B\*b\*d^2\*m^2 + 4\*B\*b\*d^2\*m + B\*b\*d^2 + 6\*(B\*b\*d^2\*m + B\*b\*d^2)\*n^3 + 11\*(B\*b\*d^2\*m^2 + 2\*B\*b\*d^2\*m + B\*b\*d^2)\*n^2 + 6\*(B\*b\*d^2\*m^3 + 3\*B\*b\*d^2\*m^2 + 3\*B\*b\*d^2\*m + B\*b\*d^2)\*n)\*x\*x^(4\*n)\*e^(m\*log(e) + m\*log(x)) + ((2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2)\*m^4 + 2\*B\*b\*c\*d + 4\*(2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2)\*m^3 + 8\*(2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2 + (2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2)\*m)\*n^3 + (B\*a + A\*b)\*d^2 + 6\*(2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2)\*m^2 + 14\*(2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2 + (2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2)\*m^2 + 2\*(2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2)\*m)\*n^2 + 4\*(2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2)\*m + 7\*(2\*B\*b\*c\*d + (2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2)\*m^3 + (B\*a + A\*b)\*d^2 + 3\*(2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2)\*m^2 + 3\*(2\*B\*b\*c\*d + (B\*a + A\*b)\*d^2)\*m)\*n)\*x\*x^(3\*n)\*e^(m\*log(e) + m\*log(x)) + ((B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d)\*m^4 + B\*b\*c^2 + A\*a\*d^2 + 4\*(B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d)\*m^3 + 12\*(B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d + (B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d)\*m)\*n^3 + 2\*(B\*a + A\*b)\*c\*d + 6\*(B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d)\*m^2 + 19\*(B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d + (B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d)\*m^2 + 2\*(B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d)\*m)\*n^2 + 4\*(B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d)\*m + 8\*(B\*b\*c^2 + A\*a\*d^2 + (B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d)\*m^3 + 2\*(B\*a + A\*b)\*c\*d + 3\*(B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d)\*m^2 + 3\*(B\*b\*c^2 + A\*a\*d^2 + 2\*(B\*a + A\*b)\*c\*d)\*m)\*n)\*x\*x^n\*e^(m\*log(e) + m\*log(x)) + (A\*a\*c^2\*m^4 + 24\*A\*a\*c^2\*n^4 + 4\*A\*a\*c^2\*m^3 + 6\*A\*a\*c^2\*m^2 + 4\*A\*a\*c^2\*m + A\*a\*c^2 + 50\*(A\*a\*c^2\*m + A\*a\*c^2)\*n^3 + 35\*(A\*a\*c^2\*m^2 + 2\*A\*a\*c^2\*m + A\*a\*c^2)\*n^2 + 10\*(A\*a\*c^2\*m^3 + 3\*A\*a\*c^2\*m^2 + 3\*A\*a\*c^2\*m + A\*a\*c^2)\*n)\*x\*e^(m\*log(e) + m\*log(x)))/(m^5 + 24\*(m + 1)\*n^4 + 5\*m^4 + 50\*(m^2 + 2\*m + 1)\*n^3 + 10\*m^3 + 35\*(m^3 + 3\*m^2 + 3\*m + 1)\*n^2 + 10\*m^2 + 10\*(m^4 + 4\*m^3 + 6\*m^2 + 4\*m + 1)\*n + 5\*m + 1)

**giac** [B] time = 0.82, size = 3415, normalized size = 21.34

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="giac")

[Out]  $(B*b*d^2*m^4*x*x^m*x^{(4*n)}*e^m + 6*B*b*d^2*m^3*n*x*x^m*x^{(4*n)}*e^m + 11*B*b*d^2*m^2*n^2*x*x^m*x^{(4*n)}*e^m + 6*B*b*d^2*m*n^3*x*x^m*x^{(4*n)}*e^m + 2*B*b*c*d*m^4*x*x^m*x^{(3*n)}*e^m + B*a*d^2*m^4*x*x^m*x^{(3*n)}*e^m + A*b*d^2*m^4*x*x^m*x^{(3*n)}*e^m + 14*B*b*c*d*m^3*n*x*x^m*x^{(3*n)}*e^m + 7*B*a*d^2*m^3*n*x*x^m*x^{(3*n)}*e^m + 7*A*b*d^2*m^3*n*x*x^m*x^{(3*n)}*e^m + 28*B*b*c*d*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 14*B*a*d^2*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 14*A*b*d^2*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 16*B*b*c*d*m*n^3*x*x^m*x^{(3*n)}*e^m + 8*B*a*d^2*m*n^3*x*x^m*x^{(3*n)}*e^m + 8*A*b*d^2*m*n^3*x*x^m*x^{(3*n)}*e^m + B*b*c^2*m^4*x*x^m*x^{(2*n)}*e^m + 2*B*a*c*d*m^4*x*x^m*x^{(2*n)}*e^m + 2*A*b*c*d*m^4*x*x^m*x^{(2*n)}*e^m + A*a*d^2*m^4*x*x^m*x^{(2*n)}*e^m + 8*B*b*c^2*m^3*n*x*x^m*x^{(2*n)}*e^m + 16*B*a*c*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 16*A*b*c*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 8*A*a*d^2*m^3*n*x*x^m*x^{(2*n)}*e^m + 19*B*b*c^2*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 38*B*a*c*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 38*A*b*c*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 19*A*a*d^2*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 12*B*b*c^2*m*n^3*x*x^m*x^{(2*n)}*e^m + 24*B*a*c*d*m*n^3*x*x^m*x^{(2*n)}*e^m + 24*A*b*c*d*m*n^3*x*x^m*x^{(2*n)}*e^m + 12*A*a*d^2*m*n^3*x*x^m*x^{(2*n)}*e^m + B*a*c^2*m^4*x*x^m*x^n*e^m + A*b*c^2*m^4*x*x^m*x^n*e^m + 2*A*a*c*d*m^4*x*x^m*x^n*e^m + 9*B*a*c^2*m^3*n*x*x^m*x^n*e^m + 9*A*b*c^2*m^3*n*x*x^m*x^n*e^m + 18*A*a*c*d*m^3*n*x*x^m*x^n*e^m + 26*B*a*c^2*m^2*n^2*x*x^m*x^n*e^m + 26*A*b*c^2*m^2*n^2*x*x^m*x^n*e^m + 52*A*a*c*d*m^2*n^2*x*x^m*x^n*e^m + 24*B*a*c^2*m*n^3*x*x^m*x^n*e^m + 24*A*b*c^2*m*n^3*x*x^m*x^n*e^m + 48*A*a*c*d*m*n^3*x*x^m*x^n*e^m + A*a*c^2*m^4*x*x^m*e^m + 10*A*a*c^2*m^3*n*x*x^m*e^m + 35*A*a*c^2*m^2*n^2*x*x^m*e^m + 50*A*a*c^2*m*n^3*x*x^m*e^m + 24*A*a*c^2*n^4*x*x^m*e^m + 4*B*b*d^2*m^3*x*x^m*x^{(4*n)}*e^m + 18*B*b*d^2*m^2*n*x*x^m*x^{(4*n)}*e^m + 22*B*b*d^2*m*n^2*x*x^m*x^{(4*n)}*e^m + 6*B*b*d^2*n^3*x*x^m*x^{(4*n)}*e^m + 8*B*b*c*d*m^3*x*x^m*x^{(3*n)}*e^m + 4*B*a*d^2*m^3*x*x^m*x^{(3*n)}*e^m + 4*A*b*d^2*m^3*x*x^m*x^{(3*n)}*e^m + 42*B*b*c*d*m^2*n*x*x^m*x^{(3*n)}*e^m + 21*B*a*d^2*m^2*n*x*x^m*x^{(3*n)}*e^m + 21*A*b*d^2*m^2*n*x*x^m*x^{(3*n)}*e^m + 56*B*b*c*d*m*n^2*x*x^m*x^{(3*n)}*e^m + 28*B*a*d^2*m*n^2*x*x^m*x^{(3*n)}*e^m + 16*B*b*c*d*n^3*x*x^m*x^{(3*n)}*e^m + 8*B*a*d^2*n^3*x*x^m*x^{(3*n)}*e^m + 8*A*b*d^2*n^3*x*x^m*x^{(3*n)}*e^m + 4*B*b*c^2*m^3*x*x^m*x^{(2*n)}*e^m + 8*B*a*c*d*m^3*x*x^m*x^{(2*n)}*e^m + 8*A*b*c*d*m^3*x*x^m*x^{(2*n)}*e^m + 4*A*a*d^2*m^3*x*x^m*x^{(2*n)}*e^m + 24*B*b*c^2*m^2*n*x*x^m*x^{(2*n)}*e^m + 48*B*a*c*d*m^2*n*x*x^m*x^{(2*n)}*e^m + 48*A*b*c*d*m^2*n*x*x^m*x^{(2*n)}*e^m + 24*A*a*d^2*m^2*n*x*x^m*x^{(2*n)}*e^m + 38*B*b*c^2*m*n^2*x*x^m*x^{(2*n)}*e^m + 76*B*a*c*d*m*n^2*x*x^m*x^{(2*n)}*e^m + 76*A*b*c*d*m*n^2*x*x^m*x^{(2*n)}*e^m + 38*A*a*d^2*m*n^2*x*x^m*x^{(2*n)}*e^m + 12*B*b*c^2*n^3*x*x^m*x^{(2*n)}*e^m + 24*B*a*c*d*n^3*x*x^m*x^{(2*n)}*e^m + 24*A*b*c*d*n^3*x*x^m*x^{(2*n)}*e^m + 12*A*a*d^2*n^3*x*x^m*x^{(2*n)}*e^m + 4*B*a*c^2*m^3*x*x^m*x^n*e^m + 4*A*b*c^2*m^3*x*x^m*x^n*e^m + 8*A*a*c*d*m^3*x*x^m*x^n*e^m + 27*B*a*c^2*m^2*n*x*x^m*x^n*e^m + 27*A*b*c^2*m^2*n*x*x^m*x^n*e^m + 54*A*a*c*d*m^2*n*x*x^m*x^n*e^m + 52*B*a*c^2*m*n^2*x*x^m*x^n*e^m + 52*A*b*c^2*m*n^2*x*x^m*x^n*e^m + 104*A*a*c*d*m*n^2*x*x^m*x^n*e^m + 24*B*a*c^2*n^3*x*x^m*x^n*e^m + 24*A*b*c^2*n^3*x*x^m*x^n*e^m + 48*A*a*c*d*n^3*x*x^m*x^n*e^m + 4*A*a*c^2*m^3*x*x^m*e^m + 30*A*a*c^2*m^2*n*x*x^m*e^m + 70*A*a*c^2*m*n^2*x*x^m*e^m + 50*A*a*c^2*n^3*x*x^m*e^m + 6*B*b*d^2*m^2*x*x^m*x^{(4*n)}*e^m + 18*B*b*d^2*m*n*x*x^m*x^{(4*n)}*e^m + 11*B*b*d^2*n^2*x*x^m*x^{(4*n)}*e^m + 12*B*b*c*d*m^2*x*x^m*x^{(3*n)}*e^m + 6*B*a*d^2*m^2*x*x^m*x^{(3*n)}*e^m + 6*A*b*d^2*m^2*x*x^m*x^{(3*n)}*e^m + 42*B*b*c*d*m*n*x*x^m*x^{(3*n)}*e^m + 21*B*a*d^2*m*n*x*x^m*x^{(3*n)}*e^m + 21*A*b*d^2*m*n*x*x^m*x^{(3*n)}*e^m + 28*B*b*c*d*n^2*x*x^m*x^{(3*n)}*e^m + 14*B*a*d^2*n^2*x*x^m*x^{(3*n)}*e^m + 14*A*b*d^2*n^2*x*x^m*x^{(3*n)}*e^m + 6*B*b*c^2*m^2*x*x^m*x^{(2*n)}*e^m + 12*B*a*c*d*m^2*x*x^m*x^{(2*n)}*e^m + 12*A*b*c*d*m^2*x*x^m*x^{(2*n)}*e^m + 6*A*a*d^2*m^2*x*x^m*x^{(2*n)}*e^m + 24*B*b*c^2*m*n*x*x^m*x^{(2*n)}*e^m + 48*B*a*c*d*m*n*x*x^m*x^{(2*n)}*e^m + 48*A*b*c*d*m*n*x*x^m*x^{(2*n)}*e^m + 24*A*a*d^2*m*n*x*x^m*x^{(2*n)}*e^m + 19*B*b*c^2*n^2*x*x^m*x^{(2*n)}*e^m +$

$$\begin{aligned}
& 38*B*a*c*d*n^2*x*x^m*x^{(2*n)}*e^m + 38*A*b*c*d*n^2*x*x^m*x^{(2*n)}*e^m + 19*A* \\
& a*d^2*n^2*x*x^m*x^{(2*n)}*e^m + 6*B*a*c^2*m^2*x*x^m*x^n*e^m + 6*A*b*c^2*m^2*x \\
& *x^m*x^n*e^m + 12*A*a*c*d*m^2*x*x^m*x^n*e^m + 27*B*a*c^2*m*n*x*x^m*x^n*e^m \\
& + 27*A*b*c^2*m*n*x*x^m*x^n*e^m + 54*A*a*c*d*m*n*x*x^m*x^n*e^m + 26*B*a*c^2*n^2 \\
& n^2*x*x^m*x^n*e^m + 26*A*b*c^2*n^2*x*x^m*x^n*e^m + 52*A*a*c*d*n^2*x*x^m*x^n \\
& *e^m + 6*A*a*c^2*m^2*x*x^m*e^m + 30*A*a*c^2*m*n*x*x^m*e^m + 35*A*a*c^2*n^2*x \\
& x*x^m*e^m + 4*B*b*d^2*m*x*x^m*x^{(4*n)}*e^m + 6*B*b*d^2*n*x*x^m*x^{(4*n)}*e^m + \\
& 8*B*b*c*d*m*x*x^m*x^{(3*n)}*e^m + 4*B*a*d^2*m*x*x^m*x^{(3*n)}*e^m + 4*A*b*d^2*m \\
& *x*x^m*x^{(3*n)}*e^m + 14*B*b*c*d*n*x*x^m*x^{(3*n)}*e^m + 7*B*a*d^2*n*x*x^m*x^{(3*n)} \\
& *e^m + 7*A*b*d^2*n*x*x^m*x^{(3*n)}*e^m + 4*B*b*c^2*m*x*x^m*x^{(2*n)}*e^m + \\
& 8*B*a*c*d*m*x*x^m*x^{(2*n)}*e^m + 8*A*b*c*d*m*x*x^m*x^{(2*n)}*e^m + 4*A*a*d^2*m \\
& *x*x^m*x^{(2*n)}*e^m + 8*B*b*c^2*n*x*x^m*x^{(2*n)}*e^m + 16*B*a*c*d*n*x*x^m*x^{(2*n)} \\
& *e^m + 16*A*b*c*d*n*x*x^m*x^{(2*n)}*e^m + 8*A*a*d^2*n*x*x^m*x^{(2*n)}*e^m \\
& + 4*B*a*c^2*m*x*x^m*x^n*e^m + 4*A*b*c^2*m*x*x^m*x^n*e^m + 8*A*a*c*d*m*x*x^m \\
& *x^n*e^m + 9*B*a*c^2*n*x*x^m*x^n*e^m + 9*A*b*c^2*n*x*x^m*x^n*e^m + 18*A*a*c \\
& *d*n*x*x^m*x^n*e^m + 4*A*a*c^2*m*x*x^m*e^m + 10*A*a*c^2*n*x*x^m*e^m + B*b*d \\
& ^2*x*x^m*x^{(4*n)}*e^m + 2*B*b*c*d*x*x^m*x^{(3*n)}*e^m + B*a*d^2*x*x^m*x^{(3*n)} \\
& *e^m + A*b*d^2*x*x^m*x^{(3*n)}*e^m + B*b*c^2*x*x^m*x^{(2*n)}*e^m + 2*B*a*c*d*x*x \\
& ^m*x^{(2*n)}*e^m + 2*A*b*c*d*x*x^m*x^{(2*n)}*e^m + A*a*d^2*x*x^m*x^{(2*n)}*e^m + \\
& B*a*c^2*x*x^m*x^n*e^m + A*b*c^2*x*x^m*x^n*e^m + 2*A*a*c*d*x*x^m*x^n*e^m + A \\
& *a*c^2*x*x^m*e^m)/(m^5 + 10*m^4*n + 35*m^3*n^2 + 50*m^2*n^3 + 24*m*n^4 + 5* \\
& m^4 + 40*m^3*n + 105*m^2*n^2 + 100*m*n^3 + 24*n^4 + 10*m^3 + 60*m^2*n + 105 \\
& *m*n^2 + 50*n^3 + 10*m^2 + 40*m*n + 35*n^2 + 5*m + 10*n + 1)
\end{aligned}$$

**maple [C]** time = 0.14, size = 2410, normalized size = 15.06

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(b*x^n+a)*(B*x^n+A)*(d*x^n+c)^2,x)$

[Out]  $x*(28*A*b*d^2*m*n^2*(x^n)^3+18*B*b*d^2*m^2*n*(x^n)^4+22*B*b*d^2*m*n^2*(x^n)^4+8*A*a*d^2*m^3*n*(x^n)^2+2*B*a*c*d*m^4*(x^n)^2+21*B*a*d^2*m^2*n*(x^n)^3+28*B*a*d^2*m*n^2*(x^n)^3+8*B*b*c^2*m^3*n*(x^n)^2+19*B*b*c^2*m^2*n^2*(x^n)^2+12*B*b*c^2*m*n^3*(x^n)^2+8*B*b*c*d*m^3*(x^n)^3+16*B*b*c*d*n^3*(x^n)^3+18*B*b*d^2*m*n*(x^n)^4+21*A*b*d^2*m^2*n*(x^n)^3+24*A*a*d^2*m^2*n*(x^n)^2+38*A*a*d^2*m*n^2*(x^n)^2+9*A*b*c^2*m^3*n*x^n+26*A*b*c^2*m^2*n^2*x^n+24*A*b*c^2*m*n^3*x^n+8*A*b*c*d*m^3*(x^n)^2+24*A*b*c*d*n^3*(x^n)^2+21*A*b*d^2*m*n*(x^n)^3+9*B*a*c^2*m^3*n*x^n+26*B*a*c^2*m^2*n^2*x^n+24*B*a*c^2*m*n^3*x^n+8*A*a*c*d*m^3*x^n+48*A*a*c*d*n^3*x^n+24*A*a*d^2*m*n*(x^n)^2+27*A*b*c^2*m^2*n*x^n+52*A*b*c^2*m*n^2*x^n+8*B*a*c*d*m^3*(x^n)^2+24*B*a*c*d*n^3*(x^n)^2+21*B*a*d^2*m*n*(x^n)^3+24*B*b*c^2*m^2*n*(x^n)^2+38*B*b*c^2*m*n^2*(x^n)^2+12*B*b*c*d*m^2*(x^n)^3+2*A*a*c*d*m^4*x^n+8*B*b*c*d*(x^n)^3+m+14*B*b*c*d*(x^n)^3+n+12*A*b*c*d*m^2*(x^n)^2+38*A*b*c*d*n^2*(x^n)^2+27*B*a*c^2*m^2*n*x^n+52*B*a*c^2*m*n^2*x^n+12*B*a*c*d*m^2*(x^n)^2+38*B*a*c*d*n^2*(x^n)^2+24*B*b*c^2*m*n*(x^n)^2+28*B*b*c*d*n^2*(x^n)^3+16*B*a*c*d*(x^n)^2*n+8*A*a*c*d*x^n*m+18*A*a*c*d*x^n*n+12*A*a*c*d*m^2*x^n+52*A*a*c*d*n^2*x^n+27*A*b*c^2*m*n*x^n+8*A*b*c*d*(x^n)^2*m+16*A*b*c*d*(x^n)^2*n+27*B*a*c^2*m*n*x^n+8*B*a*c*d*(x^n)^2*m+B*b*c^2*(x^n)^2+A*b*c^2*x^n+B*a*c^2*x^n+b*B*d^2*(x^n)^4+A*b*d^2*(x^n)^3+B*a*d^2*(x^n)^3+A*a*d^2*(x^n)^2+a*A*c^2+6*A*a*c^2*m^2+35*A*a*c^2*n^2+A*a*c^2*m^4+4*A*a*c^2*m^3+50*A*a*c^2*n^3+24*A*a*c^2*n^4+4*A*a*c^2*m+10*A*a*c^2*n+38*A*b*c*d*m^2*n^2*(x^n)^2+24*A*b*c*d*m*n^3*(x^n)^2+16*B*a*c*d*m^3*n*(x^n)^2+24*B*a*c*d*m*n^3*(x^n)^2+42*B*b*c*d*m^2*n*(x^n)^3+56*B*b*c*d*m*n^2*(x^n)^3+18*A*a*c*d*m^3*n*x^n+52*A*a*c*d*m^2*n^2*x^n+48*A*a*c*d*m*n^3*x^n+4*B*a*d^2*m^3*(x^n)^3+38*B*a*c*d*m^2*n^2*(x^n)^2+48*B*a*c*d*m*n*(x^n)^2+54*A*a*c*d*m*n*x^n+16*B*b*c*d*m*n^3*(x^n)^3+16*A*b*c*d*m^3*n*(x^n)^2+42*B*b*c*d*m*n*(x^n)^3+54*A*a*c*d*m^2*n*x^n+104*A*a*c*d*m*n^2*x^n+14*B*b*c*d*m^3*n*(x^n)^3+28*B*b*c*d*m^2*n^2*(x^n)^3+48*A*b*c*d*m^2*n*(x^n)^2+76*A*b*c*d*m*n^2*(x^n)^2+48*B*a*c*d*m^2*n*(x^n)^2+76*B*a*c*d*m*n^2*(x^n)^2+48*A*b*c*d*m*n*(x^n)^2+14*A*b*d^2*n^2*(x^n)^3+B*a*c^2*m^4*x^n+6*B*a*d^2*m^2*(x^n)^3+14*B*a*d^2*n^2*(x^n)^3+4*B*b*c^$

$$2*m^3*(x^n)^2+12*B*b*c^2*n^3*(x^n)^2+4*m*b*B*d^2*(x^n)^4+6*b*B*d^2*(x^n)^4+n+8*B*a*d^2*m*n^3*(x^n)^3+2*B*b*c*d*m^4*(x^n)^3+14*A*b*d^2*m^2*n^2*(x^n)^3+7*A*b*d^2*m^3*n*(x^n)^3+6*B*b*d^2*m*n^3*(x^n)^4+6*B*b*d^2*m^3*n*(x^n)^4+11*B*b*d^2*m^2*n^2*(x^n)^4+19*A*a*d^2*m^2*n^2*(x^n)^2+12*A*a*d^2*m*n^3*(x^n)^2+2*A*b*c*d*m^4*(x^n)^2+8*A*b*d^2*m*n^3*(x^n)^3+7*B*a*d^2*m^3*n*(x^n)^3+14*B*a*d^2*m^2*n^2*(x^n)^3+8*B*a*d^2*n^3*(x^n)^3+6*A*b*c^2*m^2*x^n+26*A*b*c^2*n^2*x^n+6*B*b*c^2*m^2*(x^n)^2+19*B*b*c^2*n^2*(x^n)^2+4*A*a*d^2*(x^n)^2+m+8*A*a*d^2*(x^n)^2+n+70*A*a*c^2*m*n^2+30*A*a*c^2*m*n+2*(x^n)^3*b*B*c*d+2*(x^n)^2*B*a*c*d+2*x^n*a*A*c*d+2*(x^n)^2*A*b*c*d+10*A*a*c^2*m^3*n+35*A*a*c^2*m^2*n^2+50*A*a*c^2*m*n^3+30*A*a*c^2*m^2*n+11*B*b*d^2*n^2*(x^n)^4+4*A*a*d^2*m^3*(x^n)^2+12*A*a*d^2*n^3*(x^n)^2+A*b*c^2*m^4*x^n+6*A*b*d^2*m^2*(x^n)^3+B*b*c^2*m^4*(x^n)^2+6*B*b*d^2*m^2*(x^n)^4+24*A*b*c^2*n^3*x^n+4*A*b*d^2*(x^n)^3+m+7*A*b*d^2*(x^n)^3+n+4*B*a*c^2*m^3*x^n+24*B*a*c^2*n^3*x^n+4*B*a*d^2*(x^n)^3+m+7*B*a*d^2*(x^n)^3+n+8*A*b*d^2*n^3*(x^n)^3+B*b*d^2*m^4*(x^n)^4+A*b*d^2*m^4*(x^n)^3+B*a*d^2*m^4*(x^n)^3+4*B*b*d^2*m^3*(x^n)^4+6*B*b*d^2*n^3*(x^n)^4+A*a*d^2*m^4*(x^n)^2+4*A*b*d^2*m^3*(x^n)^3+4*A*b*c^2*x^n*m+9*A*b*c^2*x^n*n+4*B*a*c^2*x^n*m+9*B*a*c^2*x^n*n+6*A*a*d^2*m^2*(x^n)^2+19*A*a*d^2*n^2*(x^n)^2+4*A*b*c^2*m^3*x^n+4*B*b*c^2*(x^n)^2*m+8*B*b*c^2*(x^n)^2*n+6*B*a*c^2*m^2*x^n+26*B*a*c^2*n^2*x^n)/(m+1)/(m+n+1)/(m+2*n+1)/(m+3*n+1)/(m+4*n+1)*exp(1/2*(-I*Pi*csgn(I*e)*csgn(I*x)*csgn(I*e*x)+I*Pi*csgn(I*e)*csgn(I*e*x))^2+I*Pi*csgn(I*x)*csgn(I*e*x))^2-I*Pi*csgn(I*e*x))^3+2*ln(e)+2*ln(x))*m)$$

**maxima [B]** time = 0.78, size = 332, normalized size = 2.08

$$\frac{B*b*d^2*m^3*(x^n)^2+12*B*b*c^2*n^3*(x^n)^2+4*m*b*B*d^2*(x^n)^4+6*b*B*d^2*(x^n)^4+n+8*B*a*d^2*m*n^3*(x^n)^3+2*B*b*c*d*m^4*(x^n)^3+14*A*b*d^2*m^2*n^2*(x^n)^3+7*A*b*d^2*m^3*n*(x^n)^3+6*B*b*d^2*m*n^3*(x^n)^4+6*B*b*d^2*m^3*n*(x^n)^4+11*B*b*d^2*m^2*n^2*(x^n)^4+19*A*a*d^2*m^2*n^2*(x^n)^2+12*A*a*d^2*m*n^3*(x^n)^2+2*A*b*c*d*m^4*(x^n)^2+8*A*b*d^2*m*n^3*(x^n)^3+7*B*a*d^2*m^3*n*(x^n)^3+14*B*a*d^2*m^2*n^2*(x^n)^3+8*B*a*d^2*n^3*(x^n)^3+6*A*b*c^2*m^2*x^n+26*A*b*c^2*n^2*x^n+6*B*b*c^2*m^2*(x^n)^2+19*B*b*c^2*n^2*(x^n)^2+4*A*a*d^2*(x^n)^2+m+8*A*a*d^2*(x^n)^2+n+70*A*a*c^2*m*n^2+30*A*a*c^2*m*n+2*(x^n)^3*b*B*c*d+2*(x^n)^2*B*a*c*d+2*x^n*a*A*c*d+2*(x^n)^2*A*b*c*d+10*A*a*c^2*m^3*n+35*A*a*c^2*m^2*n^2+50*A*a*c^2*m*n^3+30*A*a*c^2*m^2*n+11*B*b*d^2*n^2*(x^n)^4+4*A*a*d^2*m^3*(x^n)^2+12*A*a*d^2*n^3*(x^n)^2+A*b*c^2*m^4*x^n+6*A*b*d^2*m^2*(x^n)^3+B*b*c^2*m^4*(x^n)^2+6*B*b*d^2*m^2*(x^n)^4+24*A*b*c^2*n^3*x^n+4*A*b*d^2*(x^n)^3+m+7*A*b*d^2*(x^n)^3+n+4*B*a*c^2*m^3*x^n+24*B*a*c^2*n^3*x^n+4*B*a*d^2*(x^n)^3+m+7*B*a*d^2*(x^n)^3+n+8*A*b*d^2*n^3*(x^n)^3+B*b*d^2*m^4*(x^n)^4+A*b*d^2*m^4*(x^n)^3+B*a*d^2*m^4*(x^n)^3+4*B*b*d^2*m^3*(x^n)^4+6*B*b*d^2*n^3*(x^n)^4+A*a*d^2*m^4*(x^n)^2+4*A*b*d^2*m^3*(x^n)^3+4*A*b*c^2*x^n*m+9*A*b*c^2*x^n*n+4*B*a*c^2*x^n*m+9*B*a*c^2*x^n*n+6*A*a*d^2*m^2*(x^n)^2+19*A*a*d^2*n^2*(x^n)^2+4*A*b*c^2*m^3*x^n+4*B*b*c^2*(x^n)^2*m+8*B*b*c^2*(x^n)^2*n+6*B*a*c^2*m^2*x^n+26*B*a*c^2*n^2*x^n}{(m+1)*(m+n+1)*(m+2*n+1)*(m+3*n+1)*(m+4*n+1)}*exp(1/2*(-I*Pi*csgn(I*e)*csgn(I*x)*csgn(I*e*x)+I*Pi*csgn(I*e)*csgn(I*e*x))^2+I*Pi*csgn(I*x)*csgn(I*e*x))^2-I*Pi*csgn(I*e*x))^3+2*ln(e)+2*ln(x))*m$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="maxima")

[Out] B\*b\*d^2\*e^m\*x\*e^(m\*log(x) + 4\*n\*log(x))/(m + 4\*n + 1) + 2\*B\*b\*c\*d\*e^m\*x\*e^(m\*log(x) + 3\*n\*log(x))/(m + 3\*n + 1) + B\*a\*d^2\*e^m\*x\*e^(m\*log(x) + 3\*n\*log(x))/(m + 3\*n + 1) + A\*b\*d^2\*e^m\*x\*e^(m\*log(x) + 3\*n\*log(x))/(m + 3\*n + 1) + B\*b\*c^2\*e^m\*x\*e^(m\*log(x) + 2\*n\*log(x))/(m + 2\*n + 1) + 2\*B\*a\*c\*d\*e^m\*x\*e^(m\*log(x) + 2\*n\*log(x))/(m + 2\*n + 1) + 2\*A\*b\*c\*d\*e^m\*x\*e^(m\*log(x) + 2\*n\*log(x))/(m + 2\*n + 1) + A\*a\*d^2\*e^m\*x\*e^(m\*log(x) + 2\*n\*log(x))/(m + 2\*n + 1) + B\*a\*c^2\*e^m\*x\*e^(m\*log(x) + n\*log(x))/(m + n + 1) + A\*b\*c^2\*e^m\*x\*e^(m\*log(x) + n\*log(x))/(m + n + 1) + 2\*A\*a\*c\*d\*e^m\*x\*e^(m\*log(x) + n\*log(x))/(m + n + 1) + (e\*x)^(m + 1)\*A\*a\*c^2/(e\*(m + 1))

**mupad [B]** time = 5.20, size = 588, normalized size = 3.68

$$\frac{B*b*d^2*m^3*(x^n)^2+12*B*b*c^2*n^3*(x^n)^2+4*m*b*B*d^2*(x^n)^4+6*b*B*d^2*(x^n)^4+n+8*B*a*d^2*m*n^3*(x^n)^3+2*B*b*c*d*m^4*(x^n)^3+14*A*b*d^2*m^2*n^2*(x^n)^3+7*A*b*d^2*m^3*n*(x^n)^3+6*B*b*d^2*m*n^3*(x^n)^4+6*B*b*d^2*m^3*n*(x^n)^4+11*B*b*d^2*m^2*n^2*(x^n)^4+19*A*a*d^2*m^2*n^2*(x^n)^2+12*A*a*d^2*m*n^3*(x^n)^2+2*A*b*c*d*m^4*(x^n)^2+8*A*b*d^2*m*n^3*(x^n)^3+7*B*a*d^2*m^3*n*(x^n)^3+14*B*a*d^2*m^2*n^2*(x^n)^3+8*B*a*d^2*n^3*(x^n)^3+6*A*b*c^2*m^2*x^n+26*A*b*c^2*n^2*x^n+6*B*b*c^2*m^2*(x^n)^2+19*B*b*c^2*n^2*(x^n)^2+4*A*a*d^2*(x^n)^2+m+8*A*a*d^2*(x^n)^2+n+70*A*a*c^2*m*n^2+30*A*a*c^2*m*n+2*(x^n)^3*b*B*c*d+2*(x^n)^2*B*a*c*d+2*x^n*a*A*c*d+2*(x^n)^2*A*b*c*d+10*A*a*c^2*m^3*n+35*A*a*c^2*m^2*n^2+50*A*a*c^2*m*n^3+30*A*a*c^2*m^2*n+11*B*b*d^2*n^2*(x^n)^4+4*A*a*d^2*m^3*(x^n)^2+12*A*a*d^2*n^3*(x^n)^2+A*b*c^2*m^4*x^n+6*A*b*d^2*m^2*(x^n)^3+B*b*c^2*m^4*(x^n)^2+6*B*b*d^2*m^2*(x^n)^4+24*A*b*c^2*n^3*x^n+4*A*b*d^2*(x^n)^3+m+7*A*b*d^2*(x^n)^3+n+4*B*a*c^2*m^3*x^n+24*B*a*c^2*n^3*x^n+4*B*a*d^2*(x^n)^3+m+7*B*a*d^2*(x^n)^3+n+8*A*b*d^2*n^3*(x^n)^3+B*b*d^2*m^4*(x^n)^4+A*b*d^2*m^4*(x^n)^3+B*a*d^2*m^4*(x^n)^3+4*B*b*d^2*m^3*(x^n)^4+6*B*b*d^2*n^3*(x^n)^4+A*a*d^2*m^4*(x^n)^2+4*A*b*d^2*m^3*(x^n)^3+4*A*b*c^2*x^n*m+9*A*b*c^2*x^n*n+4*B*a*c^2*x^n*m+9*B*a*c^2*x^n*n+6*A*a*d^2*m^2*(x^n)^2+19*A*a*d^2*n^2*(x^n)^2+4*A*b*c^2*m^3*x^n+4*B*b*c^2*(x^n)^2*m+8*B*b*c^2*(x^n)^2*n+6*B*a*c^2*m^2*x^n+26*B*a*c^2*n^2*x^n}{(m+1)*(m+n+1)*(m+2*n+1)*(m+3*n+1)*(m+4*n+1)}*exp(1/2*(-I*Pi*csgn(I*e)*csgn(I*x)*csgn(I*e*x)+I*Pi*csgn(I*e)*csgn(I*e*x))^2+I*Pi*csgn(I*x)*csgn(I*e*x))^2-I*Pi*csgn(I*e*x))^3+2*ln(e)+2*ln(x))*m$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)\*(c + d\*x^n)^2,x)

[Out] (x\*x^(2\*n))\*(e\*x)^m\*(A\*a\*d^2 + B\*b\*c^2 + 2\*A\*b\*c\*d + 2\*B\*a\*c\*d)\*(3\*m + 8\*n + 16\*m\*n + 19\*m\*n^2 + 8\*m^2\*n + 3\*m^2 + m^3 + 19\*n^2 + 12\*n^3 + 1)/(4\*m + 10\*n + 30\*m\*n + 70\*m\*n^2 + 30\*m^2\*n + 50\*m\*n^3 + 10\*m^3\*n + 6\*m^2 + 4\*m^3 + m^4 + 35\*n^2 + 50\*n^3 + 24\*n^4 + 35\*m^2\*n^2 + 1) + (A\*a\*c^2\*x\*(e\*x)^m)/(m + 1) + (c\*x\*x^n\*(e\*x)^m\*(2\*A\*a\*d + A\*b\*c + B\*a\*c)\*(3\*m + 9\*n + 18\*m\*n + 26\*m\*n^2 + 9\*m^2\*n + 3\*m^2 + m^3 + 26\*n^2 + 24\*n^3 + 1))/(4\*m + 10\*n + 30\*m\*n + 70\*m\*n^2 + 30\*m^2\*n + 50\*m\*n^3 + 10\*m^3\*n + 6\*m^2 + 4\*m^3 + m^4 + 35\*n^2 + 50\*n^3 + 24\*n^4 + 35\*m^2\*n^2 + 1) + (d\*x\*x^n\*(3\*n)\*(e\*x)^m\*(A\*b\*d + B\*a\*d + 2\*B\*b\*c)\*(3\*m + 7\*n + 14\*m\*n + 14\*m\*n^2 + 7\*m^2\*n + 3\*m^2 + m^3 + 14\*n^2 + 8\*n^3 + 1))/(4\*m + 10\*n + 30\*m\*n + 70\*m\*n^2 + 30\*m^2\*n + 50\*m\*n^3 + 10\*m^3\*n + 6\*m^2 + 4\*m^3 + m^4 + 35\*n^2 + 50\*n^3 + 24\*n^4 + 35\*m^2\*n^2 + 1) + (B\*b\*d^2\*x\*x^(4\*n)\*(e\*x)^m\*(3\*m + 6\*n + 12\*m\*n + 11\*m\*n^2 + 6\*m^2\*n + 3\*m^2 + m^3 + 11\*n^2 + 6\*n^3 + 1))/(4\*m + 10\*n + 30\*m\*n + 70\*m\*n^2 + 30\*m^2\*n + 50\*m

```
*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n  
^2 + 1)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(a+b*x**n)*(A+B*x**n)*(c+d*x**n)**2,x)
```

```
[Out] Timed out
```

### 3.8 $\int (ex)^m (A + Bx^n) (c + dx^n)^2 dx$

**Optimal.** Leaf size=102

$$\frac{cx^{n+1}(ex)^m(2Ad + Bc)}{m + n + 1} + \frac{dx^{2n+1}(ex)^m(Ad + 2Bc)}{m + 2n + 1} + \frac{Ac^2(ex)^{m+1}}{e(m + 1)} + \frac{Bd^2x^{3n+1}(ex)^m}{m + 3n + 1}$$

**Rubi [A]** time = 0.08, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 3, integrand size = 22,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$ , Rules used = {448, 20, 30}

$$\frac{cx^{n+1}(ex)^m(2Ad + Bc)}{m + n + 1} + \frac{dx^{2n+1}(ex)^m(Ad + 2Bc)}{m + 2n + 1} + \frac{Ac^2(ex)^{m+1}}{e(m + 1)} + \frac{Bd^2x^{3n+1}(ex)^m}{m + 3n + 1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] (c\*(B\*c + 2\*A\*d)\*x^(1 + n)\*(e\*x)^m)/(1 + m + n) + (d\*(2\*B\*c + A\*d)\*x^(1 + 2\*n)\*(e\*x)^m)/(1 + m + 2\*n) + (B\*d^2\*x^(1 + 3\*n)\*(e\*x)^m)/(1 + m + 3\*n) + (A\*c^2\*(e\*x)^(1 + m))/(e\*(1 + m))

#### Rule 20

Int[(u\_.)\*((a\_.)\*(v\_))^(m\_.)\*((b\_.)\*(v\_))^(n\_.), x\_Symbol] :> Dist[(b^IntPart[n]\*(b\*v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m + n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

#### Rule 30

Int[(x\_)^(m\_.), x\_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

#### Rule 448

Int[((e\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_))^(q\_.), x\_Symbol] :> Int[ExpandIntegrand[(e\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[b\*c - a\*d, 0] && IGtQ[p, 0] && IGtQ[q, 0]

#### Rubi steps

$$\begin{aligned} \int (ex)^m (A + Bx^n) (c + dx^n)^2 dx &= \int (Ac^2(ex)^m + c(Bc + 2Ad)x^n(ex)^m + d(2Bc + Ad)x^{2n}(ex)^m + Bd^2x^{3n}(ex)^m) dx \\ &= \frac{Ac^2(ex)^{1+m}}{e(1+m)} + (Bd^2) \int x^{3n}(ex)^m dx + (d(2Bc + Ad)) \int x^{2n}(ex)^m dx + (c(Bc + 2Ad)) \int x^n(ex)^m dx \\ &= \frac{Ac^2(ex)^{1+m}}{e(1+m)} + (Bd^2x^{-m}(ex)^m) \int x^{m+3n} dx + (d(2Bc + Ad)x^{-m}(ex)^m) \int x^{m+2n} dx + (c(Bc + 2Ad)x^{-m}(ex)^m) \int x^{m+n} dx \\ &= \frac{c(Bc + 2Ad)x^{1+n}(ex)^m}{1+m+n} + \frac{d(2Bc + Ad)x^{1+2n}(ex)^m}{1+m+2n} + \frac{Bd^2x^{1+3n}(ex)^m}{1+m+3n} + \frac{Ac^2(ex)^{1+m}}{e(1+m)} \end{aligned}$$

**Mathematica [A]** time = 0.18, size = 78, normalized size = 0.76

$$x(ex)^m \left( \frac{dx^{2n}(Ad + 2Bc)}{m + 2n + 1} + \frac{cx^n(2Ad + Bc)}{m + n + 1} + \frac{Ac^2}{m + 1} + \frac{Bd^2x^{3n}}{m + 3n + 1} \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(e*x)^m*(A + B*x^n)*(c + d*x^n)^2,x]
```

```
[Out] x*(e*x)^m*((A*c^2)/(1 + m) + (c*(B*c + 2*A*d)*x^n)/(1 + m + n) + (d*(2*B*c + A*d)*x^(2*n))/(1 + m + 2*n) + (B*d^2*x^(3*n))/(1 + m + 3*n))
```

**IntegrateAlgebraic** [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (ex)^m (A + Bx^n)(c + dx^n)^2 dx$$

Verification is not applicable to the result.

```
[In] IntegrateAlgebraic[(e*x)^m*(A + B*x^n)*(c + d*x^n)^2,x]
```

```
[Out] Defer[IntegrateAlgebraic] [(e*x)^m*(A + B*x^n)*(c + d*x^n)^2, x]
```

**fricas** [B] time = 0.45, size = 527, normalized size = 5.17

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^2,x, algorithm="fricas")
```

```
[Out] ((B*d^2*m^3 + 3*B*d^2*m^2 + 3*B*d^2*m + B*d^2 + 2*(B*d^2*m + B*d^2)*n^2 + 3*(B*d^2*m^2 + 2*B*d^2*m + B*d^2)*n)*x*x^(3*n)*e^(m*log(e) + m*log(x)) + ((2*B*c*d + A*d^2)*m^3 + 2*B*c*d + A*d^2 + 3*(2*B*c*d + A*d^2)*m^2 + 3*(2*B*c*d + A*d^2 + (2*B*c*d + A*d^2)*m)*n^2 + 3*(2*B*c*d + A*d^2)*m + 4*(2*B*c*d + A*d^2 + (2*B*c*d + A*d^2)*m^2 + 2*(2*B*c*d + A*d^2)*m)*n)*x*x^(2*n)*e^(m*log(e) + m*log(x)) + ((B*c^2 + 2*A*c*d)*m^3 + B*c^2 + 2*A*c*d + 3*(B*c^2 + 2*A*c*d)*m^2 + 6*(B*c^2 + 2*A*c*d + (B*c^2 + 2*A*c*d)*m)*n^2 + 3*(B*c^2 + 2*A*c*d)*m + 5*(B*c^2 + 2*A*c*d + (B*c^2 + 2*A*c*d)*m^2 + 2*(B*c^2 + 2*A*c*d)*m)*n)*x*x^n*e^(m*log(e) + m*log(x)) + (A*c^2*m^3 + 6*A*c^2*n^3 + 3*A*c^2*m^2 + 3*A*c^2*m + A*c^2 + 11*(A*c^2*m + A*c^2)*n^2 + 6*(A*c^2*m^2 + 2*A*c^2*m + A*c^2)*n)*x*e^(m*log(e) + m*log(x))/(m^4 + 6*(m + 1)*n^3 + 4*m^3 + 11*(m^2 + 2*m + 1)*n^2 + 6*m^2 + 6*(m^3 + 3*m^2 + 3*m + 1)*n + 4*m + 1)
```

**giac** [B] time = 0.58, size = 1023, normalized size = 10.03

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^2,x, algorithm="giac")
```

```
[Out] (B*d^2*m^3*x*x^m*x^(3*n)*e^m + 3*B*d^2*m^2*n*x*x^m*x^(3*n)*e^m + 2*B*d^2*m*n^2*x*x^m*x^(3*n)*e^m + 2*B*c*d*m^3*x*x^m*x^(2*n)*e^m + A*d^2*m^3*x*x^m*x^(2*n)*e^m + 8*B*c*d*m^2*n*x*x^m*x^(2*n)*e^m + 4*A*d^2*m^2*n*x*x^m*x^(2*n)*e^m + 6*B*c*d*m*n^2*x*x^m*x^(2*n)*e^m + 3*A*d^2*m*n^2*x*x^m*x^(2*n)*e^m + B*c^2*m^3*x*x^m*x^n*e^m + 2*A*c*d*m^3*x*x^m*x^n*e^m + 5*B*c^2*m^2*n*x*x^m*x^n*e^m + 10*A*c*d*m^2*n*x*x^m*x^n*e^m + 6*B*c^2*m*n^2*x*x^m*x^n*e^m + 12*A*c*d*m*n^2*x*x^m*x^n*e^m + A*c^2*m^3*x*x^m*e^m + 6*A*c^2*m^2*n*x*x^m*e^m + 11*A*c^2*m*n^2*x*x^m*e^m + 6*A*c^2*n^3*x*x^m*e^m + 3*B*d^2*m^2*x*x^m*x^(3*n)*e^m + 6*B*d^2*m*n*x*x^m*x^(3*n)*e^m + 2*B*d^2*n^2*x*x^m*x^(3*n)*e^m + 6*B*c*d*m^2*x*x^m*x^(2*n)*e^m + 3*A*d^2*m^2*x*x^m*x^(2*n)*e^m + 16*B*c*d*m*n*x*x^m*x^(2*n)*e^m + 8*A*d^2*m*n*x*x^m*x^(2*n)*e^m + 6*B*c*d*n^2*x*x^m*x^(2*n)*e^m + 3*A*d^2*n^2*x*x^m*x^(2*n)*e^m + 3*B*c^2*m^2*x*x^m*x^n*e^m + 6*A*c*d*m^2*x*x^m*x^n*e^m + 10*B*c^2*m*n*x*x^m*x^n*e^m + 20*A*c*d*m*n*x*x^m*x^n*e^m + 6*B*c^2*n^2*x*x^m*x^n*e^m + 12*A*c*d*n^2*x*x^m*x^n*e^m + 3*A*c^2*m^2*x*x^m*e^m + 12*A*c^2*m*n*x*x^m*e^m + 11*A*c^2*n^2*x*x^m*e^m + 3*B*d^2*m*x*x^m*x^(3*n)*e^m + 3*B*d^2*n*x*x^m*x^(3*n)*e^m + 6*B*c*d*m*x*x^m*x^(2*n)*e^m + 3*A
```



$$\frac{d^2 m^2 x^2 e^{m x} + 8 B^2 c^2 d^2 n^2 x^2 e^{m x} + 4 A^2 d^2 n^2 x^2 e^{m x} + 2 m^2 x^2 e^{m x} + 3 B^2 c^2 m^2 x^2 e^{m x} + 6 A^2 c^2 d^2 m^2 x^2 e^{m x} + 5 B^2 c^2 n^2 x^2 e^{m x} + 10 A^2 c^2 d^2 n^2 x^2 e^{m x} + 3 A^2 c^2 m^2 x^2 e^{m x} + 6 A^2 c^2 n^2 x^2 e^{m x} + B^2 d^2 x^2 e^{m x} + 2 B^2 c^2 d^2 x^2 e^{m x} + A^2 d^2 x^2 e^{m x} + B^2 c^2 x^2 e^{m x} + 2 A^2 c^2 d^2 x^2 e^{m x} + A^2 c^2 x^2 e^{m x}}{(m^4 + 6 m^3 n + 11 m^2 n^2 + 6 m n^3 + 4 m^3 + 18 m^2 n + 22 m n^2 + 6 n^3 + 6 m^2 + 18 m n + 11 n^2 + 4 m + 6 n + 1)}$$

**maple [C]** time = 0.11, size = 732, normalized size = 7.18

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(B\*x^n+A)\*(d\*x^n+c)^2,x)

[Out]  $x(2B^2cd^3m^3(x^n)^2+6B^2d^2m^2n(x^n)^3+2B^2d^2n^2(x^n)^3+A^2d^2m^3(x^n)^2+3B^2d^2m^2(x^n)^3+B^2d^2m^3(x^n)^3+B^2c^2m^3x^n+3A^2d^2(x^n)^2m+3A^2d^2m^2(x^n)^2+3A^2d^2n^2(x^n)^2+3m^2B^2d^2(x^n)^3+3B^2d^2(x^n)^3n+2B^2cd(x^n)^2+2A^2cdx^n+3B^2c^2m^2x^n+6B^2c^2n^2x^n+3B^2c^2x^nm+5B^2c^2x^nn+4A^2d^2(x^n)^2n+6A^2c^2m^2n+11A^2c^2m^2n^2+12A^2c^2m^2n+A^2c^2+6B^2cdm^2n(x^n)^2+10A^2cdm^2n^2x^n+12A^2cdm^2n^2x^n+16B^2cdm^2n(x^n)^2+20A^2cdm^2n^2x^n+8B^2cdm^2n(x^n)^2+6A^2cdm^2x^n+12A^2cdm^2n^2x^n+10B^2c^2m^2n^2x^n+6B^2cd(x^n)^2m+8B^2cd(x^n)^2n+6A^2cdx^nm+10A^2cdx^nn+3B^2d^2m^2n(x^n)^3+2B^2d^2m^2n(x^n)^3+3A^2c^2m+6A^2c^2n+6A^2c^2n^3+3A^2c^2m^2+11A^2c^2n^2+x^nB^2c^2+(x^n)^3B^2d^2+A^2c^2m^3+(x^n)^2A^2d^2+4A^2d^2m^2n(x^n)^2+3A^2d^2m^2n(x^n)^2+2A^2cdm^3x^n+8A^2d^2m^2n(x^n)^2+5B^2c^2m^2n^2x^n+6B^2c^2m^2n^2x^n+6B^2cdm^2(x^n)^2+6B^2cdn^2(x^n)^2)/(m+1)/(m+n+1)/(m+2n+1)/(m+3n+1)*exp(1/2*(-I*Pi*csgn(I*e)*csgn(I*x)*csgn(I*e*x)+I*Pi*csgn(I*e)*csgn(I*e*x)^2+I*Pi*csgn(I*x)*csgn(I*e*x)^2-I*Pi*csgn(I*e*x)^3+2*ln(e)+2*ln(x))*m)$

**maxima [A]** time = 0.63, size = 155, normalized size = 1.52

$$\frac{Bd^2e^{mx}xe^{(m\log(x)+3n\log(x))}}{m+3n+1} + \frac{2Bcde^{mx}xe^{(m\log(x)+2n\log(x))}}{m+2n+1} + \frac{Ad^2e^{mx}xe^{(m\log(x)+2n\log(x))}}{m+2n+1} + \frac{Bc^2e^{mx}xe^{(m\log(x)+n\log(x))}}{m+n+1} + \frac{2Acde^{mx}xe^{(m\log(x)+n\log(x))}}{m+n+1} + \frac{(ex)^{m+1}Ac^2}{e(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="maxima")

[Out]  $B^2d^2e^{mx}xe^{(m\log(x)+3n\log(x))}/(m+3n+1) + 2B^2cd^2e^{mx}xe^{(m\log(x)+2n\log(x))}/(m+2n+1) + A^2d^2e^{mx}xe^{(m\log(x)+2n\log(x))}/(m+2n+1) + B^2c^2e^{mx}xe^{(m\log(x)+n\log(x))}/(m+n+1) + 2A^2cd^2e^{mx}xe^{(m\log(x)+n\log(x))}/(m+n+1) + (e*x)^{m+1}A^2c^2/(e*(m+1))$

**mupad [B]** time = 5.11, size = 265, normalized size = 2.60

$$\frac{Ac^2x(ex)^m}{m+1} + \frac{c^2xx^3(ex)^m(2Ad+Bc)(m^2+5mn+2m+6n^2+5n+1)}{m^3+6m^2n+3m^2+11mn^2+12mn+3m+6n^3+11n^2+6n+1} + \frac{d^2xx^2(ex)^m(Ad+2Bc)(m^2+4mn+2m+3n^2+4n+1)}{m^3+6m^2n+3m^2+11mn^2+12mn+3m+6n^3+11n^2+6n+1} + \frac{Bd^2x^3(ex)^m(m^2+3mn+2m+2n^2+3n+1)}{m^3+6m^2n+3m^2+11mn^2+12mn+3m+6n^3+11n^2+6n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2,x)

[Out]  $(A^2c^2x^2(e*x)^m)/(m+1) + (c^2x^3(e*x)^m(2Ad+Bc)(2m+5n+5m^2n+m^2+6n^2+1))/(3m+6n+12m^2n+11m^2n^2+6m^2n+3m^2+m^3+11n^2+6n^3+1) + (d^2x^2(e*x)^m(A^2d+2B^2c)(2m+4n+4m^2n+m^2+3n^2+1))/(3m+6n+12m^2n+11m^2n^2+6m^2n+3m^2+m^3+11n^2+6n^3+1) + (B^2d^2x^3(e*x)^m(2m+3n+3m^2n+m^2+2n^2+1))/(3m+6n+12m^2n+11m^2n^2+6m^2n+3m^2+m^3+11n^2+6n^3+1)$

**sympy [A]** time = 74.16, size = 6399, normalized size = 62.74

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(A+B*x**n)*(c+d*x**n)**2,x)
```

```
[Out] Piecewise(((A + B)*(c + d)**2*log(x)/e, Eq(m, -1) & Eq(n, 0)), ((A*c**2*log
(x) + 2*A*c*d*x**n/n + A*d**2*x**(2*n)/(2*n) + B*c**2*x**n/n + B*c*d*x**(2*
n)/n + B*d**2*x**(3*n)/(3*n))/e, Eq(m, -1)), (A*c**2*Piecewise((log(x), Eq(
n, 0)), (-x**(-3*n)*(0**(1/n))**(-3*n)/(3*n), Eq(e, 0**(1/n))), (-e**(-3*n)
*x**(-3*n)/(3*n), True))/e + 2*A*c*d*Piecewise((log(x), Eq(n, 0)), (-x**n/(
3*0**(1/n)*zoo**(1/n)*n*x**(3*n)*(0**(1/n))**3*n) - n*x**(3*n)*(0**(1/n))
*(3*n)), Eq(e, 0**(1/n))), (-e**(-3*n)*x**(-2*n)/(2*n), True))/e + A*d**2*P
iecewise((log(x), Eq(n, 0)), (-x**(2*n)/(3*0**(1/n)*zoo**(1/n)*n*x**(3*n)*
(0**(1/n))**3*n) - 2*n*x**(3*n)*(0**(1/n))**3*n), Eq(e, 0**(1/n))), (-e**
(-3*n)*x**(-n)/n, True))/e + B*c**2*Piecewise((log(x), Eq(n, 0)), (-x**n/(3
*0**(1/n)*zoo**(1/n)*n*x**(3*n)*(0**(1/n))**3*n) - n*x**(3*n)*(0**(1/n))
*(3*n)), Eq(e, 0**(1/n))), (-e**(-3*n)*x**(-2*n)/(2*n), True))/e + 2*B*c*d*P
iecewise((log(x), Eq(n, 0)), (-x**(2*n)/(3*0**(1/n)*zoo**(1/n)*n*x**(3*n)*
(0**(1/n))**3*n) - 2*n*x**(3*n)*(0**(1/n))**3*n), Eq(e, 0**(1/n))), (-e**
(-3*n)*x**(-n)/n, True))/e + B*d**2*Piecewise((e**(-3*n)*log(x), Abs(x) < 1
), (-e**(-3*n)*log(1/x), 1/Abs(x) < 1), (-e**(-3*n)*meijerg(((), (1, 1)), (
(0, 0), ()), x) + e**(-3*n)*meijerg(((1, 1), ()), ((), (0, 0)), x), True))/
e, Eq(m, -3*n - 1)), (A*c**2*Piecewise((log(x), Eq(n, 0)), (-x**(-2*n)*(0**
(1/n))**(-2*n)/(2*n), Eq(e, 0**(1/n))), (-e**(-2*n)*x**(-2*n)/(2*n), True)
)/e + 2*A*c*d*Piecewise((log(x), Eq(n, 0)), (-x**n/(2*0**(1/n)*zoo**(1/n)*n
*x**(2*n)*(0**(1/n))**2*n) - n*x**(2*n)*(0**(1/n))**2*n), Eq(e, 0**(1/n)
)), (-e**(-2*n)*x**(-n)/n, True))/e + A*d**2*Piecewise((e**(-2*n)*log(x), Ab
s(x) < 1), (-e**(-2*n)*log(1/x), 1/Abs(x) < 1), (-e**(-2*n)*meijerg(((), (1
, 1)), ((0, 0), ()), x) + e**(-2*n)*meijerg(((1, 1), ()), ((), (0, 0)), x),
True))/e + B*c**2*Piecewise((log(x), Eq(n, 0)), (-x**n/(2*0**(1/n)*zoo**(1
/n)*n*x**(2*n)*(0**(1/n))**2*n) - n*x**(2*n)*(0**(1/n))**2*n), Eq(e, 0**
(1/n))), (-e**(-2*n)*x**(-n)/n, True))/e + 2*B*c*d*Piecewise((e**(-2*n)*log
(x), Abs(x) < 1), (-e**(-2*n)*log(1/x), 1/Abs(x) < 1), (-e**(-2*n)*meijerg(
((), (1, 1)), ((0, 0), ()), x) + e**(-2*n)*meijerg(((1, 1), ()), ((), (0, 0
)), x), True))/e + B*d**2*Piecewise((log(x), Eq(n, 0)), (-x**(3*n)/(2*0**(1
/n)*zoo**(1/n)*n*x**(2*n)*(0**(1/n))**2*n) - 3*n*x**(2*n)*(0**(1/n))**2*n
)), Eq(e, 0**(1/n))), (e**(-2*n)*x**n/n, True))/e, Eq(m, -2*n - 1)), (A*c**
2*Piecewise((log(x), Eq(n, 0)), (-x**(-n)*(0**(1/n))**(-n)/n, Eq(e, 0**(1/n
))), (-e**(-n)*x**(-n)/n, True))/e + 2*A*c*d*Piecewise((e**(-n)*log(x), Abs
(x) < 1), (-e**(-n)*log(1/x), 1/Abs(x) < 1), (-e**(-n)*meijerg(((), (1, 1)
), ((0, 0), ()), x) + e**(-n)*meijerg(((1, 1), ()), ((), (0, 0)), x), True)
)/e + A*d**2*Piecewise((log(x), Eq(n, 0)), (-x**(2*n)/(0**(1/n)*zoo**(1/n)*n
*x**n*(0**(1/n))**n) - 2*n*x**n*(0**(1/n))**n), Eq(e, 0**(1/n))), (e**(-n)*x
**n/n, True))/e + B*c**2*Piecewise((e**(-n)*log(x), Abs(x) < 1), (-e**(-n)*
log(1/x), 1/Abs(x) < 1), (-e**(-n)*meijerg(((), (1, 1)), ((0, 0), ()), x) +
e**(-n)*meijerg(((1, 1), ()), ((), (0, 0)), x), True))/e + 2*B*c*d*Piecewi
se((log(x), Eq(n, 0)), (-x**(2*n)/(0**(1/n)*zoo**(1/n)*n*x**n*(0**(1/n))**n
- 2*n*x**n*(0**(1/n))**n), Eq(e, 0**(1/n))), (e**(-n)*x**n/n, True))/e + B
*d**2*Piecewise((log(x), Eq(n, 0)), (-x**(3*n)/(0**(1/n)*zoo**(1/n)*n*x**n*
(0**(1/n))**n) - 3*n*x**n*(0**(1/n))**n), Eq(e, 0**(1/n))), (e**(-n)*x**(2*n
)/(2*n), True))/e, Eq(m, -n - 1)), (A*c**2*e**m*m**3*x*x**m/(m**4 + 6*m**3*
n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*
m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 6*A*c**2*e**m*m**2*n*x*x**m/(m**4
+ 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*
n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*A*c**2*e**m*m**2*x*x*
*m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3
+ 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 11*A*c**2*e**m*
m*n**2*x*x**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2
+ 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 12*A
```

$$\begin{aligned}
& *c**2*e**m*m*n*x*x**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n \\
& + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1 \\
& ) + 3*A*c**2*e**m*m*x*x**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m* \\
& *2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6* \\
& n + 1) + 6*A*c**2*e**m*n**3*x*x**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 \\
& + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n \\
& **2 + 6*n + 1) + 11*A*c**2*e**m*n**2*x*x**m/(m**4 + 6*m**3*n + 4*m**3 + 11* \\
& m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n* \\
& *3 + 11*n**2 + 6*n + 1) + 6*A*c**2*e**m*n*x*x**m/(m**4 + 6*m**3*n + 4*m**3 \\
& + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + \\
& 6*n**3 + 11*n**2 + 6*n + 1) + A*c**2*e**m*x*x**m/(m**4 + 6*m**3*n + 4*m**3 \\
& + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m \\
& + 6*n**3 + 11*n**2 + 6*n + 1) + 2*A*c*d*e**m*m**3*x*x**m*x**n/(m**4 + 6*m** \\
& 3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 1 \\
& 8*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 10*A*c*d*e**m*m**2*n*x*x**m*x** \\
& n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 \\
& + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 6*A*c*d*e**m*m** \\
& 2*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 \\
& + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 12*A \\
& *c*d*e**m*m*n**2*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18* \\
& m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + \\
& 6*n + 1) + 20*A*c*d*e**m*m*n*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m** \\
& 2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 \\
& + 11*n**2 + 6*n + 1) + 6*A*c*d*e**m*m*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 \\
& + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m \\
& + 6*n**3 + 11*n**2 + 6*n + 1) + 12*A*c*d*e**m*n**2*x*x**m*x**n/(m**4 + 6*m* \\
& **3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + \\
& 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 10*A*c*d*e**m*n*x*x**m*x**n/(m \\
& **4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22 \\
& *m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 2*A*c*d*e**m*x*x**m* \\
& x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n* \\
& **3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + A*d**2*e**m*m \\
& **3*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + \\
& 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) \\
& + 4*A*d**2*e**m*m**2*n*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n \\
& **2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + \\
& 11*n**2 + 6*n + 1) + 3*A*d**2*e**m*m**2*x*x**m*x**n/(m**4 + 6*m**3*n + \\
& 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n \\
& + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*A*d**2*e**m*m*n**2*x*x**m*x**n/( \\
& m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + \\
& 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 8*A*d**2*e**m*m*n* \\
& x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m* \\
& **2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3* \\
& A*d**2*e**m*m*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18 \\
& *m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + \\
& 6*n + 1) + 3*A*d**2*e**m*n**2*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + \\
& 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6 \\
& *n**3 + 11*n**2 + 6*n + 1) + 4*A*d**2*e**m*n*x*x**m*x**n/(m**4 + 6*m**3 \\
& *n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18 \\
& *m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + A*d**2*e**m*x*x**m*x**n/(m** \\
& 4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m \\
& *n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + B*c**2*e**m*m**3*x*x** \\
& m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m* \\
& n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 5*B*c**2*e* \\
& *m*m**2*n*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n \\
& + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1 \\
& ) + 3*B*c**2*e**m*m**2*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 \\
& + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n \\
& **2 + 6*n + 1) + 6*B*c**2*e**m*m*n**2*x*x**m*x**n/(m**4 + 6*m**3*n + 4*m**3
\end{aligned}$$

$$\begin{aligned}
& + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m \\
& + 6n^{**3} + 11n^{**2} + 6n + 1) + 10B^{**c}e^{**m}m^{**n}x^{**x}m^{**x}n^{**n}/(m^{**4} + 6m^{**} \\
& *3n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} + \\
& 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + 3B^{**c}e^{**m}m^{**x}x^{**m}x^{**n}/(m \\
& **4 + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22 \\
& *m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + 6B^{**c}e^{**m}n^{**2}x \\
& *x^{**m}x^{**n}/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + \\
& 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + 5B^{**c} \\
& 2e^{**m}n^{**x}x^{**m}x^{**n}/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + \\
& 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) \\
& + B^{**c}e^{**m}x^{**x}m^{**x}n^{**n}/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**} \\
& *2n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n \\
& + 1) + 2B^{**c}d^{**e}m^{**m}3x^{**x}m^{**x}(2n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**} \\
& **2n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**} \\
& 3 + 11n^{**2} + 6n + 1) + 8B^{**c}d^{**e}m^{**m}2n^{**x}x^{**m}x^{**}(2n)/(m^{**4} + 6m^{**3} \\
& *n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18 \\
& *m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + 6B^{**c}d^{**e}m^{**m}2x^{**x}m^{**x}(2n \\
& )/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 3 \\
& + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + 6B^{**c}d^{**e}m^{**m} \\
& **2x^{**x}m^{**x}(2n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + \\
& 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) \\
& + 16B^{**c}d^{**e}m^{**m}n^{**x}x^{**m}x^{**}(2n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**} \\
& 2 + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11 \\
& n^{**2} + 6n + 1) + 6B^{**c}d^{**e}m^{**m}x^{**x}m^{**x}(2n)/(m^{**4} + 6m^{**3}n + 4m^{**3} \\
& + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + \\
& 6n^{**3} + 11n^{**2} + 6n + 1) + 6B^{**c}d^{**e}m^{**n}2x^{**x}m^{**x}(2n)/(m^{**4} + 6 \\
& m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} \\
& + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + 8B^{**c}d^{**e}m^{**n}x^{**x}m^{**x}(2 \\
& n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 3 \\
& + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + 2B^{**c}d^{**e}m^{**x} \\
& x^{**m}x^{**}(2n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} \\
& + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + B^{**d} \\
& *2e^{**m}m^{**3}x^{**x}m^{**x}(3n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18 \\
& m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + \\
& 6n + 1) + 3B^{**d}e^{**m}m^{**2}n^{**x}x^{**m}x^{**}(3n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + \\
& 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + \\
& 6n^{**3} + 11n^{**2} + 6n + 1) + 3B^{**d}e^{**m}m^{**2}x^{**x}m^{**x}(3n)/(m^{**4} + 6 \\
& m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} \\
& + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + 2B^{**d}e^{**m}m^{**2}x^{**x}m^{**} \\
& x^{**}(3n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6 \\
& m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + 6B^{**d}e^{**m} \\
& **n^{**x}x^{**m}x^{**}(3n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2} \\
& *n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n \\
& + 1) + 3B^{**d}e^{**m}m^{**x}x^{**m}x^{**}(3n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2} \\
& n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + \\
& 11n^{**2} + 6n + 1) + 2B^{**d}e^{**m}n^{**2}x^{**x}m^{**x}(3n)/(m^{**4} + 6m^{**3}n + \\
& 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**n} + 18m^{**n} \\
& + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + 3B^{**d}e^{**m}n^{**x}x^{**m}x^{**}(3n)/(m^{**4} \\
& + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} + 22m^{**} \\
& n^{**2} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1) + B^{**d}e^{**m}x^{**x}m^{**x}( \\
& 3n)/(m^{**4} + 6m^{**3}n + 4m^{**3} + 11m^{**2}n^{**2} + 18m^{**2}n + 6m^{**2} + 6m^{**n} \\
& *3 + 22m^{**n} + 18m^{**n} + 4m + 6n^{**3} + 11n^{**2} + 6n + 1), True))
\end{aligned}$$

### 3.9 $\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^3 dx$

**Optimal.** Leaf size=410

$$\frac{a^3 Ac^3 (ex)^{m+1}}{e(m+1)} + \frac{3acx^{2n+1} (ex)^m \left( A(a^2 d^2 + 3abcd + b^2 c^2) + aBc(ad + bc) \right)}{m+2n+1} + \frac{3bdx^{5n+1} (ex)^m (a^2 Bd^2 + abd(Ad + Bc))}{m+5n+1}$$

**Rubi [A]** time = 0.62, antiderivative size = 410, normalized size of antiderivative = 1.00, number of steps used = 16, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {570, 20, 30}

$$\frac{3acx^{2n+1}(ex)^{m+1}(A^2d^2 + 3abcd + b^2c^2) + abC(ad + bc)}{m+2n+1} + \frac{3acx^{2n+1}(ex)^m(A^2d^2 + 3abcd + b^2c^2) + 3abC(A^2d^2 + 3abcd + b^2c^2)}{m+2n+1} + \frac{3bdx^{5n+1}(ex)^m(a^2Bd^2 + abd(Ad + Bc))}{m+5n+1} + \frac{3bdx^{5n+1}(ex)^m(a^2Bd^2 + abd(Ad + Bc))}{m+5n+1} + \frac{3bdx^{5n+1}(ex)^m(a^2Bd^2 + abd(Ad + Bc))}{m+5n+1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out] (a^2\*c^2\*(a\*B\*c + 3\*A\*(b\*c + a\*d))\*x^(1 + n)\*(e\*x)^m/(1 + m + n) + (3\*a\*c\*(a\*B\*c\*(b\*c + a\*d) + A\*(b^2\*c^2 + 3\*a\*b\*c\*d + a^2\*d^2))\*x^(1 + 2\*n)\*(e\*x)^m/(1 + m + 2\*n) + ((3\*a\*B\*c\*(b^2\*c^2 + 3\*a\*b\*c\*d + a^2\*d^2) + A\*(b^3\*c^3 + 9\*a\*b^2\*c^2\*d + 9\*a^2\*b\*c\*d^2 + a^3\*d^3))\*x^(1 + 3\*n)\*(e\*x)^m/(1 + m + 3\*n) + ((a^3\*B\*d^3 + 9\*a\*b^2\*c\*d\*(B\*c + A\*d) + 3\*a^2\*b\*d^2\*(3\*B\*c + A\*d) + b^3\*c^2\*(B\*c + 3\*A\*d))\*x^(1 + 4\*n)\*(e\*x)^m/(1 + m + 4\*n) + (3\*b\*d\*(a^2\*B\*d^2 + b^2\*c\*(B\*c + A\*d) + a\*b\*d\*(3\*B\*c + A\*d))\*x^(1 + 5\*n)\*(e\*x)^m/(1 + m + 5\*n) + (b^2\*d^2\*(3\*b\*B\*c + A\*b\*d + 3\*a\*B\*d))\*x^(1 + 6\*n)\*(e\*x)^m/(1 + m + 6\*n) + (b^3\*B\*d^3\*x^(1 + 7\*n)\*(e\*x)^m)/(1 + m + 7\*n) + (a^3\*A\*c^3\*(e\*x)^(1 + m))/(e\*(1 + m))

#### Rule 20

Int[(u\_)\*((a\_)\*(v\_))^(m\_)\*((b\_)\*(v\_))^(n\_), x\_Symbol] := Dist[(b^IntPart[n]\*(b\*v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

#### Rule 30

Int[(x\_)^(m\_), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]

#### Rule 570

Int[((g\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_)\*((e\_) + (f\_)\*(x\_)^(n\_))^(r\_), x\_Symbol] := Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

#### Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^3 dx &= \int \left( a^3 Ac^3 (ex)^m + a^2 c^2 (aBc + 3A(bc + ad)) x^n (ex)^m + 3ac (aBc(b^2 c^2 + 3abd(Ad + Bc)) + A^2 d^2) x^{2n} (ex)^m + 3bdx^{5n+1} (ex)^m (a^2 Bd^2 + abd(Ad + Bc)) \right) dx \\ &= \frac{a^3 Ac^3 (ex)^{1+m}}{e(1+m)} + (b^3 Bd^3) \int x^{7n} (ex)^m dx + (b^2 d^2 (3bBc + Abd + A^2 d^2)) \int x^{2n} (ex)^m dx + \frac{3bdx^{5n+1} (ex)^m (a^2 Bd^2 + abd(Ad + Bc))}{m+5n+1} \\ &= \frac{a^3 Ac^3 (ex)^{1+m}}{e(1+m)} + (b^3 Bd^3 x^{-m} (ex)^m) \int x^{m+7n} dx + (b^2 d^2 (3bBc + Abd + A^2 d^2)) \int x^{m+2n} dx + \frac{3bdx^{5n+1} (ex)^m (a^2 Bd^2 + abd(Ad + Bc))}{m+5n+1} \\ &= \frac{a^2 c^2 (aBc + 3A(bc + ad)) x^{1+n} (ex)^m}{1+m+n} + \frac{3ac (aBc(bc + ad) + A(b^2 c^2 + 3abd(Ad + Bc))) x^{1+n} (ex)^m}{1+m+n} \end{aligned}$$

**Mathematica [A]** time = 1.43, size = 358, normalized size = 0.87

$$x^{m+1} \left( \frac{a^3 A^3}{m+1} + \frac{3acx^{2m} (A(a^2 d^2 + 3abcd + b^2 c^2) + aB(ad + bc))}{m+2n+1} + \frac{3abd^{2m} (a^2 Bd^2 + abd(Ad + 3Bc) + b^2 d(Ad + Bc))}{m+5n+1} + \frac{a^2 c^2 x^{m+1} (3A(ad + bc) + aBc)}{m+n+1} + \frac{a^{4m} (a^2 Bd^2 + 3a^2 b^2 d(Ad + 3Bc) + 9ab^2 d(Ad + Bc) + b^3 d^2 (3Ad + Bc))}{m+4n+1} + \frac{a^{3m} (3aBc (a^2 d^2 + 3abcd + b^2 c^2) + A(a^2 d^2 + 9a^2 b^2 d + 9ab^2 d^2 + b^3 d^2))}{m+3n+1} + \frac{b^2 d^{2m} (3aBd + Abd + 3Bc)}{m+6n+1} + \frac{b^3 Bd^{2m}}{m+7n+1} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out] x\*(e\*x)^m\*((a^3\*A\*c^3)/(1 + m) + (a^2\*c^2\*(a\*B\*c + 3\*A\*(b\*c + a\*d))\*x^n)/(1 + m + n) + (3\*a\*c\*(a\*B\*c\*(b\*c + a\*d) + A\*(b^2\*c^2 + 3\*a\*b\*c\*d + a^2\*d^2))\*x^(2\*n))/(1 + m + 2\*n) + ((3\*a\*B\*c\*(b^2\*c^2 + 3\*a\*b\*c\*d + a^2\*d^2) + A\*(b^3\*c^3 + 9\*a\*b^2\*c^2\*d + 9\*a^2\*b\*c\*d^2 + a^3\*d^3))\*x^(3\*n))/(1 + m + 3\*n) + ((a^3\*B\*d^3 + 9\*a\*b^2\*c\*d\*(B\*c + A\*d) + 3\*a^2\*b\*d^2\*(3\*B\*c + A\*d) + b^3\*c^2\*(B\*c + 3\*A\*d))\*x^(4\*n))/(1 + m + 4\*n) + (3\*b\*d\*(a^2\*B\*d^2 + b^2\*c\*(B\*c + A\*d) + a\*b\*d\*(3\*B\*c + A\*d))\*x^(5\*n))/(1 + m + 5\*n) + (b^2\*d^2\*(3\*b\*B\*c + A\*b\*d + 3\*a\*B\*d))\*x^(6\*n))/(1 + m + 6\*n) + (b^3\*B\*d^3\*x^(7\*n))/(1 + m + 7\*n))

**IntegrateAlgebraic [F]** time = 1.25, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^3 dx$$

Verification is not applicable to the result.

[In] IntegrateAlgebraic[(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out] Defer[IntegrateAlgebraic] [(e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n)\*(c + d\*x^n)^3, x]

**fricas [B]** time = 0.74, size = 11628, normalized size = 28.36

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="fricas")

[Out] ((B\*b^3\*d^3\*m^7 + 7\*B\*b^3\*d^3\*m^6 + 21\*B\*b^3\*d^3\*m^5 + 35\*B\*b^3\*d^3\*m^4 + 35\*B\*b^3\*d^3\*m^3 + 21\*B\*b^3\*d^3\*m^2 + 7\*B\*b^3\*d^3\*m + B\*b^3\*d^3 + 720\*(B\*b^3\*d^3\*m + B\*b^3\*d^3)\*n^6 + 1764\*(B\*b^3\*d^3\*m^2 + 2\*B\*b^3\*d^3\*m + B\*b^3\*d^3)\*n^5 + 1624\*(B\*b^3\*d^3\*m^3 + 3\*B\*b^3\*d^3\*m^2 + 3\*B\*b^3\*d^3\*m + B\*b^3\*d^3)\*n^4 + 735\*(B\*b^3\*d^3\*m^4 + 4\*B\*b^3\*d^3\*m^3 + 6\*B\*b^3\*d^3\*m^2 + 4\*B\*b^3\*d^3\*m + B\*b^3\*d^3)\*n^3 + 175\*(B\*b^3\*d^3\*m^5 + 5\*B\*b^3\*d^3\*m^4 + 10\*B\*b^3\*d^3\*m^3 + 10\*B\*b^3\*d^3\*m^2 + 5\*B\*b^3\*d^3\*m + B\*b^3\*d^3)\*n^2 + 21\*(B\*b^3\*d^3\*m^6 + 6\*B\*b^3\*d^3\*m^5 + 15\*B\*b^3\*d^3\*m^4 + 20\*B\*b^3\*d^3\*m^3 + 15\*B\*b^3\*d^3\*m^2 + 6\*B\*b^3\*d^3\*m + B\*b^3\*d^3)\*n)\*x\*x^(7\*n)\*e^(m\*log(e) + m\*log(x)) + ((3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^7 + 3\*B\*b^3\*c\*d^2 + 7\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^6 + 840\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3 + (3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m)\*n^6 + 21\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^5 + 2038\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3 + (3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^2 + 2\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m)\*n^5 + 35\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^4 + 1849\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3 + (3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^3 + 3\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^2 + 3\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m)\*n^4 + (3\*B\*a\*b^2 + A\*b^3)\*d^3 + 35\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^3 + 820\*(3\*B\*b^3\*c\*d^2 + (3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^4 + (3\*B\*a\*b^2 + A\*b^3)\*d^3 + 4\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^3 + 6\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^2 + 4\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m)\*n^3 + 21\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^2 + 190\*(3\*B\*b^3\*c\*d^2 + (3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^5 + 5\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^4 + (3\*B\*a\*b^2 + A\*b^3)\*d^3 + 10\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^3 + 10\*(3\*B\*b^3\*c\*d^2 + (3\*B\*a\*b^2 + A\*b^3)\*d^3)\*m^2 +

$$\begin{aligned}
& 5*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m)*n^2 + 7*(3*B*b^3*c*d^2 + (3* \\
& *B*a*b^2 + A*b^3)*d^3)*m + 22*(3*B*b^3*c*d^2 + (3*B*b^3*c*d^2 + (3*B*a*b^2 \\
& + A*b^3)*d^3)*m^6 + 6*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^5 + 15*(3 \\
& *B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^4 + (3*B*a*b^2 + A*b^3)*d^3 + 20* \\
& (3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^3 + 15*(3*B*b^3*c*d^2 + (3*B*a* \\
& b^2 + A*b^3)*d^3)*m^2 + 6*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m)*n)*x \\
& *x^{(6*n)}*e^{(m*\log(e) + m*\log(x))} + 3*((B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c* \\
& d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^7 + B*b^3*c^2*d + 7*(B*b^3*c^2*d + (3*B*a* \\
& b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^6 + 1008*(B*b^3*c^2*d + (3* \\
& B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + (B*b^3*c^2*d + (3*B*a*b^ \\
& 2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m)*n^6 + 21*(B*b^3*c^2*d + (3*B \\
& *a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^5 + 2412*(B*b^3*c^2*d + \\
& (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + (B*b^3*c^2*d + (3*B*a \\
& *b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 2*(B*b^3*c^2*d + (3*B* \\
& a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m)*n^5 + 35*(B*b^3*c^2*d + \\
& (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^4 + 2144*(B*b^3*c^2* \\
& d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + (B*b^3*c^2*d + (3 \\
& *B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^3 + 3*(B*b^3*c^2*d + ( \\
& 3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 3*(B*b^3*c^2*d + \\
& (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m)*n^4 + (3*B*a*b^2 + \\
& A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + 35*(B*b^3*c^2*d + (3*B*a*b^2 + A*b \\
& ^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^3 + 925*(B*b^3*c^2*d + (B*b^3*c^2*d \\
& + (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^4 + (3*B*a*b^2 + A \\
& *b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + 4*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3 \\
& )*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^3 + 6*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^ \\
& 3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 4*(B*b^3*c^2*d + (3*B*a*b^2 + A*b \\
& ^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m)*n^3 + 21*(B*b^3*c^2*d + (3*B*a*b^2 \\
& + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 207*(B*b^3*c^2*d + (B*b^3*c \\
& ^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^5 + 5*(B*b^3*c \\
& ^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^4 + (3*B*a*b \\
& ^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + 10*(B*b^3*c^2*d + (3*B*a*b^2 \\
& + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^3 + 10*(B*b^3*c^2*d + (3*B*a*b^ \\
& 2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 5*(B*b^3*c^2*d + (3*B*a*b \\
& ^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m)*n^2 + 7*(B*b^3*c^2*d + (3*B \\
& *a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m + 23*(B*b^3*c^2*d + (B*b \\
& ^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^6 + 6*(B* \\
& b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^5 + 15*( \\
& B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^4 + (3 \\
& *B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + 20*(B*b^3*c^2*d + (3*B* \\
& a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^3 + 15*(B*b^3*c^2*d + (3* \\
& B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 6*(B*b^3*c^2*d + (3 \\
& *B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m)*n)*x*x^{(5*n)}*e^{(m*\log \\
& (e) + m*\log(x))} + ((B*b^3*c^3 + 3*(3*B*a*b^2 + A*b^3)*c^2*d + 9*(B*a^2*b + \\
& A*a*b^2)*c*d^2 + (B*a^3 + 3*A*a^2*b)*d^3)*m^7 + B*b^3*c^3 + 7*(B*b^3*c^3 + \\
& 3*(3*B*a*b^2 + A*b^3)*c^2*d + 9*(B*a^2*b + A*a*b^2)*c*d^2 + (B*a^3 + 3*A*a^ \\
& 2*b)*d^3)*m^6 + 1260*(B*b^3*c^3 + 3*(3*B*a*b^2 + A*b^3)*c^2*d + 9*(B*a^2*b \\
& + A*a*b^2)*c*d^2 + (B*a^3 + 3*A*a^2*b)*d^3 + (B*b^3*c^3 + 3*(3*B*a*b^2 + A* \\
& b^3)*c^2*d + 9*(B*a^2*b + A*a*b^2)*c*d^2 + (B*a^3 + 3*A*a^2*b)*d^3)*m)*n^6 \\
& + 21*(B*b^3*c^3 + 3*(3*B*a*b^2 + A*b^3)*c^2*d + 9*(B*a^2*b + A*a*b^2)*c*d^2 \\
& + (B*a^3 + 3*A*a^2*b)*d^3)*m^5 + 2952*(B*b^3*c^3 + 3*(3*B*a*b^2 + A*b^3)*c \\
& ^2*d + 9*(B*a^2*b + A*a*b^2)*c*d^2 + (B*a^3 + 3*A*a^2*b)*d^3 + (B*b^3*c^3 + \\
& 3*(3*B*a*b^2 + A*b^3)*c^2*d + 9*(B*a^2*b + A*a*b^2)*c*d^2 + (B*a^3 + 3*A*a \\
& ^2*b)*d^3)*m^2 + 2*(B*b^3*c^3 + 3*(3*B*a*b^2 + A*b^3)*c^2*d + 9*(B*a^2*b + \\
& A*a*b^2)*c*d^2 + (B*a^3 + 3*A*a^2*b)*d^3)*m)*n^5 + 35*(B*b^3*c^3 + 3*(3*B*a \\
& *b^2 + A*b^3)*c^2*d + 9*(B*a^2*b + A*a*b^2)*c*d^2 + (B*a^3 + 3*A*a^2*b)*d^3 \\
& )*m^4 + 2545*(B*b^3*c^3 + 3*(3*B*a*b^2 + A*b^3)*c^2*d + 9*(B*a^2*b + A*a*b^ \\
& 2)*c*d^2 + (B*a^3 + 3*A*a^2*b)*d^3 + (B*b^3*c^3 + 3*(3*B*a*b^2 + A*b^3)*c^2 \\
& *d + 9*(B*a^2*b + A*a*b^2)*c*d^2 + (B*a^3 + 3*A*a^2*b)*d^3)*m^3 + 3*(B*b^3*c \\
& ^3 + 3*(3*B*a*b^2 + A*b^3)*c^2*d + 9*(B*a^2*b + A*a*b^2)*c*d^2 + (B*a^3 +
\end{aligned}$$





$$\begin{aligned}
& *a*b^2)*c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2)*m^2 + 4*(A*a^3*d^3 + (3*B*a*b^2 \\
& + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2) \\
& *m)*n^3 + 21*(A*a^3*d^3 + (3*B*a*b^2 + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c \\
& ^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2)*m^2 + 247*(A*a^3*d^3 + (A*a^3*d^3 + (3* \\
& B*a*b^2 + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c^2*d + 3*(B*a^3 + 3*A*a^2*b)* \\
& c*d^2)*m^5 + 5*(A*a^3*d^3 + (3*B*a*b^2 + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2) \\
& *c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2)*m^4 + (3*B*a*b^2 + A*b^3)*c^3 + 9*(B* \\
& a^2*b + A*a*b^2)*c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2 + 10*(A*a^3*d^3 + (3*B \\
& *a*b^2 + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c \\
& *d^2)*m^3 + 10*(A*a^3*d^3 + (3*B*a*b^2 + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2) \\
& *c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2)*m^2 + 5*(A*a^3*d^3 + (3*B*a*b^2 + A*b \\
& ^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2)*m)*n^2 \\
& + 7*(A*a^3*d^3 + (3*B*a*b^2 + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c^2*d + 3 \\
& *(B*a^3 + 3*A*a^2*b)*c*d^2)*m + 25*(A*a^3*d^3 + (A*a^3*d^3 + (3*B*a*b^2 + A \\
& *b^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2)*m^6 \\
& + 6*(A*a^3*d^3 + (3*B*a*b^2 + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c^2*d + 3* \\
& (B*a^3 + 3*A*a^2*b)*c*d^2)*m^5 + 15*(A*a^3*d^3 + (3*B*a*b^2 + A*b^3)*c^3 + \\
& 9*(B*a^2*b + A*a*b^2)*c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2)*m^4 + (3*B*a*b^2 \\
& + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2 + \\
& 20*(A*a^3*d^3 + (3*B*a*b^2 + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c^2*d + 3* \\
& (B*a^3 + 3*A*a^2*b)*c*d^2)*m^3 + 15*(A*a^3*d^3 + (3*B*a*b^2 + A*b^3)*c^3 + \\
& 9*(B*a^2*b + A*a*b^2)*c^2*d + 3*(B*a^3 + 3*A*a^2*b)*c*d^2)*m^2 + 6*(A*a^3*d \\
& ^3 + (3*B*a*b^2 + A*b^3)*c^3 + 9*(B*a^2*b + A*a*b^2)*c^2*d + 3*(B*a^3 + 3*A \\
& *a^2*b)*c*d^2)*m)*n)*x*x^(3*n)*e^(m*log(e) + m*log(x)) + 3*((A*a^3*c*d^2 + \\
& (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^7 + A*a^3*c*d^2 + 7* \\
& (A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^6 + 2 \\
& 520*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d + (A \\
& *a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m)*n^6 + \\
& 21*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^5 \\
& + 5274*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d + \\
& (A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^2 + \\
& 2*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m)*n^ \\
& 5 + 35*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)* \\
& m^4 + 3929*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2 \\
& *d + (A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^ \\
& 3 + 3*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m \\
& ^2 + 3*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)* \\
& m)*n^4 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d + 35*(A*a^3*c* \\
& d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^3 + 1420*(A*a^ \\
& 3*c*d^2 + (A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2* \\
& d)*m^4 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d + 4*(A*a^3*c*d \\
& ^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^3 + 6*(A*a^3*c* \\
& d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^2 + 4*(A*a^3*c \\
& *d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m)*n^3 + 21*(A* \\
& a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^2 + 270* \\
& (A*a^3*c*d^2 + (A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b) \\
& *c^2*d)*m^5 + 5*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b) \\
& )*c^2*d)*m^4 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d + 10*(A* \\
& a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^3 + 10*( \\
& A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^2 + 5* \\
& (A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m)*n^2 \\
& + 7*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m + \\
& 26*(A*a^3*c*d^2 + (A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^ \\
& 2*b)*c^2*d)*m^6 + 6*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a \\
& ^2*b)*c^2*d)*m^5 + 15*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A \\
& *a^2*b)*c^2*d)*m^4 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d + \\
& 20*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^3 \\
& + 15*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m^ \\
& 2 + 6*(A*a^3*c*d^2 + (B*a^2*b + A*a*b^2)*c^3 + (B*a^3 + 3*A*a^2*b)*c^2*d)*m
\end{aligned}$$

$$\begin{aligned}
& ) * n) * x * x^{(2 * n)} * e^{(m * \log(e) + m * \log(x))} + ((3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^7 + 3 * A * a^3 * c^2 * d + 7 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^6 + 5040 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^5 + 8028 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^4 + 21 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^3 + 1665 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^2 + 1960 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m + 27 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^6 + 6 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^5 + 15 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^4 + (B * a^3 + 3 * A * a^2 * b) * c^3 + 20 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^3 + 15 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m^2 + 6 * (3 * A * a^3 * c^2 * d + (B * a^3 + 3 * A * a^2 * b) * c^3) * m) * n * x^n * e^{(m * \log(e) + m * \log(x))} + (A * a^3 * c^3 * m^7 + 5040 * A * a^3 * c^3 * n^7 + 7 * A * a^3 * c^3 * m^6 + 21 * A * a^3 * c^3 * m^5 + 35 * A * a^3 * c^3 * m^4 + 35 * A * a^3 * c^3 * m^3 + 21 * A * a^3 * c^3 * m^2 + 7 * A * a^3 * c^3 * m + A * a^3 * c^3 + 13068 * (A * a^3 * c^3 * m + A * a^3 * c^3) * n^6 + 13132 * (A * a^3 * c^3 * m^2 + 2 * A * a^3 * c^3 * m + A * a^3 * c^3) * n^5 + 6769 * (A * a^3 * c^3 * m^3 + 3 * A * a^3 * c^3 * m^2 + 3 * A * a^3 * c^3 * m + A * a^3 * c^3) * n^4 + 1960 * (A * a^3 * c^3 * m^4 + 4 * A * a^3 * c^3 * m^3 + 6 * A * a^3 * c^3 * m^2 + 4 * A * a^3 * c^3 * m + A * a^3 * c^3) * n^3 + 322 * (A * a^3 * c^3 * m^5 + 5 * A * a^3 * c^3 * m^4 + 10 * A * a^3 * c^3 * m^3 + 10 * A * a^3 * c^3 * m^2 + 5 * A * a^3 * c^3 * m + A * a^3 * c^3) * n^2 + 28 * (A * a^3 * c^3 * m^6 + 6 * A * a^3 * c^3 * m^5 + 15 * A * a^3 * c^3 * m^4 + 20 * A * a^3 * c^3 * m^3 + 15 * A * a^3 * c^3 * m^2 + 6 * A * a^3 * c^3 * m + A * a^3 * c^3) * n) * x * e^{(m * \log(e) + m * \log(x))} / (m^8 + 5040 * (m + 1) * n^7 + 8 * m^7 + 13068 * (m^2 + 2 * m + 1) * n^6 + 28 * m^6 + 13132 * (m^3 + 3 * m^2 + 3 * m + 1) * n^5 + 56 * m^5 + 6769 * (m^4 + 4 * m^3 + 6 * m^2 + 4 * m + 1) * n^4 + 70 * m^4 + 1960 * (m^5 + 5 * m^4 + 10 * m^3 + 10 * m^2 + 5 * m + 1) * n^3 + 56 * m^3 + 322 * (m^6 + 6 * m^5 + 15 * m^4 + 20 * m^3 + 15 * m^2 + 6 * m + 1) * n^2 + 28 * m^2 + 28 * (m^7 + 7 * m^6 + 21 * m^5 + 35 * m^4 + 35 * m^3 + 21 * m^2 + 7 * m + 1) * n + 8 * m + 1)
\end{aligned}$$

**giac** [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="giac")

[Out] Timed out

**maple** [C] time = 0.34, size = 20937, normalized size = 51.07

output too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(b\*x^n+a)^3\*(B\*x^n+A)\*(d\*x^n+c)^3,x)

[Out] result too large to display

**maxima** [B] time = 1.47, size = 1032, normalized size = 2.52

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^3*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="maxima")
```

```
[Out] B*b^3*d^3*e^m*x*e^(m*log(x) + 7*n*log(x))/(m + 7*n + 1) + 3*B*b^3*c*d^2*e^m
*x*e^(m*log(x) + 6*n*log(x))/(m + 6*n + 1) + 3*B*a*b^2*d^3*e^m*x*e^(m*log(x)
) + 6*n*log(x))/(m + 6*n + 1) + A*b^3*d^3*e^m*x*e^(m*log(x) + 6*n*log(x))/(
m + 6*n + 1) + 3*B*b^3*c^2*d*e^m*x*e^(m*log(x) + 5*n*log(x))/(m + 5*n + 1)
+ 9*B*a*b^2*c*d^2*e^m*x*e^(m*log(x) + 5*n*log(x))/(m + 5*n + 1) + 3*A*b^3*c
*d^2*e^m*x*e^(m*log(x) + 5*n*log(x))/(m + 5*n + 1) + 3*B*a^2*b*d^3*e^m*x*e^
(m*log(x) + 5*n*log(x))/(m + 5*n + 1) + 3*A*a*b^2*d^3*e^m*x*e^(m*log(x) + 5
*n*log(x))/(m + 5*n + 1) + B*b^3*c^3*e^m*x*e^(m*log(x) + 4*n*log(x))/(m + 4
*n + 1) + 9*B*a*b^2*c^2*d*e^m*x*e^(m*log(x) + 4*n*log(x))/(m + 4*n + 1) + 3
*A*b^3*c^2*d*e^m*x*e^(m*log(x) + 4*n*log(x))/(m + 4*n + 1) + 9*B*a^2*b*c*d^
2*e^m*x*e^(m*log(x) + 4*n*log(x))/(m + 4*n + 1) + 9*A*a*b^2*c*d^2*e^m*x*e^
(m*log(x) + 4*n*log(x))/(m + 4*n + 1) + B*a^3*d^3*e^m*x*e^(m*log(x) + 4*n*lo
g(x))/(m + 4*n + 1) + 3*A*a^2*b*d^3*e^m*x*e^(m*log(x) + 4*n*log(x))/(m + 4*
n + 1) + 3*B*a*b^2*c^3*e^m*x*e^(m*log(x) + 3*n*log(x))/(m + 3*n + 1) + A*b^
3*c^3*e^m*x*e^(m*log(x) + 3*n*log(x))/(m + 3*n + 1) + 9*B*a^2*b*c^2*d*e^m*x
*e^(m*log(x) + 3*n*log(x))/(m + 3*n + 1) + 9*A*a*b^2*c^2*d*e^m*x*e^(m*log(x
) + 3*n*log(x))/(m + 3*n + 1) + 3*B*a^3*c*d^2*e^m*x*e^(m*log(x) + 3*n*log(x
))/(m + 3*n + 1) + 9*A*a^2*b*c*d^2*e^m*x*e^(m*log(x) + 3*n*log(x))/(m + 3*n
+ 1) + A*a^3*d^3*e^m*x*e^(m*log(x) + 3*n*log(x))/(m + 3*n + 1) + 3*B*a^2*b
*c^3*e^m*x*e^(m*log(x) + 2*n*log(x))/(m + 2*n + 1) + 3*A*a*b^2*c^3*e^m*x*e^
(m*log(x) + 2*n*log(x))/(m + 2*n + 1) + 3*B*a^3*c^2*d*e^m*x*e^(m*log(x) + 2
*n*log(x))/(m + 2*n + 1) + 9*A*a^2*b*c^2*d*e^m*x*e^(m*log(x) + 2*n*log(x))/
(m + 2*n + 1) + 3*A*a^3*c*d^2*e^m*x*e^(m*log(x) + 2*n*log(x))/(m + 2*n + 1)
+ B*a^3*c^3*e^m*x*e^(m*log(x) + n*log(x))/(m + n + 1) + 3*A*a^2*b*c^3*e^m*x
*e^(m*log(x) + n*log(x))/(m + n + 1) + 3*A*a^3*c^2*d*e^m*x*e^(m*log(x) + n
*log(x))/(m + n + 1) + (e*x)^(m + 1)*A*a^3*c^3/(e*(m + 1))
```

**mupad [B]** time = 7.49, size = 2949, normalized size = 7.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(A + B*x^n)*(a + b*x^n)^3*(c + d*x^n)^3,x)
```

```
[Out] (x*x^(3*n)*(e*x)^m*(A*a^3*d^3 + A*b^3*c^3 + 3*B*a*b^2*c^3 + 3*B*a^3*c*d^2 +
9*A*a*b^2*c^2*d + 9*A*a^2*b*c*d^2 + 9*B*a^2*b*c^2*d)*(6*m + 25*n + 125*m*n
+ 988*m*n^2 + 250*m^2*n + 3657*m*n^3 + 250*m^3*n + 6224*m*n^4 + 125*m^4*n
+ 3796*m*n^5 + 25*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 247*n^2
+ 1219*n^3 + 3112*n^4 + 3796*n^5 + 1680*n^6 + 1482*m^2*n^2 + 3657*m^2*n^3 +
988*m^3*n^2 + 3112*m^2*n^4 + 1219*m^3*n^3 + 247*m^4*n^2 + 1))/(7*m + 28*n
+ 168*m*n + 1610*m*n^2 + 420*m^2*n + 7840*m*n^3 + 560*m^3*n + 20307*m*n^4 +
420*m^4*n + 26264*m*n^5 + 168*m^5*n + 13068*m*n^6 + 28*m^6*n + 21*m^2 + 35
*m^3 + 35*m^4 + 21*m^5 + 7*m^6 + m^7 + 322*n^2 + 1960*n^3 + 6769*n^4 + 1313
2*n^5 + 13068*n^6 + 5040*n^7 + 3220*m^2*n^2 + 11760*m^2*n^3 + 3220*m^3*n^2
+ 20307*m^2*n^4 + 7840*m^3*n^3 + 1610*m^4*n^2 + 13132*m^2*n^5 + 6769*m^3*n^
4 + 1960*m^4*n^3 + 322*m^5*n^2 + 1) + (x*x^(4*n)*(e*x)^m*(B*a^3*d^3 + B*b^3
*c^3 + 3*A*a^2*b*d^3 + 3*A*b^3*c^2*d + 9*A*a*b^2*c*d^2 + 9*B*a*b^2*c^2*d +
9*B*a^2*b*c*d^2)*(6*m + 24*n + 120*m*n + 904*m*n^2 + 240*m^2*n + 3168*m*n^3
+ 240*m^3*n + 5090*m*n^4 + 120*m^4*n + 2952*m*n^5 + 24*m^5*n + 15*m^2 + 20
*m^3 + 15*m^4 + 6*m^5 + m^6 + 226*n^2 + 1056*n^3 + 2545*n^4 + 2952*n^5 + 12
60*n^6 + 1356*m^2*n^2 + 3168*m^2*n^3 + 904*m^3*n^2 + 2545*m^2*n^4 + 1056*m^
3*n^3 + 226*m^4*n^2 + 1))/(7*m + 28*n + 168*m*n + 1610*m*n^2 + 420*m^2*n +
7840*m*n^3 + 560*m^3*n + 20307*m*n^4 + 420*m^4*n + 26264*m*n^5 + 168*m^5*n
+ 13068*m*n^6 + 28*m^6*n + 21*m^2 + 35*m^3 + 35*m^4 + 21*m^5 + 7*m^6 + m^7
+ 322*n^2 + 1960*n^3 + 6769*n^4 + 13132*n^5 + 13068*n^6 + 5040*n^7 + 3220*m
```

$$\begin{aligned}
& ^2n^2 + 11760m^2n^3 + 3220m^3n^2 + 20307m^2n^4 + 7840m^3n^3 + 1610 \\
& m^4n^2 + 13132m^2n^5 + 6769m^3n^4 + 1960m^4n^3 + 322m^5n^2 + 1) + \\
& (A^3c^3x^m(e^x)^m)/(m + 1) + (a^2c^2xxx^n(e^x)^m(3A^2ad + 3A^2bc \\
& + B^2ac)*(6m + 27n + 135m^2n + 1180m^3n^2 + 270m^4n + 4995m^5n^3 + 270m^6n^4 \\
& + 10208m^7n^5 + 135m^8n^6 + 8028m^9n^7 + 27m^{10}n^8 + 15m^{11}n^9 + 20m^{12}n^{10} + \\
& 15m^{13}n^{11} + 6m^{14}n^{12} + m^{15}n^{13} + 295n^2 + 1665n^3 + 5104n^4 + 8028n^5 + 5040n^6 \\
& + 1770m^2n^2 + 4995m^2n^3 + 1180m^3n^2 + 5104m^2n^4 + 1665m^3n^3 \\
& + 295m^4n^2 + 1))/(7m + 28n + 168m^2n + 1610m^3n^2 + 420m^4n + 7840m^5n^3 \\
& + 560m^6n^4 + 20307m^7n^5 + 420m^8n^6 + 26264m^9n^7 + 168m^{10}n^8 + 130 \\
& 68m^{11}n^9 + 28m^{12}n^{10} + 21m^{13}n^{11} + 35m^{14}n^{12} + 35m^{15}n^{13} + 21m^{16}n^{14} + 7m^{17}n^{15} + 322 \\
& n^2 + 1960n^3 + 6769n^4 + 13132n^5 + 13068n^6 + 5040n^7 + 3220m^2n^2 \\
& + 11760m^2n^3 + 3220m^3n^2 + 20307m^2n^4 + 7840m^3n^3 + 1610m^4n^2 + 13132m^2n^5 \\
& + 6769m^3n^4 + 1960m^4n^3 + 322m^5n^2 + 1) + (B^3d^3xxx^{(7n)}(e^x)^m(6m + 21n + 105m^2n + 700m^3n^2 + 210m^4n^3 + 22 \\
& 05m^5n^4 + 210m^6n^5 + 3248m^7n^6 + 105m^8n^7 + 1764m^9n^8 + 21m^{10}n^9 + 15m^{11}n^{10} \\
& + 20m^{12}n^{11} + 15m^{13}n^{12} + 6m^{14}n^{13} + m^{15}n^{14} + 175n^2 + 735n^3 + 1624n^4 + 1764n^5 \\
& + 720n^6 + 1050m^2n^2 + 2205m^2n^3 + 700m^3n^2 + 1624m^2n^4 + 7 \\
& 35m^3n^3 + 175m^4n^2 + 1))/(7m + 28n + 168m^2n + 1610m^3n^2 + 420m^4n^3 \\
& + 7840m^5n^4 + 560m^6n^5 + 20307m^7n^6 + 420m^8n^7 + 26264m^9n^8 + 168m^{10}n^9 \\
& + 13068m^{11}n^{10} + 28m^{12}n^{11} + 21m^{13}n^{12} + 35m^{14}n^{13} + 35m^{15}n^{14} + 21m^{16}n^{15} + 7m^{17}n^{16} + \\
& m^{18}n^{17} + 322n^2 + 1960n^3 + 6769n^4 + 13132n^5 + 13068n^6 + 5040n^7 + 3 \\
& 220m^2n^2 + 11760m^2n^3 + 3220m^3n^2 + 20307m^2n^4 + 7840m^3n^3 + 1610m^4n^2 + 13132m^2n^5 \\
& + 6769m^3n^4 + 1960m^4n^3 + 322m^5n^2 + 1) + (3a^2c^2xxx^{(2n)}(e^x)^m(A^2d^2 + A^2b^2c^2 + B^2a^2b^2c^2 + B^2a^2c^2 \\
& *d + 3A^2a^2b^2c^2*d)*(6m + 26n + 130m^2n + 1080m^3n^2 + 260m^4n^3 + 4260m^5n^4 \\
& + 260m^6n^5 + 7858m^7n^6 + 130m^8n^7 + 5274m^9n^8 + 26m^{10}n^9 + 15m^{11}n^{10} + 20m^{12}n^{11} \\
& + 15m^{13}n^{12} + 6m^{14}n^{13} + m^{15}n^{14} + 270n^2 + 1420n^3 + 3929n^4 + 5274n^5 + \\
& 2520n^6 + 1620m^2n^2 + 4260m^2n^3 + 1080m^3n^2 + 3929m^2n^4 + 1420 \\
& m^3n^3 + 270m^4n^2 + 1))/(7m + 28n + 168m^2n + 1610m^3n^2 + 420m^4n^3 + 7840m^5n^4 \\
& + 560m^6n^5 + 20307m^7n^6 + 420m^8n^7 + 26264m^9n^8 + 168m^{10}n^9 + 13068m^{11}n^{10} \\
& + 28m^{12}n^{11} + 21m^{13}n^{12} + 35m^{14}n^{13} + 35m^{15}n^{14} + 21m^{16}n^{15} + 7m^{17}n^{16} + m^{18}n^{17} \\
& + 322n^2 + 1960n^3 + 6769n^4 + 13132n^5 + 13068n^6 + 5040n^7 + 322 \\
& 0m^2n^2 + 11760m^2n^3 + 3220m^3n^2 + 20307m^2n^4 + 7840m^3n^3 + 1 \\
& 610m^4n^2 + 13132m^2n^5 + 6769m^3n^4 + 1960m^4n^3 + 322m^5n^2 + 1) \\
& ) + (3b^2d^2xxx^{(5n)}(e^x)^m(B^2d^2 + B^2b^2c^2 + A^2a^2b^2d^2 + A^2b^2c^2d^2 \\
& + 3B^2a^2b^2c^2*d)*(6m + 23n + 115m^2n + 828m^3n^2 + 230m^4n^3 + 2775m^5n^4 \\
& + 230m^6n^5 + 4288m^7n^6 + 115m^8n^7 + 2412m^9n^8 + 23m^{10}n^9 + 15m^{11}n^{10} + 20m^{12}n^{11} \\
& + 15m^{13}n^{12} + 6m^{14}n^{13} + m^{15}n^{14} + 207n^2 + 925n^3 + 2144n^4 + 2412n^5 + 1008 \\
& n^6 + 1242m^2n^2 + 2775m^2n^3 + 828m^3n^2 + 2144m^2n^4 + 925m^3n^3 \\
& + 207m^4n^2 + 1))/(7m + 28n + 168m^2n + 1610m^3n^2 + 420m^4n^3 + 7840m^5n^4 \\
& + 560m^6n^5 + 20307m^7n^6 + 420m^8n^7 + 26264m^9n^8 + 168m^{10}n^9 + 1 \\
& 3068m^{11}n^{10} + 28m^{12}n^{11} + 21m^{13}n^{12} + 35m^{14}n^{13} + 35m^{15}n^{14} + 21m^{16}n^{15} + 7m^{17}n^{16} + m^{18}n^{17} \\
& + 322n^2 + 1960n^3 + 6769n^4 + 13132n^5 + 13068n^6 + 5040n^7 + 3220m^2n^2 \\
& + 11760m^2n^3 + 3220m^3n^2 + 20307m^2n^4 + 7840m^3n^3 + 1610m^4n^2 + 13132m^2n^5 \\
& + 6769m^3n^4 + 1960m^4n^3 + 322m^5n^2 + 1) + (b^2d^2xxx^{(6n)}(e^x)^m(A^2b^2d^2 + 3B^2a^2d^2 + 3B^2b^2c^2)*(6m + 22n + 110m^2n \\
& + 760m^3n^2 + 220m^4n^3 + 2460m^5n^4 + 220m^6n^5 + 3698m^7n^6 + 110m^8n^7 + 2038m^9n^8 \\
& + 22m^{10}n^9 + 15m^{11}n^{10} + 20m^{12}n^{11} + 15m^{13}n^{12} + 6m^{14}n^{13} + m^{15}n^{14} + 190n^2 + \\
& 820n^3 + 1849n^4 + 2038n^5 + 840n^6 + 1140m^2n^2 + 2460m^2n^3 + 76 \\
& 0m^3n^2 + 1849m^2n^4 + 820m^3n^3 + 190m^4n^2 + 1))/(7m + 28n + 16 \\
& 8m^2n + 1610m^3n^2 + 420m^4n^3 + 7840m^5n^4 + 560m^6n^5 + 20307m^7n^6 + 420 \\
& m^8n^7 + 26264m^9n^8 + 168m^{10}n^9 + 13068m^{11}n^{10} + 28m^{12}n^{11} + 21m^{13}n^{12} \\
& + 35m^{14}n^{13} + 35m^{15}n^{14} + 21m^{16}n^{15} + 7m^{17}n^{16} + m^{18}n^{17} + 322n^2 + 1960n^3 \\
& + 6769n^4 + 13132n^5 + 13068n^6 + 5040n^7 + 3220m^2n^2 + 11760m^2n^3 + 3220m^3n^2 + 20 \\
& 307m^2n^4 + 7840m^3n^3 + 1610m^4n^2 + 13132m^2n^5 + 6769m^3n^4 + \\
& 1960m^4n^3 + 322m^5n^2 + 1)
\end{aligned}$$

**sympy** [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(a+b*x**n)**3*(A+B*x**n)*(c+d*x**n)**3,x)
```

```
[Out] Timed out
```

### 3.10 $\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^3 dx$

**Optimal.** Leaf size=310

$$\frac{cx^{2n+1}(ex)^m \left( A(3a^2d^2 + 6abcd + b^2c^2) + aBc(3ad + 2bc) \right)}{m + 2n + 1} + \frac{x^{3n+1}(ex)^m \left( a^2d^2(Ad + 3Bc) + 6abcd(Ad + Bc) + b^2c^2 \right)}{m + 3n + 1}$$

**Rubi [A]** time = 0.41, antiderivative size = 310, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {570, 20, 30}

$$\frac{c^{2m+1}(ex)^m \left( A(3a^2d^2 + 6abcd + b^2c^2) + aBc(3ad + 2bc) \right)}{m + 2n + 1} + \frac{x^{3n+1}(ex)^m \left( a^2d^2(Ad + 3Bc) + 6abcd(Ad + Bc) + b^2c^2 \right)}{m + 3n + 1} + \frac{d^{4m+1}(ex)^m \left( a^2Bd^2 + 2abd(Ad + 3Bc) + 3B^2c(Ad + Bc) \right)}{m + 4n + 1} + \frac{a^2Ac^3(ex)^{m+1}}{e(m+1)} + \frac{a^2x^{n+1}(ex)^m(3aAd + aBc + 2Abc)}{m + n + 1} + \frac{b^2x^{2n+1}(ex)^m(2aBd + Abd + 3Bc)}{m + 5n + 1} + \frac{b^2Bd^3x^{6n+1}(ex)^m}{m + 6n + 1}$$

Antiderivative was successfully verified.

```
[In] Int[(e*x)^m*(a + b*x^n)^2*(A + B*x^n)*(c + d*x^n)^3,x]
[Out] (a*c^2*(2*A*b*c + a*B*c + 3*a*A*d)*x^(1 + n)*(e*x)^m)/(1 + m + n) + (c*(a*B*c*(2*b*c + 3*a*d) + A*(b^2*c^2 + 6*a*b*c*d + 3*a^2*d^2))*x^(1 + 2*n)*(e*x)^m)/(1 + m + 2*n) + ((6*a*b*c*d*(B*c + A*d) + a^2*d^2*(3*B*c + A*d) + b^2*c^2*(B*c + 3*A*d))*x^(1 + 3*n)*(e*x)^m)/(1 + m + 3*n) + (d*(a^2*B*d^2 + 3*b^2*c*(B*c + A*d) + 2*a*b*d*(3*B*c + A*d))*x^(1 + 4*n)*(e*x)^m)/(1 + m + 4*n) + (b*d^2*(3*b*B*c + A*b*d + 2*a*B*d))*x^(1 + 5*n)*(e*x)^m)/(1 + m + 5*n) + (b^2*B*d^3*x^(1 + 6*n)*(e*x)^m)/(1 + m + 6*n) + (a^2*A*c^3*(e*x)^(1 + m))/(e*(1 + m))
```

#### Rule 20

```
Int[(u_)*((a_)*(v_))^(m_)*((b_)*(v_))^(n_), x_Symbol] := Dist[(b^IntPart[n]*(b*v)^FracPart[n])/(a^IntPart[n]*(a*v)^FracPart[n]), Int[u*(a*v)^(m + n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]
```

#### Rule 30

```
Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]
```

#### Rule 570

```
Int[((g_)*(x_))^(m_)*((a_) + (b_)*(x_)^(n_))^(p_)*((c_) + (d_)*(x_)^(n_))^(q_)*((e_) + (f_)*(x_)^(n_))^(r_), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

#### Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^3 dx &= \int (a^2 Ac^3(ex)^m + ac^2(2Abc + aBc + 3aAd)x^n(ex)^m + c(aBc(2bc + 3ad) + A(b^2c^2 + 6abcd + 3a^2d^2))x^{2n}(ex)^m) dx \\ &= \frac{a^2 Ac^3(ex)^{1+m}}{e(1+m)} + (b^2 Bd^3) \int x^{6n}(ex)^m dx + (ac^2(2Abc + aBc + 3aAd) + c(aBc(2bc + 3ad) + A(b^2c^2 + 6abcd + 3a^2d^2))) \int x^{m+6n} dx \\ &= \frac{a^2 Ac^3(ex)^{1+m}}{e(1+m)} + (b^2 Bd^3 x^{-m}(ex)^m) \int x^{m+6n} dx + (ac^2(2Abc + aBc + 3aAd) + c(aBc(2bc + 3ad) + A(b^2c^2 + 6abcd + 3a^2d^2))) \int x^{m+6n} dx \\ &= \frac{ac^2(2Abc + aBc + 3aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{c(aBc(2bc + 3ad) + A(b^2c^2 + 6abcd + 3a^2d^2))x^{m+6n+1}(ex)^m}{1+m+6n+1} \end{aligned}$$

**Mathematica [A]** time = 1.52, size = 265, normalized size = 0.85

$$x^{(ex)^m} \left( \frac{cx^{2m} (A(3a^2d^2 + 6abcd + b^2c^2) + abc(3ad + 2bc))}{m+2n+1} + \frac{x^{2m} (a^2d^2(Ad + 3Bc) + 6abcd(Ad + Bc) + b^2c^2(3Ad + Bc))}{m+3n+1} + \frac{dx^{4m} (a^2Bd^2 + 2abd(Ad + 3Bc) + 3b^2c(Ad + Bc))}{m+4n+1} + \frac{a^2Ac^3}{m+1} + \frac{ac^2x^{2m}(3aAd + aBc + 2Abc)}{m+n+1} + \frac{bd^2x^{5m}(2aBd + Abd + 3Bc)}{m+5n+1} + \frac{b^2Bd^3x^{6m}}{m+6n+1} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out] x\*(e\*x)^m\*((a^2\*A\*c^3)/(1 + m) + (a\*c^2\*(2\*A\*b\*c + a\*B\*c + 3\*a\*A\*d)\*x^n)/(1 + m + n) + (c\*(a\*B\*c\*(2\*b\*c + 3\*a\*d) + A\*(b^2\*c^2 + 6\*a\*b\*c\*d + 3\*a^2\*d^2))\*x^(2\*n))/(1 + m + 2\*n) + ((6\*a\*b\*c\*d\*(B\*c + A\*d) + a^2\*d^2\*(3\*B\*c + A\*d) + b^2\*c^2\*(B\*c + 3\*A\*d))\*x^(3\*n))/(1 + m + 3\*n) + (d\*(a^2\*B\*d^2 + 3\*b^2\*c\*(B\*c + A\*d) + 2\*a\*b\*d\*(3\*B\*c + A\*d))\*x^(4\*n))/(1 + m + 4\*n) + (b\*d^2\*(3\*b\*B\*c + A\*b\*d + 2\*a\*B\*d)\*x^(5\*n))/(1 + m + 5\*n) + (b^2\*B\*d^3\*x^(6\*n))/(1 + m + 6\*n))

**IntegrateAlgebraic [F]** time = 1.01, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^3 dx$$

Verification is not applicable to the result.

[In] IntegrateAlgebraic[(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out] Defer[IntegrateAlgebraic] [(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n)^3, x]

**fricas [B]** time = 0.58, size = 6557, normalized size = 21.15

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="fricas")

[Out] ((B\*b^2\*d^3\*m^6 + 6\*B\*b^2\*d^3\*m^5 + 15\*B\*b^2\*d^3\*m^4 + 20\*B\*b^2\*d^3\*m^3 + 15\*B\*b^2\*d^3\*m^2 + 6\*B\*b^2\*d^3\*m + B\*b^2\*d^3 + 120\*(B\*b^2\*d^3\*m + B\*b^2\*d^3)\*n^5 + 274\*(B\*b^2\*d^3\*m^2 + 2\*B\*b^2\*d^3\*m + B\*b^2\*d^3)\*n^4 + 225\*(B\*b^2\*d^3\*m^3 + 3\*B\*b^2\*d^3\*m^2 + 3\*B\*b^2\*d^3\*m + B\*b^2\*d^3)\*n^3 + 85\*(B\*b^2\*d^3\*m^4 + 4\*B\*b^2\*d^3\*m^3 + 6\*B\*b^2\*d^3\*m^2 + 4\*B\*b^2\*d^3\*m + B\*b^2\*d^3)\*n^2 + 15\*(B\*b^2\*d^3\*m^5 + 5\*B\*b^2\*d^3\*m^4 + 10\*B\*b^2\*d^3\*m^3 + 10\*B\*b^2\*d^3\*m^2 + 5\*B\*b^2\*d^3\*m + B\*b^2\*d^3)\*n)\*x\*x^(6\*n)\*e^(m\*log(e) + m\*log(x)) + ((3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^6 + 3\*B\*b^2\*c\*d^2 + 6\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^5 + 144\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3 + (3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m)\*n^5 + 15\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^4 + 324\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3 + (3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m)\*n^4 + (2\*B\*a\*b + A\*b^2)\*d^3 + 20\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^3 + 260\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3 + (3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m)\*n^3 + 15\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^2 + 95\*(3\*B\*b^2\*c\*d^2 + (3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^4 + (2\*B\*a\*b + A\*b^2)\*d^3 + 4\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^3 + 6\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^2 + 4\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m)\*n^2 + 6\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m + 16\*(3\*B\*b^2\*c\*d^2 + (3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^5 + 5\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^4 + (2\*B\*a\*b + A\*b^2)\*d^3 + 10\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^3 + 10\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m^2 + 5\*(3\*B\*b^2\*c\*d^2 + (2\*B\*a\*b + A\*b^2)\*d^3)\*m)\*n)\*x\*x^(5\*n)\*e^(m\*log(e) + m\*log(x)) + ((3\*B\*b^2\*c^2\*d + 3\*(2\*B\*a\*b + A\*b^2)\*c\*d^2 + (B\*a^2 + 2\*A\*a\*b)\*d^3)\*m^6 + 3\*B\*b^2\*c^2\*d + 6\*(3\*B\*b^2\*c^2\*d + 3\*(2\*B\*a\*b + A\*b^2)\*c\*d^2 + (B\*a^2 + 2\*A\*a\*b)\*d^3)\*m^5 + 180\*(3\*B\*b^2\*c^2\*d + 3\*(2\*B\*a\*b +

$$\begin{aligned}
& A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^3 + (3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2) \\
& )*c*d^2 + (B*a^2 + 2*A*a*b)*d^3)*m)*n^5 + 15*(3*B*b^2*c^2*d + 3*(2*B*a*b + \\
& A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^3)*m^4 + 396*(3*B*b^2*c^2*d + 3*(2*B*a*b + \\
& + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^3 + (3*B*b^2*c^2*d + 3*(2*B*a*b + A*b \\
& ^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^3)*m^2 + 2*(3*B*b^2*c^2*d + 3*(2*B*a*b + A* \\
& b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^3)*m)*n^4 + 3*(2*B*a*b + A*b^2)*c*d^2 + (B \\
& *a^2 + 2*A*a*b)*d^3 + 20*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^ \\
& 2 + 2*A*a*b)*d^3)*m^3 + 307*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B \\
& *a^2 + 2*A*a*b)*d^3 + (3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + \\
& 2*A*a*b)*d^3)*m^3 + 3*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 \\
& + 2*A*a*b)*d^3)*m^2 + 3*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 \\
& + 2*A*a*b)*d^3)*m)*n^3 + 15*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + ( \\
& B*a^2 + 2*A*a*b)*d^3)*m^2 + 107*(3*B*b^2*c^2*d + (3*B*b^2*c^2*d + 3*(2*B*a* \\
& b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^3)*m^4 + 3*(2*B*a*b + A*b^2)*c*d^2 + \\
& (B*a^2 + 2*A*a*b)*d^3 + 4*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B* \\
& a^2 + 2*A*a*b)*d^3)*m^3 + 6*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B \\
& *a^2 + 2*A*a*b)*d^3)*m^2 + 4*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + ( \\
& B*a^2 + 2*A*a*b)*d^3)*m)*n^2 + 6*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 \\
& + (B*a^2 + 2*A*a*b)*d^3)*m + 17*(3*B*b^2*c^2*d + (3*B*b^2*c^2*d + 3*(2*B*a \\
& *b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^3)*m^5 + 5*(3*B*b^2*c^2*d + 3*(2*B* \\
& a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^3)*m^4 + 3*(2*B*a*b + A*b^2)*c*d^2 \\
& + (B*a^2 + 2*A*a*b)*d^3 + 10*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + \\
& (B*a^2 + 2*A*a*b)*d^3)*m^3 + 10*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 \\
& + (B*a^2 + 2*A*a*b)*d^3)*m^2 + 5*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 \\
& + (B*a^2 + 2*A*a*b)*d^3)*m)*n)*x*x^(4*n)*e^(m*log(e) + m*log(x)) + ((B*b^2 \\
& *c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m \\
& ^6 + B*b^2*c^3 + A*a^2*d^3 + 6*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2) \\
& *c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^5 + 240*(B*b^2*c^3 + A*a^2*d^3 + 3*(2 \\
& *B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2 + (B*b^2*c^3 + A*a^2*d^3 \\
& + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m)*n^5 + 15*(B*b^2 \\
& *c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m \\
& ^4 + 508*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2* \\
& A*a*b)*c*d^2 + (B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^ \\
& 2 + 2*A*a*b)*c*d^2)*m^2 + 2*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^ \\
& 2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m)*n^4 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B* \\
& a^2 + 2*A*a*b)*c*d^2 + 20*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2* \\
& d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^3 + 372*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a* \\
& b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2 + (B*b^2*c^3 + A*a^2*d^3 + 3*( \\
& 2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^3 + 3*(B*b^2*c^3 + A* \\
& a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^2 + 3*(B \\
& *b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^ \\
& 2)*m)*n^3 + 15*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^ \\
& 2 + 2*A*a*b)*c*d^2)*m^2 + 121*(B*b^2*c^3 + A*a^2*d^3 + (B*b^2*c^3 + A*a^2*d \\
& ^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^4 + 3*(2*B*a* \\
& b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2 + 4*(B*b^2*c^3 + A*a^2*d^3 + 3 \\
& *(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^3 + 6*(B*b^2*c^3 + \\
& A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^2 + 4* \\
& (B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c* \\
& d^2)*m)*n^2 + 6*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a \\
& ^2 + 2*A*a*b)*c*d^2)*m + 18*(B*b^2*c^3 + A*a^2*d^3 + (B*b^2*c^3 + A*a^2*d^3 \\
& + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^5 + 5*(B*b^2*c^ \\
& 3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^4 \\
& + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2 + 10*(B*b^2*c^3 + A \\
& *a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^3 + 10* \\
& (B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c* \\
& d^2)*m^2 + 5*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 \\
& + 2*A*a*b)*c*d^2)*m)*n)*x*x^(3*n)*e^(m*log(e) + m*log(x)) + ((3*A*a^2*c*d^2 \\
& + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^6 + 3*A*a^2*c*d^2 + \\
& 6*(3*A*a^2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^5
\end{aligned}$$



$$\begin{aligned}
& + 360*(3*A*a^2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d + \\
& (3*A*a^2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m)*n^5 \\
& + 15*(3*A*a^2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^4 \\
& + 702*(3*A*a^2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d \\
& + (3*A*a^2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^2 + \\
& 2*(3*A*a^2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m)*n \\
& ^4 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d + 20*(3*A*a^2*c*d^2 \\
& + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^3 + 461*(3*A*a^2*c*d \\
& ^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d + (3*A*a^2*c*d^2 + ( \\
& 2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^3 + 3*(3*A*a^2*c*d^2 + \\
& (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^2 + 3*(3*A*a^2*c*d^2 + \\
& (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m)*n^3 + 15*(3*A*a^2*c* \\
& d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^2 + 137*(3*A*a^2 \\
& *c*d^2 + (3*A*a^2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d \\
& )*m^4 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d + 4*(3*A*a^2*c*d^ \\
& 2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^3 + 6*(3*A*a^2*c*d \\
& ^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^2 + 4*(3*A*a^2*c* \\
& d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m)*n^2 + 6*(3*A*a^ \\
& 2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m + 19*(3*A*a^ \\
& 2*c*d^2 + (3*A*a^2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2* \\
& d)*m^5 + 5*(3*A*a^2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2 \\
& *d)*m^4 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d + 10*(3*A*a^2*c \\
& *d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^3 + 10*(3*A*a^2 \\
& *c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m^2 + 5*(3*A*a^ \\
& 2*c*d^2 + (2*B*a*b + A*b^2)*c^3 + 3*(B*a^2 + 2*A*a*b)*c^2*d)*m)*n)*x*x^(2*n \\
& )*e^(m*log(e) + m*log(x)) + ((3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^6 + \\
& 3*A*a^2*c^2*d + 6*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^5 + 720*(3*A*a^ \\
& 2*c^2*d + (B*a^2 + 2*A*a*b)*c^3 + (3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m \\
& )*n^5 + 15*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^4 + 1044*(3*A*a^2*c^2* \\
& d + (B*a^2 + 2*A*a*b)*c^3 + (3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^2 + 2 \\
& *(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m)*n^4 + (B*a^2 + 2*A*a*b)*c^3 + 2 \\
& 0*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^3 + 580*(3*A*a^2*c^2*d + (B*a^2 \\
& + 2*A*a*b)*c^3 + (3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^3 + 3*(3*A*a^2* \\
& c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^2 + 3*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c \\
& ^3)*m)*n^3 + 15*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^2 + 155*(3*A*a^2* \\
& c^2*d + (3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^4 + (B*a^2 + 2*A*a*b)*c^3 \\
& + 4*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^3 + 6*(3*A*a^2*c^2*d + (B*a^ \\
& 2 + 2*A*a*b)*c^3)*m^2 + 4*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m)*n^2 + \\
& 6*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m + 20*(3*A*a^2*c^2*d + (3*A*a^2* \\
& c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^5 + 5*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c \\
& ^3)*m^4 + (B*a^2 + 2*A*a*b)*c^3 + 10*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3 \\
& )*m^3 + 10*(3*A*a^2*c^2*d + (B*a^2 + 2*A*a*b)*c^3)*m^2 + 5*(3*A*a^2*c^2*d + \\
& (B*a^2 + 2*A*a*b)*c^3)*m)*n)*x*x^n*e^(m*log(e) + m*log(x)) + (A*a^2*c^3*m^ \\
& 6 + 720*A*a^2*c^3*n^6 + 6*A*a^2*c^3*m^5 + 15*A*a^2*c^3*m^4 + 20*A*a^2*c^3*m \\
& ^3 + 15*A*a^2*c^3*m^2 + 6*A*a^2*c^3*m + A*a^2*c^3 + 1764*(A*a^2*c^3*m + A*a \\
& ^2*c^3)*n^5 + 1624*(A*a^2*c^3*m^2 + 2*A*a^2*c^3*m + A*a^2*c^3)*n^4 + 735*(A \\
& *a^2*c^3*m^3 + 3*A*a^2*c^3*m^2 + 3*A*a^2*c^3*m + A*a^2*c^3)*n^3 + 175*(A*a^ \\
& 2*c^3*m^4 + 4*A*a^2*c^3*m^3 + 6*A*a^2*c^3*m^2 + 4*A*a^2*c^3*m + A*a^2*c^3)* \\
& n^2 + 21*(A*a^2*c^3*m^5 + 5*A*a^2*c^3*m^4 + 10*A*a^2*c^3*m^3 + 10*A*a^2*c^3 \\
& *m^2 + 5*A*a^2*c^3*m + A*a^2*c^3)*n)*x*x^n*e^(m*log(e) + m*log(x))/(m^7 + 720* \\
& (m + 1)*n^6 + 7*m^6 + 1764*(m^2 + 2*m + 1)*n^5 + 21*m^5 + 1624*(m^3 + 3*m^2 \\
& + 3*m + 1)*n^4 + 35*m^4 + 735*(m^4 + 4*m^3 + 6*m^2 + 4*m + 1)*n^3 + 35*m^3 \\
& + 175*(m^5 + 5*m^4 + 10*m^3 + 10*m^2 + 5*m + 1)*n^2 + 21*m^2 + 21*(m^6 + 6 \\
& *m^5 + 15*m^4 + 20*m^3 + 15*m^2 + 6*m + 1)*n + 7*m + 1)
\end{aligned}$$

**giac [B]** time = 1.30, size = 15358, normalized size = 49.54

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="giac")

[Out]  $(B*b^2*d^3*m^6*x*x^m*x^{(6*n)}*e^m + 15*B*b^2*d^3*m^5*n*x*x^m*x^{(6*n)}*e^m + 8*5*B*b^2*d^3*m^4*n^2*x*x^m*x^{(6*n)}*e^m + 225*B*b^2*d^3*m^3*n^3*x*x^m*x^{(6*n)}*e^m + 274*B*b^2*d^3*m^2*n^4*x*x^m*x^{(6*n)}*e^m + 120*B*b^2*d^3*m*n^5*x*x^m*x^{(6*n)}*e^m + 3*B*b^2*c*d^2*m^6*x*x^m*x^{(5*n)}*e^m + 2*B*a*b*d^3*m^6*x*x^m*x^{(5*n)}*e^m + A*b^2*d^3*m^6*x*x^m*x^{(5*n)}*e^m + 48*B*b^2*c*d^2*m^5*n*x*x^m*x^{(5*n)}*e^m + 32*B*a*b*d^3*m^5*n*x*x^m*x^{(5*n)}*e^m + 16*A*b^2*d^3*m^5*n*x*x^m*x^{(5*n)}*e^m + 285*B*b^2*c*d^2*m^4*n^2*x*x^m*x^{(5*n)}*e^m + 190*B*a*b*d^3*m^4*n^2*x*x^m*x^{(5*n)}*e^m + 95*A*b^2*d^3*m^4*n^2*x*x^m*x^{(5*n)}*e^m + 780*B*b^2*c*d^2*m^3*n^3*x*x^m*x^{(5*n)}*e^m + 520*B*a*b*d^3*m^3*n^3*x*x^m*x^{(5*n)}*e^m + 260*A*b^2*d^3*m^3*n^3*x*x^m*x^{(5*n)}*e^m + 972*B*b^2*c*d^2*m^2*n^4*x*x^m*x^{(5*n)}*e^m + 648*B*a*b*d^3*m^2*n^4*x*x^m*x^{(5*n)}*e^m + 324*A*b^2*d^3*m^2*n^4*x*x^m*x^{(5*n)}*e^m + 432*B*b^2*c*d^2*m*n^5*x*x^m*x^{(5*n)}*e^m + 288*B*a*b*d^3*m*n^5*x*x^m*x^{(5*n)}*e^m + 144*A*b^2*d^3*m*n^5*x*x^m*x^{(5*n)}*e^m + 3*B*b^2*c^2*d*m^6*x*x^m*x^{(4*n)}*e^m + 6*B*a*b*c*d^2*m^6*x*x^m*x^{(4*n)}*e^m + 3*A*b^2*c*d^2*m^6*x*x^m*x^{(4*n)}*e^m + B*a^2*d^3*m^6*x*x^m*x^{(4*n)}*e^m + 2*A*a*b*d^3*m^6*x*x^m*x^{(4*n)}*e^m + 51*B*b^2*c^2*d*m^5*n*x*x^m*x^{(4*n)}*e^m + 102*B*a*b*c*d^2*m^5*n*x*x^m*x^{(4*n)}*e^m + 51*A*b^2*c*d^2*m^5*n*x*x^m*x^{(4*n)}*e^m + 17*B*a^2*d^3*m^5*n*x*x^m*x^{(4*n)}*e^m + 34*A*a*b*d^3*m^5*n*x*x^m*x^{(4*n)}*e^m + 321*B*b^2*c^2*d*m^4*n^2*x*x^m*x^{(4*n)}*e^m + 642*B*a*b*c*d^2*m^4*n^2*x*x^m*x^{(4*n)}*e^m + 321*A*b^2*c*d^2*m^4*n^2*x*x^m*x^{(4*n)}*e^m + 107*B*a^2*d^3*m^4*n^2*x*x^m*x^{(4*n)}*e^m + 214*A*a*b*d^3*m^4*n^2*x*x^m*x^{(4*n)}*e^m + 921*B*b^2*c^2*d*m^3*n^3*x*x^m*x^{(4*n)}*e^m + 1842*B*a*b*c*d^2*m^3*n^3*x*x^m*x^{(4*n)}*e^m + 921*A*b^2*c*d^2*m^3*n^3*x*x^m*x^{(4*n)}*e^m + 307*B*a^2*d^3*m^3*n^3*x*x^m*x^{(4*n)}*e^m + 614*A*a*b*d^3*m^3*n^3*x*x^m*x^{(4*n)}*e^m + 1188*B*b^2*c^2*d*m^2*n^4*x*x^m*x^{(4*n)}*e^m + 2376*B*a*b*c*d^2*m^2*n^4*x*x^m*x^{(4*n)}*e^m + 1188*A*b^2*c*d^2*m^2*n^4*x*x^m*x^{(4*n)}*e^m + 396*B*a^2*d^3*m^2*n^4*x*x^m*x^{(4*n)}*e^m + 792*A*a*b*d^3*m^2*n^4*x*x^m*x^{(4*n)}*e^m + 540*B*b^2*c^2*d*m*n^5*x*x^m*x^{(4*n)}*e^m + 1080*B*a*b*c*d^2*m*n^5*x*x^m*x^{(4*n)}*e^m + 540*A*b^2*c*d^2*m*n^5*x*x^m*x^{(4*n)}*e^m + 180*B*a^2*d^3*m*n^5*x*x^m*x^{(4*n)}*e^m + 360*A*a*b*d^3*m*n^5*x*x^m*x^{(4*n)}*e^m + B*b^2*c^3*m^6*x*x^m*x^{(3*n)}*e^m + 6*B*a*b*c^2*d*m^6*x*x^m*x^{(3*n)}*e^m + 3*A*b^2*c^2*d*m^6*x*x^m*x^{(3*n)}*e^m + 3*B*a^2*c*d^2*m^6*x*x^m*x^{(3*n)}*e^m + 6*A*a*b*c*d^2*m^6*x*x^m*x^{(3*n)}*e^m + A*a^2*d^3*m^6*x*x^m*x^{(3*n)}*e^m + 18*B*b^2*c^3*m^5*n*x*x^m*x^{(3*n)}*e^m + 108*B*a*b*c^2*d*m^5*n*x*x^m*x^{(3*n)}*e^m + 54*A*b^2*c^2*d*m^5*n*x*x^m*x^{(3*n)}*e^m + 54*B*a^2*c*d^2*m^5*n*x*x^m*x^{(3*n)}*e^m + 108*A*a*b*c*d^2*m^5*n*x*x^m*x^{(3*n)}*e^m + 18*A*a^2*d^3*m^5*n*x*x^m*x^{(3*n)}*e^m + 121*B*b^2*c^3*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 726*B*a*b*c^2*d*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 363*A*b^2*c^2*d*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 363*B*a^2*c*d^2*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 726*A*a*b*c*d^2*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 121*A*a^2*d^3*m^4*n^2*x*x^m*x^{(3*n)}*e^m + 372*B*b^2*c^3*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 2232*B*a*b*c^2*d*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 1116*A*b^2*c^2*d*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 1116*B*a^2*c*d^2*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 2232*A*a*b*c*d^2*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 372*A*a^2*d^3*m^3*n^3*x*x^m*x^{(3*n)}*e^m + 508*B*b^2*c^3*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 3048*B*a*b*c^2*d*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 1524*A*b^2*c^2*d*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 1524*B*a^2*c*d^2*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 3048*A*a*b*c*d^2*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 508*A*a^2*d^3*m^2*n^4*x*x^m*x^{(3*n)}*e^m + 240*B*b^2*c^3*m*n^5*x*x^m*x^{(3*n)}*e^m + 1440*B*a*b*c^2*d*m*n^5*x*x^m*x^{(3*n)}*e^m + 720*A*b^2*c^2*d*m*n^5*x*x^m*x^{(3*n)}*e^m + 720*B*a^2*c*d^2*m*n^5*x*x^m*x^{(3*n)}*e^m + 1440*A*a*b*c*d^2*m*n^5*x*x^m*x^{(3*n)}*e^m + 240*A*a^2*d^3*m*n^5*x*x^m*x^{(3*n)}*e^m + 2*B*a*b*c^3*m^6*x*x^m*x^{(2*n)}*e^m + A*b^2*c^3*m^6*x*x^m*x^{(2*n)}*e^m + 3*B*a^2*c^2*d*m^6*x*x^m*x^{(2*n)}*e^m + 6*A*a*b*c^2*d*m^6*x*x^m*x^{(2*n)}*e^m + 3*A*a^2*c*d^2*m^6*x*x^m*x^{(2*n)}*e^m + 38*B*a*b*c^3*m^5*n*x*x^m*x^{(2*n)}*e^m + 19*A*b^2*c^3*m^5*n*x*x^m*x^{(2*n)}*e^m + 57*B*a^2*c^2*d*m^5*n*x*x^m*x^{(2*n)}*e^m + 114*A*a*b*c^2*d*m^5*n*x*x^m*x^{(2*n)}*e^m + 57*A*a^2*c*d^2*m^5*n*x*x^m*x^{(2*n)}*e^m + 274*B*a*b*c^3*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 137*A*b^2*c^3*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 411*B*a^2*c^2*d*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 822*A*a*b*c^2*d*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 411*A*a^2*c*d^2*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 922*B*a*b*c^3*m^3*n^3*x*x^m*x^{(2*n)}*e^m$



$$\begin{aligned}
& d^3 m^3 n^2 x x^m x^{(3n)} e^m + 1116 B b^2 c^3 m^2 n^3 x x^m x^{(3n)} e^m + \\
& 6696 B a b c^2 d m^2 n^3 x x^m x^{(3n)} e^m + 3348 A b^2 c^2 d m^2 n^3 x x^m \\
& x^{(3n)} e^m + 3348 B a^2 c d^2 m^2 n^3 x x^m x^{(3n)} e^m + 6696 A a b c d^2 \\
& m^2 n^3 x x^m x^{(3n)} e^m + 1116 A a^2 d^3 m^2 n^3 x x^m x^{(3n)} e^m + 10 \\
& 16 B b^2 c^3 m n^4 x x^m x^{(3n)} e^m + 6096 B a b c^2 d m n^4 x x^m x^{(3n)} \\
& e^m + 3048 A b^2 c^2 d m n^4 x x^m x^{(3n)} e^m + 3048 B a^2 c d^2 m n^4 x x \\
& x^m x^{(3n)} e^m + 6096 A a b c d^2 m n^4 x x^m x^{(3n)} e^m + 1016 A a^2 d^3 \\
& m n^4 x x^m x^{(3n)} e^m + 240 B b^2 c^3 m^5 x x^m x^{(3n)} e^m + 1440 B a b \\
& c^2 d n^5 x x^m x^{(3n)} e^m + 720 A b^2 c^2 d n^5 x x^m x^{(3n)} e^m + 720 \\
& B a^2 c d^2 n^5 x x^m x^{(3n)} e^m + 1440 A a b c d^2 n^5 x x^m x^{(3n)} e^m \\
& + 240 A a^2 d^3 n^5 x x^m x^{(3n)} e^m + 12 B a b c^3 m^5 x x^m x^{(2n)} e^m \\
& + 6 A b^2 c^3 m^5 x x^m x^{(2n)} e^m + 18 B a^2 c^2 d m^5 x x^m x^{(2n)} e^m \\
& + 36 A a b c^2 d m^5 x x^m x^{(2n)} e^m + 18 A a^2 c d^2 m^5 x x^m x^{(2n)} e \\
& m + 190 B a b c^3 m^4 n x x^m x^{(2n)} e^m + 95 A b^2 c^3 m^4 n x x^m x^{(2n)} \\
& e^m + 285 B a^2 c^2 d m^4 n x x^m x^{(2n)} e^m + 570 A a b c^2 d m^4 n x x \\
& x^m x^{(2n)} e^m + 285 A a^2 c d^2 m^4 n x x^m x^{(2n)} e^m + 1096 B a b c^3 m \\
& m^3 n^2 x x^m x^{(2n)} e^m + 548 A b^2 c^3 m^3 n^2 x x^m x^{(2n)} e^m + 1644 B \\
& B a^2 c^2 d m^3 n^2 x x^m x^{(2n)} e^m + 3288 A a b c^2 d m^3 n^2 x x^m x^{(2n)} \\
& e^m + 1644 A a^2 c d^2 m^3 n^2 x x^m x^{(2n)} e^m + 2766 B a b c^3 m^2 n \\
& ^3 x x^m x^{(2n)} e^m + 1383 A b^2 c^3 m^2 n^3 x x^m x^{(2n)} e^m + 4149 B a^2 \\
& c^2 d m^2 n^3 x x^m x^{(2n)} e^m + 8298 A a b c^2 d m^2 n^3 x x^m x^{(2n)} e \\
& m + 4149 A a^2 c d^2 m^2 n^3 x x^m x^{(2n)} e^m + 2808 B a b c^3 m n^4 x x \\
& x^m x^{(2n)} e^m + 1404 A b^2 c^3 m n^4 x x^m x^{(2n)} e^m + 4212 B a^2 c^2 d \\
& m n^4 x x^m x^{(2n)} e^m + 8424 A a b c^2 d m n^4 x x^m x^{(2n)} e^m + 4212 A \\
& a^2 c d^2 m n^4 x x^m x^{(2n)} e^m + 720 B a b c^3 n^5 x x^m x^{(2n)} e^m + \\
& 360 A b^2 c^3 n^5 x x^m x^{(2n)} e^m + 1080 B a^2 c^2 d n^5 x x^m x^{(2n)} e \\
& m + 2160 A a b c^2 d n^5 x x^m x^{(2n)} e^m + 1080 A a^2 c d^2 n^5 x x^m x^{(2n)} \\
& e^m + 6 B a^2 c^3 m^5 x x^m x^n e^m + 12 A a b c^3 m^5 x x^m x^n e^m + \\
& 18 A a^2 c^2 d m^5 x x^m x^n e^m + 100 B a^2 c^3 m^4 n x x^m x^n e^m + 200 \\
& A a b c^3 m^4 n x x^m x^n e^m + 300 A a^2 c^2 d m^4 n x x^m x^n e^m + 620 B \\
& B a^2 c^3 m^3 n^2 x x^m x^n e^m + 1240 A a b c^3 m^3 n^2 x x^m x^n e^m + 18 \\
& 60 A a^2 c^2 d m^3 n^2 x x^m x^n e^m + 1740 B a^2 c^3 m^2 n^3 x x^m x^n e^m \\
& + 3480 A a b c^3 m^2 n^3 x x^m x^n e^m + 5220 A a^2 c^2 d m^2 n^3 x x^m x^n \\
& e^m + 2088 B a^2 c^3 m n^4 x x^m x^n e^m + 4176 A a b c^3 m n^4 x x^m x^n \\
& e^m + 6264 A a^2 c^2 d m n^4 x x^m x^n e^m + 720 B a^2 c^3 n^5 x x^m x^n e \\
& m + 1440 A a b c^3 n^5 x x^m x^n e^m + 2160 A a^2 c^2 d n^5 x x^m x^n e^m \\
& + 6 A a^2 c^3 m^5 x x^m e^m + 105 A a^2 c^3 m^4 n x x^m e^m + 700 A a^2 c^3 \\
& m^3 n^2 x x^m e^m + 2205 A a^2 c^3 m^2 n^3 x x^m e^m + 3248 A a^2 c^3 m n^4 \\
& x x^m e^m + 1764 A a^2 c^3 n^5 x x^m e^m + 15 B b^2 d^3 m^4 x x^m x^{(6n)} \\
& e^m + 150 B b^2 d^3 m^3 n x x^m x^{(6n)} e^m + 510 B b^2 d^3 m^2 n^2 x x^m \\
& x^{(6n)} e^m + 675 B b^2 d^3 m n^3 x x^m x^{(6n)} e^m + 274 B b^2 d^3 n^4 x x \\
& x^m x^{(6n)} e^m + 45 B b^2 c d^2 m^4 x x^m x^{(5n)} e^m + 30 B a b d^3 m^4 x x \\
& x^m x^{(5n)} e^m + 15 A b^2 d^3 m^4 x x^m x^{(5n)} e^m + 480 B b^2 c d^2 m^3 \\
& n x x^m x^{(5n)} e^m + 320 B a b d^3 m^3 n x x^m x^{(5n)} e^m + 160 A b^2 d^3 \\
& m^3 n x x^m x^{(5n)} e^m + 1710 B b^2 c d^2 m^2 n^2 x x^m x^{(5n)} e^m + 114 \\
& 0 B a b d^3 m^2 n^2 x x^m x^{(5n)} e^m + 570 A b^2 d^3 m^2 n^2 x x^m x^{(5n)} \\
& e^m + 2340 B b^2 c d^2 m n^3 x x^m x^{(5n)} e^m + 1560 B a b d^3 m n^3 x x \\
& m x^{(5n)} e^m + 780 A b^2 d^3 m n^3 x x^m x^{(5n)} e^m + 972 B b^2 c d^2 n^4 \\
& x x^m x^{(5n)} e^m + 648 B a b d^3 n^4 x x^m x^{(5n)} e^m + 324 A b^2 d^3 n^4 \\
& x x^m x^{(5n)} e^m + 45 B b^2 c^2 d m^4 x x^m x^{(4n)} e^m + 90 B a b c d^2 \\
& m^4 x x^m x^{(4n)} e^m + 45 A b^2 c d^2 m^4 x x^m x^{(4n)} e^m + 15 B a^2 d^3 \\
& m^4 x x^m x^{(4n)} e^m + 30 A a b d^3 m^4 x x^m x^{(4n)} e^m + 510 B b^2 c^2 \\
& d m^3 n x x^m x^{(4n)} e^m + 1020 B a b c d^2 m^3 n x x^m x^{(4n)} e^m + 51 \\
& 0 A b^2 c d^2 m^3 n x x^m x^{(4n)} e^m + 170 B a^2 d^3 m^3 n x x^m x^{(4n)} e \\
& m + 340 A a b d^3 m^3 n x x^m x^{(4n)} e^m + 1926 B b^2 c^2 d m^2 n^2 x x^m \\
& x^{(4n)} e^m + 3852 B a b c d^2 m^2 n^2 x x^m x^{(4n)} e^m + 1926 A b^2 c d^2 \\
& m^2 n^2 x x^m x^{(4n)} e^m + 642 B a^2 d^3 m^2 n^2 x x^m x^{(4n)} e^m + 128 \\
& 4 A a b d^3 m^2 n^2 x x^m x^{(4n)} e^m + 2763 B b^2 c^2 d m n^3 x x^m x^{(4n)} \\
& e^m + 5526 B a b c d^2 m n^3 x x^m x^{(4n)} e^m + 2763 A b^2 c d^2 m n^3 x
\end{aligned}$$

$$\begin{aligned}
& *x^m*x^{(4*n)}*e^m + 921*B*a^2*d^3*m*n^3*x*x^m*x^{(4*n)}*e^m + 1842*A*a*b*d^3*m \\
& *n^3*x*x^m*x^{(4*n)}*e^m + 1188*B*b^2*c^2*d*n^4*x*x^m*x^{(4*n)}*e^m + 2376*B*a* \\
& b*c*d^2*n^4*x*x^m*x^{(4*n)}*e^m + 1188*A*b^2*c*d^2*n^4*x*x^m*x^{(4*n)}*e^m + 39 \\
& 6*B*a^2*d^3*n^4*x*x^m*x^{(4*n)}*e^m + 792*A*a*b*d^3*n^4*x*x^m*x^{(4*n)}*e^m + 1 \\
& 5*B*b^2*c^3*m^4*x*x^m*x^{(3*n)}*e^m + 90*B*a*b*c^2*d*m^4*x*x^m*x^{(3*n)}*e^m + \\
& 45*A*b^2*c^2*d*m^4*x*x^m*x^{(3*n)}*e^m + 45*B*a^2*c*d^2*m^4*x*x^m*x^{(3*n)}*e^m \\
& + 90*A*a*b*c*d^2*m^4*x*x^m*x^{(3*n)}*e^m + 15*A*a^2*d^3*m^4*x*x^m*x^{(3*n)}*e^m \\
& + 180*B*b^2*c^3*m^3*n*x*x^m*x^{(3*n)}*e^m + 1080*B*a*b*c^2*d*m^3*n*x*x^m*x^{(3*n)} \\
& *e^m + 540*A*b^2*c^2*d*m^3*n*x*x^m*x^{(3*n)}*e^m + 540*B*a^2*c*d^2*m^3*n \\
& *x*x^m*x^{(3*n)}*e^m + 1080*A*a*b*c*d^2*m^3*n*x*x^m*x^{(3*n)}*e^m + 180*A*a^2*d \\
& ^3*m^3*n*x*x^m*x^{(3*n)}*e^m + 726*B*b^2*c^3*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 4356 \\
& *B*a*b*c^2*d*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 2178*A*b^2*c^2*d*m^2*n^2*x*x^m*x^{(3 \\
& *n)}*e^m + 2178*B*a^2*c*d^2*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 4356*A*a*b*c*d^2*m^2 \\
& *n^2*x*x^m*x^{(3*n)}*e^m + 726*A*a^2*d^3*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 1116*B* \\
& b^2*c^3*m*n^3*x*x^m*x^{(3*n)}*e^m + 6696*B*a*b*c^2*d*m*n^3*x*x^m*x^{(3*n)}*e^m \\
& + 3348*A*b^2*c^2*d*m*n^3*x*x^m*x^{(3*n)}*e^m + 3348*B*a^2*c*d^2*m*n^3*x*x^m*x \\
& ^{(3*n)}*e^m + 6696*A*a*b*c*d^2*m*n^3*x*x^m*x^{(3*n)}*e^m + 1116*A*a^2*d^3*m*n^3 \\
& *x*x^m*x^{(3*n)}*e^m + 508*B*b^2*c^3*n^4*x*x^m*x^{(3*n)}*e^m + 3048*B*a*b*c^2* \\
& d*n^4*x*x^m*x^{(3*n)}*e^m + 1524*A*b^2*c^2*d*n^4*x*x^m*x^{(3*n)}*e^m + 1524*B*a \\
& ^2*c*d^2*n^4*x*x^m*x^{(3*n)}*e^m + 3048*A*a*b*c*d^2*n^4*x*x^m*x^{(3*n)}*e^m + 5 \\
& 08*A*a^2*d^3*n^4*x*x^m*x^{(3*n)}*e^m + 30*B*a*b*c^3*m^4*x*x^m*x^{(2*n)}*e^m + 1 \\
& 5*A*b^2*c^3*m^4*x*x^m*x^{(2*n)}*e^m + 45*B*a^2*c^2*d*m^4*x*x^m*x^{(2*n)}*e^m + \\
& 90*A*a*b*c^2*d*m^4*x*x^m*x^{(2*n)}*e^m + 45*A*a^2*c*d^2*m^4*x*x^m*x^{(2*n)}*e^m \\
& + 380*B*a*b*c^3*m^3*n*x*x^m*x^{(2*n)}*e^m + 190*A*b^2*c^3*m^3*n*x*x^m*x^{(2*n)} \\
& *e^m + 570*B*a^2*c^2*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 1140*A*a*b*c^2*d*m^3*n*x*x \\
& ^m*x^{(2*n)}*e^m + 570*A*a^2*c*d^2*m^3*n*x*x^m*x^{(2*n)}*e^m + 1644*B*a*b*c^3*m \\
& ^2*n^2*x*x^m*x^{(2*n)}*e^m + 822*A*b^2*c^3*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 2466*B \\
& *a^2*c^2*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 4932*A*a*b*c^2*d*m^2*n^2*x*x^m*x^{(2 \\
& *n)}*e^m + 2466*A*a^2*c*d^2*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 2766*B*a*b*c^3*m*n^3 \\
& *x*x^m*x^{(2*n)}*e^m + 1383*A*b^2*c^3*m*n^3*x*x^m*x^{(2*n)}*e^m + 4149*B*a^2*c^2 \\
& *d*m*n^3*x*x^m*x^{(2*n)}*e^m + 8298*A*a*b*c^2*d*m*n^3*x*x^m*x^{(2*n)}*e^m + 41 \\
& 49*A*a^2*c*d^2*m*n^3*x*x^m*x^{(2*n)}*e^m + 1404*B*a*b*c^3*n^4*x*x^m*x^{(2*n)}*e \\
& ^m + 702*A*b^2*c^3*n^4*x*x^m*x^{(2*n)}*e^m + 2106*B*a^2*c^2*d*n^4*x*x^m*x^{(2* \\
& n)}*e^m + 4212*A*a*b*c^2*d*n^4*x*x^m*x^{(2*n)}*e^m + 2106*A*a^2*c*d^2*n^4*x*x^ \\
& m*x^{(2*n)}*e^m + 15*B*a^2*c^3*m^4*x*x^m*x^n*e^m + 30*A*a*b*c^3*m^4*x*x^m*x^n \\
& *e^m + 45*A*a^2*c^2*d*m^4*x*x^m*x^n*e^m + 200*B*a^2*c^3*m^3*n*x*x^m*x^n*e^m \\
& + 400*A*a*b*c^3*m^3*n*x*x^m*x^n*e^m + 600*A*a^2*c^2*d*m^3*n*x*x^m*x^n*e^m \\
& + 930*B*a^2*c^3*m^2*n^2*x*x^m*x^n*e^m + 1860*A*a*b*c^3*m^2*n^2*x*x^m*x^n*e^m \\
& + 2790*A*a^2*c^2*d*m^2*n^2*x*x^m*x^n*e^m + 1740*B*a^2*c^3*m*n^3*x*x^m*x^n \\
& *e^m + 3480*A*a*b*c^3*m*n^3*x*x^m*x^n*e^m + 5220*A*a^2*c^2*d*m*n^3*x*x^m*x^n \\
& *e^m + 1044*B*a^2*c^3*n^4*x*x^m*x^n*e^m + 2088*A*a*b*c^3*n^4*x*x^m*x^n*e^m \\
& + 3132*A*a^2*c^2*d*n^4*x*x^m*x^n*e^m + 15*A*a^2*c^3*m^4*x*x^m*e^m + 210*A* \\
& a^2*c^3*m^3*n*x*x^m*e^m + 1050*A*a^2*c^3*m^2*n^2*x*x^m*e^m + 2205*A*a^2*c^3 \\
& *m*n^3*x*x^m*e^m + 1624*A*a^2*c^3*n^4*x*x^m*e^m + 20*B*b^2*d^3*m^3*x*x^m*x^{(6*n)} \\
& *e^m + 150*B*b^2*d^3*m^2*n*x*x^m*x^{(6*n)}*e^m + 340*B*b^2*d^3*m*n^2*x*x^ \\
& ^m*x^{(6*n)}*e^m + 225*B*b^2*d^3*n^3*x*x^m*x^{(6*n)}*e^m + 60*B*b^2*c*d^2*m^3*x \\
& ^m*x^{(5*n)}*e^m + 40*B*a*b*d^3*m^3*x*x^m*x^{(5*n)}*e^m + 20*A*b^2*d^3*m^3*x* \\
& x^m*x^{(5*n)}*e^m + 480*B*b^2*c*d^2*m^2*n*x*x^m*x^{(5*n)}*e^m + 320*B*a*b*d^3*m \\
& ^2*n*x*x^m*x^{(5*n)}*e^m + 160*A*b^2*d^3*m^2*n*x*x^m*x^{(5*n)}*e^m + 1140*B*b^2 \\
& *c*d^2*m*n^2*x*x^m*x^{(5*n)}*e^m + 760*B*a*b*d^3*m*n^2*x*x^m*x^{(5*n)}*e^m + 38 \\
& 0*A*b^2*d^3*m*n^2*x*x^m*x^{(5*n)}*e^m + 780*B*b^2*c*d^2*n^3*x*x^m*x^{(5*n)}*e^m \\
& + 520*B*a*b*d^3*n^3*x*x^m*x^{(5*n)}*e^m + 260*A*b^2*d^3*n^3*x*x^m*x^{(5*n)}*e^ \\
& m + 60*B*b^2*c^2*d*m^3*x*x^m*x^{(4*n)}*e^m + 120*B*a*b*c*d^2*m^3*x*x^m*x^{(4*n)} \\
& *e^m + 60*A*b^2*c*d^2*m^3*x*x^m*x^{(4*n)}*e^m + 20*B*a^2*d^3*m^3*x*x^m*x^{(4* \\
& n)}*e^m + 40*A*a*b*d^3*m^3*x*x^m*x^{(4*n)}*e^m + 510*B*b^2*c^2*d*m^2*n*x*x^m*x \\
& ^{(4*n)}*e^m + 1020*B*a*b*c*d^2*m^2*n*x*x^m*x^{(4*n)}*e^m + 510*A*b^2*c*d^2*m^2 \\
& *n*x*x^m*x^{(4*n)}*e^m + 170*B*a^2*d^3*m^2*n*x*x^m*x^{(4*n)}*e^m + 340*A*a*b*d^ \\
& 3*m^2*n*x*x^m*x^{(4*n)}*e^m + 1284*B*b^2*c^2*d*m*n^2*x*x^m*x^{(4*n)}*e^m + 2568 \\
& *B*a*b*c*d^2*m*n^2*x*x^m*x^{(4*n)}*e^m + 1284*A*b^2*c*d^2*m*n^2*x*x^m*x^{(4*n)}
\end{aligned}$$

$$\begin{aligned}
& *e^m + 428*B*a^2*d^3*m*n^2*x*x^m*x^{(4*n)}*e^m + 856*A*a*b*d^3*m*n^2*x*x^m*x^{(4*n)}*e^m + 921*B*b^2*c^2*d*n^3*x*x^m*x^{(4*n)}*e^m + 1842*B*a*b*c*d^2*n^3*x*x^m*x^{(4*n)}*e^m + 921*A*b^2*c*d^2*n^3*x*x^m*x^{(4*n)}*e^m + 307*B*a^2*d^3*n^3*x*x^m*x^{(4*n)}*e^m + 614*A*a*b*d^3*n^3*x*x^m*x^{(4*n)}*e^m + 20*B*b^2*c^3*m^3*x*x^m*x^{(3*n)}*e^m + 120*B*a*b*c^2*d*m^3*x*x^m*x^{(3*n)}*e^m + 60*A*b^2*c^2*d*m^3*x*x^m*x^{(3*n)}*e^m + 60*B*a^2*c*d^2*m^3*x*x^m*x^{(3*n)}*e^m + 120*A*a*b*c*d^2*m^3*x*x^m*x^{(3*n)}*e^m + 20*A*a^2*d^3*m^3*x*x^m*x^{(3*n)}*e^m + 180*B*b^2*c^3*m^2*n*x*x^m*x^{(3*n)}*e^m + 1080*B*a*b*c^2*d*m^2*n*x*x^m*x^{(3*n)}*e^m + 540*A*b^2*c^2*d*m^2*n*x*x^m*x^{(3*n)}*e^m + 540*B*a^2*c*d^2*m^2*n*x*x^m*x^{(3*n)}*e^m + 1080*A*a*b*c*d^2*m^2*n*x*x^m*x^{(3*n)}*e^m + 180*A*a^2*d^3*m^2*n*x*x^m*x^{(3*n)}*e^m + 484*B*b^2*c^3*m*n^2*x*x^m*x^{(3*n)}*e^m + 2904*B*a*b*c^2*d*m*n^2*x*x^m*x^{(3*n)}*e^m + 1452*A*b^2*c^2*d*m*n^2*x*x^m*x^{(3*n)}*e^m + 1452*B*a^2*c*d^2*m*n^2*x*x^m*x^{(3*n)}*e^m + 2904*A*a*b*c*d^2*m*n^2*x*x^m*x^{(3*n)}*e^m + 484*A*a^2*d^3*m*n^2*x*x^m*x^{(3*n)}*e^m + 372*B*b^2*c^3*n^3*x*x^m*x^{(3*n)}*e^m + 2232*B*a*b*c^2*d*n^3*x*x^m*x^{(3*n)}*e^m + 1116*A*b^2*c^2*d*n^3*x*x^m*x^{(3*n)}*e^m + 1116*B*a^2*c*d^2*n^3*x*x^m*x^{(3*n)}*e^m + 2232*A*a*b*c*d^2*n^3*x*x^m*x^{(3*n)}*e^m + 372*A*a^2*d^3*n^3*x*x^m*x^{(3*n)}*e^m + 40*B*a*b*c^3*m^3*x*x^m*x^{(2*n)}*e^m + 20*A*b^2*c^3*m^3*x*x^m*x^{(2*n)}*e^m + 60*B*a^2*c^2*d*m^3*x*x^m*x^{(2*n)}*e^m + 120*A*a*b*c^2*d*m^3*x*x^m*x^{(2*n)}*e^m + 60*A*a^2*c*d^2*m^3*x*x^m*x^{(2*n)}*e^m + 380*B*a*b*c^3*m^2*n*x*x^m*x^{(2*n)}*e^m + 190*A*b^2*c^3*m^2*n*x*x^m*x^{(2*n)}*e^m + 570*B*a^2*c^2*d*m^2*n*x*x^m*x^{(2*n)}*e^m + 1140*A*a*b*c^2*d*m^2*n*x*x^m*x^{(2*n)}*e^m + 570*A*a^2*c*d^2*m^2*n*x*x^m*x^{(2*n)}*e^m + 1096*B*a*b*c^3*m*n^2*x*x^m*x^{(2*n)}*e^m + 548*A*b^2*c^3*m*n^2*x*x^m*x^{(2*n)}*e^m + 1644*B*a^2*c^2*d*m*n^2*x*x^m*x^{(2*n)}*e^m + 3288*A*a*b*c^2*d*m*n^2*x*x^m*x^{(2*n)}*e^m + 1644*A*a^2*c*d^2*m*n^2*x*x^m*x^{(2*n)}*e^m + 922*B*a*b*c^3*n^3*x*x^m*x^{(2*n)}*e^m + 461*A*b^2*c^3*n^3*x*x^m*x^{(2*n)}*e^m + 1383*B*a^2*c^2*d*n^3*x*x^m*x^{(2*n)}*e^m + 2766*A*a*b*c^2*d*n^3*x*x^m*x^{(2*n)}*e^m + 1383*A*a^2*c*d^2*n^3*x*x^m*x^{(2*n)}*e^m + 20*B*a^2*c^3*m^3*x*x^m*x^n*e^m + 40*A*a*b*c^3*m^3*x*x^m*x^n*e^m + 60*A*a^2*c^2*d*m^3*x*x^m*x^n*e^m + 200*B*a^2*c^3*m^2*n*x*x^m*x^n*e^m + 400*A*a*b*c^3*m^2*n*x*x^m*x^n*e^m + 600*A*a^2*c^2*d*m^2*n*x*x^m*x^n*e^m + 620*B*a^2*c^3*m*n^2*x*x^m*x^n*e^m + 1240*A*a*b*c^3*m*n^2*x*x^m*x^n*e^m + 1860*A*a^2*c^2*d*m*n^2*x*x^m*x^n*e^m + 580*B*a^2*c^3*n^3*x*x^m*x^n*e^m + 1160*A*a*b*c^3*n^3*x*x^m*x^n*e^m + 1740*A*a^2*c^2*d*n^3*x*x^m*x^n*e^m + 20*A*a^2*c^3*m^3*x*x^m*e^m + 210*A*a^2*c^3*m^2*n*x*x^m*e^m + 700*A*a^2*c^3*m*n^2*x*x^m*e^m + 735*A*a^2*c^3*n^3*x*x^m*e^m + 15*B*b^2*d^3*m^2*x*x^m*x^{(6*n)}*e^m + 75*B*b^2*d^3*m*n*x*x^m*x^{(6*n)}*e^m + 85*B*b^2*d^3*n^2*x*x^m*x^{(6*n)}*e^m + 45*B*b^2*c*d^2*m^2*x*x^m*x^{(5*n)}*e^m + 30*B*a*b*d^3*m^2*x*x^m*x^{(5*n)}*e^m + 15*A*b^2*d^3*m^2*x*x^m*x^{(5*n)}*e^m + 240*B*b^2*c*d^2*m*n*x*x^m*x^{(5*n)}*e^m + 160*B*a*b*d^3*m*n*x*x^m*x^{(5*n)}*e^m + 80*A*b^2*d^3*m*n*x*x^m*x^{(5*n)}*e^m + 285*B*b^2*c*d^2*n^2*x*x^m*x^{(5*n)}*e^m + 190*B*a*b*d^3*n^2*x*x^m*x^{(5*n)}*e^m + 95*A*b^2*d^3*n^2*x*x^m*x^{(5*n)}*e^m + 45*B*b^2*c^2*d*m^2*x*x^m*x^{(4*n)}*e^m + 90*B*a*b*c*d^2*m^2*x*x^m*x^{(4*n)}*e^m + 45*A*b^2*c*d^2*m^2*x*x^m*x^{(4*n)}*e^m + 15*B*a^2*d^3*m^2*x*x^m*x^{(4*n)}*e^m + 30*A*a*b*d^3*m^2*x*x^m*x^{(4*n)}*e^m + 255*B*b^2*c^2*d*m*n*x*x^m*x^{(4*n)}*e^m + 510*B*a*b*c*d^2*m*n*x*x^m*x^{(4*n)}*e^m + 255*A*b^2*c*d^2*m*n*x*x^m*x^{(4*n)}*e^m + 85*B*a^2*d^3*m*n*x*x^m*x^{(4*n)}*e^m + 170*A*a*b*d^3*m*n*x*x^m*x^{(4*n)}*e^m + 321*B*b^2*c^2*d*n^2*x*x^m*x^{(4*n)}*e^m + 642*B*a*b*c*d^2*n^2*x*x^m*x^{(4*n)}*e^m + 321*A*b^2*c*d^2*n^2*x*x^m*x^{(4*n)}*e^m + 107*B*a^2*d^3*n^2*x*x^m*x^{(4*n)}*e^m + 214*A*a*b*d^3*n^2*x*x^m*x^{(4*n)}*e^m + 15*B*b^2*c^3*m^2*x*x^m*x^{(3*n)}*e^m + 90*B*a*b*c^2*d*m^2*x*x^m*x^{(3*n)}*e^m + 45*A*b^2*c^2*d*m^2*x*x^m*x^{(3*n)}*e^m + 45*B*a^2*c*d^2*m^2*x*x^m*x^{(3*n)}*e^m + 90*A*a*b*c*d^2*m^2*x*x^m*x^{(3*n)}*e^m + 15*A*a^2*d^3*m^2*x*x^m*x^{(3*n)}*e^m + 90*B*b^2*c^3*m*n*x*x^m*x^{(3*n)}*e^m + 540*B*a*b*c^2*d*m*n*x*x^m*x^{(3*n)}*e^m + 270*A*b^2*c^2*d*m*n*x*x^m*x^{(3*n)}*e^m + 270*B*a^2*c*d^2*m*n*x*x^m*x^{(3*n)}*e^m + 540*A*a*b*c*d^2*m*n*x*x^m*x^{(3*n)}*e^m + 90*A*a^2*d^3*m*n*x*x^m*x^{(3*n)}*e^m + 121*B*b^2*c^3*n^2*x*x^m*x^{(3*n)}*e^m + 726*B*a*b*c^2*d*n^2*x*x^m*x^{(3*n)}*e^m + 363*A*b^2*c^2*d*n^2*x*x^m*x^{(3*n)}*e^m + 363*B*a^2*c*d^2*n^2*x*x^m*x^{(3*n)}*e^m + 726*A*a*b*c*d^2*n^2*x*x^m*x^{(3*n)}*e^m + 121*A*a^2*d^3*n^2*x*x^m*x^{(3*n)}*e^m + 30*B*a*b*c^3*m^2*x*x^m*x^{(2*n)}*e^m + 15*A*b^2*c^3*m^2*x*x^m*x^{(2*n)}*e^m
\end{aligned}$$

$$\begin{aligned}
& + 45*B*a^2*c^2*d*m^2*x*x^m*x^(2*n)*e^m + 90*A*a*b*c^2*d*m^2*x*x^m*x^(2*n)* \\
& e^m + 45*A*a^2*c*d^2*m^2*x*x^m*x^(2*n)*e^m + 190*B*a*b*c^3*m*n*x*x^m*x^(2*n) \\
& )*e^m + 95*A*b^2*c^3*m*n*x*x^m*x^(2*n)*e^m + 285*B*a^2*c^2*d*m*n*x*x^m*x^(2 \\
& *n)*e^m + 570*A*a*b*c^2*d*m*n*x*x^m*x^(2*n)*e^m + 285*A*a^2*c*d^2*m*n*x*x^m \\
& *x^(2*n)*e^m + 274*B*a*b*c^3*n^2*x*x^m*x^(2*n)*e^m + 137*A*b^2*c^3*n^2*x*x^ \\
& m*x^(2*n)*e^m + 411*B*a^2*c^2*d*n^2*x*x^m*x^(2*n)*e^m + 822*A*a*b*c^2*d*n^2 \\
& *x*x^m*x^(2*n)*e^m + 411*A*a^2*c*d^2*n^2*x*x^m*x^(2*n)*e^m + 15*B*a^2*c^3*m \\
& ^2*x*x^m*x^n*e^m + 30*A*a*b*c^3*m^2*x*x^m*x^n*e^m + 45*A*a^2*c^2*d*m^2*x*x^ \\
& m*x^n*e^m + 100*B*a^2*c^3*m*n*x*x^m*x^n*e^m + 200*A*a*b*c^3*m*n*x*x^m*x^n*e \\
& ^m + 300*A*a^2*c^2*d*m*n*x*x^m*x^n*e^m + 155*B*a^2*c^3*n^2*x*x^m*x^n*e^m + \\
& 310*A*a*b*c^3*n^2*x*x^m*x^n*e^m + 465*A*a^2*c^2*d*n^2*x*x^m*x^n*e^m + 15*A* \\
& a^2*c^3*m^2*x*x^m*e^m + 105*A*a^2*c^3*m*n*x*x^m*e^m + 175*A*a^2*c^3*n^2*x*x \\
& ^m*e^m + 6*B*b^2*d^3*m*x*x^m*x^(6*n)*e^m + 15*B*b^2*d^3*n*x*x^m*x^(6*n)*e^m \\
& + 18*B*b^2*c*d^2*m*x*x^m*x^(5*n)*e^m + 12*B*a*b*d^3*m*x*x^m*x^(5*n)*e^m + \\
& 6*A*b^2*d^3*m*x*x^m*x^(5*n)*e^m + 48*B*b^2*c*d^2*n*x*x^m*x^(5*n)*e^m + 32*B \\
& *a*b*d^3*n*x*x^m*x^(5*n)*e^m + 16*A*b^2*d^3*n*x*x^m*x^(5*n)*e^m + 18*B*b^2* \\
& c^2*d*m*x*x^m*x^(4*n)*e^m + 36*B*a*b*c*d^2*m*x*x^m*x^(4*n)*e^m + 18*A*b^2*c \\
& *d^2*m*x*x^m*x^(4*n)*e^m + 6*B*a^2*d^3*m*x*x^m*x^(4*n)*e^m + 12*A*a*b*d^3*m \\
& *x*x^m*x^(4*n)*e^m + 51*B*b^2*c^2*d*n*x*x^m*x^(4*n)*e^m + 102*B*a*b*c*d^2*n \\
& *x*x^m*x^(4*n)*e^m + 51*A*b^2*c*d^2*n*x*x^m*x^(4*n)*e^m + 17*B*a^2*d^3*n*x* \\
& x^m*x^(4*n)*e^m + 34*A*a*b*d^3*n*x*x^m*x^(4*n)*e^m + 6*B*b^2*c^3*m*x*x^m*x^ \\
& (3*n)*e^m + 36*B*a*b*c^2*d*m*x*x^m*x^(3*n)*e^m + 18*A*b^2*c^2*d*m*x*x^m*x^ \\
& (3*n)*e^m + 18*B*a^2*c*d^2*m*x*x^m*x^(3*n)*e^m + 36*A*a*b*c*d^2*m*x*x^m*x^ \\
& (3*n)*e^m + 6*A*a^2*d^3*m*x*x^m*x^(3*n)*e^m + 18*B*b^2*c^3*n*x*x^m*x^(3*n)*e^ \\
& m + 108*B*a*b*c^2*d*n*x*x^m*x^(3*n)*e^m + 54*A*b^2*c^2*d*n*x*x^m*x^(3*n)*e^ \\
& m + 54*B*a^2*c*d^2*n*x*x^m*x^(3*n)*e^m + 108*A*a*b*c*d^2*n*x*x^m*x^(3*n)*e^ \\
& m + 18*A*a^2*d^3*n*x*x^m*x^(3*n)*e^m + 12*B*a*b*c^3*m*x*x^m*x^(2*n)*e^m + 6 \\
& *A*b^2*c^3*m*x*x^m*x^(2*n)*e^m + 18*B*a^2*c^2*d*m*x*x^m*x^(2*n)*e^m + 36*A* \\
& a*b*c^2*d*m*x*x^m*x^(2*n)*e^m + 18*A*a^2*c*d^2*m*x*x^m*x^(2*n)*e^m + 38*B*a \\
& *b*c^3*n*x*x^m*x^(2*n)*e^m + 19*A*b^2*c^3*n*x*x^m*x^(2*n)*e^m + 57*B*a^2*c^ \\
& 2*d*n*x*x^m*x^(2*n)*e^m + 114*A*a*b*c^2*d*n*x*x^m*x^(2*n)*e^m + 57*A*a^2*c* \\
& d^2*n*x*x^m*x^(2*n)*e^m + 6*B*a^2*c^3*m*x*x^m*x^n*e^m + 12*A*a*b*c^3*m*x*x^ \\
& m*x^n*e^m + 18*A*a^2*c^2*d*m*x*x^m*x^n*e^m + 20*B*a^2*c^3*n*x*x^m*x^n*e^m + \\
& 40*A*a*b*c^3*n*x*x^m*x^n*e^m + 60*A*a^2*c^2*d*n*x*x^m*x^n*e^m + 6*A*a^2*c^ \\
& 3*m*x*x^m*e^m + 21*A*a^2*c^3*n*x*x^m*e^m + B*b^2*d^3*x*x^m*x^(6*n)*e^m + 3* \\
& B*b^2*c*d^2*x*x^m*x^(5*n)*e^m + 2*B*a*b*d^3*x*x^m*x^(5*n)*e^m + A*b^2*d^3*x \\
& *x^m*x^(5*n)*e^m + 3*B*b^2*c^2*d*x*x^m*x^(4*n)*e^m + 6*B*a*b*c*d^2*x*x^m*x^ \\
& (4*n)*e^m + 3*A*b^2*c*d^2*x*x^m*x^(4*n)*e^m + B*a^2*d^3*x*x^m*x^(4*n)*e^m + \\
& 2*A*a*b*d^3*x*x^m*x^(4*n)*e^m + B*b^2*c^3*x*x^m*x^(3*n)*e^m + 6*B*a*b*c^2* \\
& d*x*x^m*x^(3*n)*e^m + 3*A*b^2*c^2*d*x*x^m*x^(3*n)*e^m + 3*B*a^2*c*d^2*x*x^m \\
& *x^(3*n)*e^m + 6*A*a*b*c*d^2*x*x^m*x^(3*n)*e^m + A*a^2*d^3*x*x^m*x^(3*n)*e^ \\
& m + 2*B*a*b*c^3*x*x^m*x^(2*n)*e^m + A*b^2*c^3*x*x^m*x^(2*n)*e^m + 3*B*a^2*c \\
& ^2*d*x*x^m*x^(2*n)*e^m + 6*A*a*b*c^2*d*x*x^m*x^(2*n)*e^m + 3*A*a^2*c*d^2*x* \\
& x^m*x^(2*n)*e^m + B*a^2*c^3*x*x^m*x^n*e^m + 2*A*a*b*c^3*x*x^m*x^n*e^m + 3*A \\
& *a^2*c^2*d*x*x^m*x^n*e^m + A*a^2*c^3*x*x^m*e^m)/(m^7 + 21*m^6*n + 175*m^5*n \\
& ^2 + 735*m^4*n^3 + 1624*m^3*n^4 + 1764*m^2*n^5 + 720*m*n^6 + 7*m^6 + 126*m^ \\
& 5*n + 875*m^4*n^2 + 2940*m^3*n^3 + 4872*m^2*n^4 + 3528*m*n^5 + 720*n^6 + 21 \\
& *m^5 + 315*m^4*n + 1750*m^3*n^2 + 4410*m^2*n^3 + 4872*m*n^4 + 1764*n^5 + 35 \\
& *m^4 + 420*m^3*n + 1750*m^2*n^2 + 2940*m*n^3 + 1624*n^4 + 35*m^3 + 315*m^2* \\
& n + 875*m*n^2 + 735*n^3 + 21*m^2 + 126*m*n + 175*n^2 + 7*m + 21*n + 1)
\end{aligned}$$

**maple [C]** time = 0.25, size = 11389, normalized size = 36.74

output too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((e*x)^m*(b*x^n+a)^2*(B*x^n+A)*(d*x^n+c)^3,x)`

[Out] result too large to display

**maxima [B]** time = 0.92, size = 748, normalized size = 2.41

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^2*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="maxima")
[Out] B*b^2*d^3*e^m*x*e^(m*log(x) + 6*n*log(x))/(m + 6*n + 1) + 3*B*b^2*c*d^2*e^m
*x*e^(m*log(x) + 5*n*log(x))/(m + 5*n + 1) + 2*B*a*b*d^3*e^m*x*e^(m*log(x)
+ 5*n*log(x))/(m + 5*n + 1) + A*b^2*d^3*e^m*x*e^(m*log(x) + 5*n*log(x))/(m
+ 5*n + 1) + 3*B*b^2*c^2*d*e^m*x*e^(m*log(x) + 4*n*log(x))/(m + 4*n + 1) +
6*B*a*b*c*d^2*e^m*x*e^(m*log(x) + 4*n*log(x))/(m + 4*n + 1) + 3*A*b^2*c*d^2
*e^m*x*e^(m*log(x) + 4*n*log(x))/(m + 4*n + 1) + B*a^2*d^3*e^m*x*e^(m*log(x)
) + 4*n*log(x))/(m + 4*n + 1) + 2*A*a*b*d^3*e^m*x*e^(m*log(x) + 4*n*log(x))
/(m + 4*n + 1) + B*b^2*c^3*e^m*x*e^(m*log(x) + 3*n*log(x))/(m + 3*n + 1) +
6*B*a*b*c^2*d*e^m*x*e^(m*log(x) + 3*n*log(x))/(m + 3*n + 1) + 3*A*b^2*c^2*d
*e^m*x*e^(m*log(x) + 3*n*log(x))/(m + 3*n + 1) + 3*B*a^2*c*d^2*e^m*x*e^(m*log(x)
+ 3*n*log(x))/(m + 3*n + 1) + 6*A*a*b*c*d^2*e^m*x*e^(m*log(x) + 3*n*log(x)
)/(m + 3*n + 1) + A*a^2*d^3*e^m*x*e^(m*log(x) + 3*n*log(x))/(m + 3*n +
1) + 2*B*a*b*c^3*e^m*x*e^(m*log(x) + 2*n*log(x))/(m + 2*n + 1) + A*b^2*c^3
*e^m*x*e^(m*log(x) + 2*n*log(x))/(m + 2*n + 1) + 3*B*a^2*c^2*d*e^m*x*e^(m*log(x)
+ 2*n*log(x))/(m + 2*n + 1) + 6*A*a*b*c^2*d*e^m*x*e^(m*log(x) + 2*n*log(x)
)/(m + 2*n + 1) + 3*A*a^2*c*d^2*e^m*x*e^(m*log(x) + 2*n*log(x))/(m + 2
*n + 1) + B*a^2*c^3*e^m*x*e^(m*log(x) + n*log(x))/(m + n + 1) + 2*A*a*b*c^3
*e^m*x*e^(m*log(x) + n*log(x))/(m + n + 1) + 3*A*a^2*c^2*d*e^m*x*e^(m*log(x)
) + n*log(x))/(m + n + 1) + (e*x)^(m + 1)*A*a^2*c^3/(e*(m + 1))
```

**mupad [B]** time = 6.41, size = 1882, normalized size = 6.07

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(A + B*x^n)*(a + b*x^n)^2*(c + d*x^n)^3,x)
[Out] (x*x^(3*n))*(e*x)^m*(A*a^2*d^3 + B*b^2*c^3 + 3*A*b^2*c^2*d + 3*B*a^2*c*d^2 +
6*A*a*b*c*d^2 + 6*B*a*b*c^2*d)*(5*m + 18*n + 72*m*n + 363*m*n^2 + 108*m^2*
n + 744*m*n^3 + 72*m^3*n + 508*m*n^4 + 18*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 +
m^5 + 121*n^2 + 372*n^3 + 508*n^4 + 240*n^5 + 363*m^2*n^2 + 372*m^2*n^3 +
121*m^3*n^2 + 1))/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^
3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 2
0*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 72
0*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*
n^3 + 175*m^4*n^2 + 1) + (A*a^2*c^3*x*(e*x)^m)/(m + 1) + (c*x*x^(2*n))*(e*x)
^m*(3*A*a^2*d^2 + A*b^2*c^2 + 2*B*a*b*c^2 + 3*B*a^2*c*d + 6*A*a*b*c*d)*(5*m
+ 19*n + 76*m*n + 411*m*n^2 + 114*m^2*n + 922*m*n^3 + 76*m^3*n + 702*m*n^4
+ 19*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 137*n^2 + 461*n^3 + 702*n^4 +
360*n^5 + 411*m^2*n^2 + 461*m^2*n^3 + 137*m^3*n^2 + 1))/(6*m + 21*n + 105*
m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4
*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n
^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3
+ 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (d*x*x^(4*n)
)*(e*x)^m*(B*a^2*d^2 + 3*B*b^2*c^2 + 2*A*a*b*d^2 + 3*A*b^2*c*d + 6*B*a*b*c*
d)*(5*m + 17*n + 68*m*n + 321*m*n^2 + 102*m^2*n + 614*m*n^3 + 68*m^3*n + 39
6*m*n^4 + 17*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 107*n^2 + 307*n^3 + 39
6*n^4 + 180*n^5 + 321*m^2*n^2 + 307*m^2*n^3 + 107*m^3*n^2 + 1))/(6*m + 21*n
+ 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 +
105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6
+ 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m
^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (a*c
^2*x*x^n*(e*x)^m*(3*A*a*d + 2*A*b*c + B*a*c)*(5*m + 20*n + 80*m*n + 465*m*n
```



$$\begin{aligned} &^2 + 120*m^2*n + 1160*m*n^3 + 80*m^3*n + 1044*m*n^4 + 20*m^4*n + 10*m^2 + 1 \\ &0*m^3 + 5*m^4 + m^5 + 155*n^2 + 580*n^3 + 1044*n^4 + 720*n^5 + 465*m^2*n^2 \\ &+ 580*m^2*n^3 + 155*m^3*n^2 + 1)) / (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m \\ &^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^ \\ &5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 \\ &+ 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^ \\ &2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (b*d^2*x*x^(5*n))*(e*x)^m*(A*b*d + \\ &2*B*a*d + 3*B*b*c)*(5*m + 16*n + 64*m*n + 285*m*n^2 + 96*m^2*n + 520*m*n^3 \\ &+ 64*m^3*n + 324*m*n^4 + 16*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 95*n^2 \\ &+ 260*n^3 + 324*n^4 + 144*n^5 + 285*m^2*n^2 + 260*m^2*n^3 + 95*m^3*n^2 + 1) \\ &)/ (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + \\ &3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + \\ &6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2 \\ &*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^ \\ &2 + 1) + (B*b^2*d^3*x*x^(6*n))*(e*x)^m*(5*m + 15*n + 60*m*n + 255*m*n^2 + 90 \\ &*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5* \\ &m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^ \\ &3 + 85*m^3*n^2 + 1)) / (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m \\ &*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 \\ &+ 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + \\ &720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m \\ &^3*n^3 + 175*m^4*n^2 + 1) \end{aligned}$$

**sympy** [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*2\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*3,x)

[Out] Timed out

### 3.11 $\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^3 dx$

**Optimal.** Leaf size=210

$$\frac{c^2 x^{n+1} (ex)^m (3aAd + aBc + Abc)}{m + n + 1} + \frac{d^2 x^{4n+1} (ex)^m (aBd + Abd + 3bBc)}{m + 4n + 1} + \frac{cx^{2n+1} (ex)^m (3ad(Ad + Bc) + bc(3Ad + Bc))}{m + 2n + 1}$$

**Rubi [A]** time = 0.26, antiderivative size = 210, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ , Rules used = {570, 20, 30}

$$\frac{c^2 x^{n+1} (ex)^m (3aAd + aBc + Abc)}{m + n + 1} + \frac{d^2 x^{4n+1} (ex)^m (aBd + Abd + 3bBc)}{m + 4n + 1} + \frac{cx^{2n+1} (ex)^m (3ad(Ad + Bc) + bc(3Ad + Bc))}{m + 2n + 1} + \frac{dx^{3n+1} (ex)^m (ad(Ad + 3Bc) + 3bc(Ad + Bc))}{m + 3n + 1} + \frac{aAc^3 (ex)^{m+1}}{e(m+1)} + \frac{bBd^3 x^{5n+1} (ex)^m}{m + 5n + 1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out] (c^2\*(A\*b\*c + a\*B\*c + 3\*a\*A\*d)\*x^(1 + n)\*(e\*x)^m)/(1 + m + n) + (c\*(3\*a\*d\*(B\*c + A\*d) + b\*c\*(B\*c + 3\*A\*d))\*x^(1 + 2\*n)\*(e\*x)^m)/(1 + m + 2\*n) + (d\*(3\*b\*c\*(B\*c + A\*d) + a\*d\*(3\*B\*c + A\*d))\*x^(1 + 3\*n)\*(e\*x)^m)/(1 + m + 3\*n) + (d^2\*(3\*b\*B\*c + A\*b\*d + a\*B\*d)\*x^(1 + 4\*n)\*(e\*x)^m)/(1 + m + 4\*n) + (b\*B\*d^3\*x^(1 + 5\*n)\*(e\*x)^m)/(1 + m + 5\*n) + (a\*A\*c^3\*(e\*x)^(1 + m))/(e\*(1 + m))

#### Rule 20

Int[(u\_)\*((a\_)\*(v\_))^(m\_)\*((b\_)\*(v\_))^(n\_), x\_Symbol] := Dist[(b^IntPart[n]\*(b\*v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m + n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

#### Rule 30

Int[(x\_)^(m\_), x\_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

#### Rule 570

Int[((g\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_)\*((e\_) + (f\_)\*(x\_)^(n\_))^(r\_), x\_Symbol] := Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

#### Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^3 dx &= \int (aAc^3(ex)^m + c^2(ABC + aBc + 3aAd)x^n(ex)^m + c(3ad(Bc + Ad) + bc(3Ad + Bc))x^{2n}(ex)^m \\ &+ \frac{aAc^3(ex)^{1+m}}{e(1+m)} + (bBd^3) \int x^{5n}(ex)^m dx + (c^2(ABC + aBc + 3aAd)) \int x^{2n}(ex)^m dx \\ &= \frac{aAc^3(ex)^{1+m}}{e(1+m)} + (bBd^3 x^{-m}(ex)^m) \int x^{m+5n} dx + (c^2(ABC + aBc + 3aAd)) \int x^{m+2n} dx \\ &= \frac{c^2(ABC + aBc + 3aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{c(3ad(Bc + Ad) + bc(3Ad + Bc))x^{1+n}(ex)^m}{1+m+2n} \end{aligned}$$

**Mathematica [A]** time = 0.75, size = 172, normalized size = 0.82

$$x(ex)^m \left( \frac{c^2 x^n (3aAd + aBc + Abc)}{m + n + 1} + \frac{d^2 x^{4n} (aBd + Abd + 3bBc)}{m + 4n + 1} + \frac{cx^{2n} (3ad(Ad + Bc) + bc(3Ad + Bc))}{m + 2n + 1} + \frac{dx^{3n} (ad(Ad + 3Bc) + 3bc(Ad + Bc))}{m + 3n + 1} + \frac{aAc^3}{m + 1} + \frac{bBd^3 x^{5n}}{m + 5n + 1} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out]  $x*(e*x)^m*((a*A*c^3)/(1+m) + (c^2*(A*b*c + a*B*c + 3*a*A*d)*x^n)/(1+m+n) + (c*(3*a*d*(B*c + A*d) + b*c*(B*c + 3*A*d))*x^{2*n})/(1+m+2*n) + (d*(3*b*c*(B*c + A*d) + a*d*(3*B*c + A*d))*x^{3*n})/(1+m+3*n) + (d^2*(3*b*B*c + A*b*d + a*B*d)*x^{4*n})/(1+m+4*n) + (b*B*d^3*x^{5*n})/(1+m+5*n))$

**IntegrateAlgebraic** [F] time = 0.64, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^3 dx$$

Verification is not applicable to the result.

[In] IntegrateAlgebraic[(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out] Defer[IntegrateAlgebraic] [(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n)^3, x]

**fricas** [B] time = 0.50, size = 2833, normalized size = 13.49

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="fricas")

[Out]  $((B*b*d^3*m^5 + 5*B*b*d^3*m^4 + 10*B*b*d^3*m^3 + 10*B*b*d^3*m^2 + 5*B*b*d^3*m + B*b*d^3 + 24*(B*b*d^3*m + B*b*d^3)*n^4 + 50*(B*b*d^3*m^2 + 2*B*b*d^3*m + B*b*d^3)*n^3 + 35*(B*b*d^3*m^3 + 3*B*b*d^3*m^2 + 3*B*b*d^3*m + B*b*d^3)*n^2 + 10*(B*b*d^3*m^4 + 4*B*b*d^3*m^3 + 6*B*b*d^3*m^2 + 4*B*b*d^3*m + B*b*d^3)*n)*x*x^{5*n}*e^{(m*\log(e) + m*\log(x))} + ((3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^5 + 3*B*b*c*d^2 + 5*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^4 + 30*(3*B*b*c*d^2 + (B*a + A*b)*d^3 + (3*B*b*c*d^2 + (B*a + A*b)*d^3)*m)*n^4 + (B*a + A*b)*d^3 + 10*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^3 + 61*(3*B*b*c*d^2 + (B*a + A*b)*d^3 + (3*B*b*c*d^2 + (B*a + A*b)*d^3)*m)*n^2 + 2*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m)*n^3 + 10*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^2 + 41*(3*B*b*c*d^2 + (B*a + A*b)*d^3 + (3*B*b*c*d^2 + (B*a + A*b)*d^3)*m)*n^2 + 5*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m + 11*(3*B*b*c*d^2 + (3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^4 + (B*a + A*b)*d^3 + 4*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^3 + 6*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^2 + 4*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m)*n)*x*x^{4*n}*e^{(m*\log(e) + m*\log(x))} + ((3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^5 + 3*B*b*c^2*d + A*a*d^3 + 5*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^4 + 40*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2 + (3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m)*n^4 + 3*(B*a + A*b)*c*d^2 + 10*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^3 + 78*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2 + (3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^2 + 2*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m)*n^3 + 10*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^2 + 49*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2 + (3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^3 + 3*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m)*n^2 + 5*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m + 12*(3*B*b*c^2*d + A*a*d^3 + (3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^4 + 3*(B*a + A*b)*c*d^2 + 4*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^3 + 6*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^2 + 4*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m)*n)*x*x^{3*n}*e^{(m*\log(e) + m*\log(x))} + ((B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^5 + B*b*c^3 + 3*A*a*c*d^2 + 5*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^4 + 60*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d + (B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m)*n^4 + 3*(B*a + A*b)*c^2*d + 10*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d$

$$\begin{aligned}
& *d)*m^3 + 107*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d + (B*b*c^3 + 3*A \\
& *a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^2 + 2*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A \\
& *b)*c^2*d)*m)*n^3 + 10*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^2 + \\
& 59*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d + (B*b*c^3 + 3*A*a*c*d^2 + \\
& 3*(B*a + A*b)*c^2*d)*m^3 + 3*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)* \\
& m^2 + 3*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m)*n^2 + 5*(B*b*c^3 + \\
& 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m + 13*(B*b*c^3 + 3*A*a*c*d^2 + (B*b*c^ \\
& 3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^4 + 3*(B*a + A*b)*c^2*d + 4*(B*b*c \\
& ^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^3 + 6*(B*b*c^3 + 3*A*a*c*d^2 + 3* \\
& (B*a + A*b)*c^2*d)*m^2 + 4*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m) \\
& *n)*x*x^(2*n)*e^(m*log(e) + m*log(x)) + ((3*A*a*c^2*d + (B*a + A*b)*c^3)*m^ \\
& 5 + 3*A*a*c^2*d + 5*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m^4 + 120*(3*A*a*c^2*d \\
& + (B*a + A*b)*c^3 + (3*A*a*c^2*d + (B*a + A*b)*c^3)*m)*n^4 + (B*a + A*b)*c^ \\
& 3 + 10*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m^3 + 154*(3*A*a*c^2*d + (B*a + A*b) \\
& *c^3 + (3*A*a*c^2*d + (B*a + A*b)*c^3)*m^2 + 2*(3*A*a*c^2*d + (B*a + A*b)*c \\
& ^3)*m)*n^3 + 10*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m^2 + 71*(3*A*a*c^2*d + (B \\
& a + A*b)*c^3 + (3*A*a*c^2*d + (B*a + A*b)*c^3)*m^3 + 3*(3*A*a*c^2*d + (B*a \\
& + A*b)*c^3)*m^2 + 3*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m)*n^2 + 5*(3*A*a*c^2*d \\
& + (B*a + A*b)*c^3)*m + 14*(3*A*a*c^2*d + (3*A*a*c^2*d + (B*a + A*b)*c^3)*m \\
& ^4 + (B*a + A*b)*c^3 + 4*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m^3 + 6*(3*A*a*c^2 \\
& *d + (B*a + A*b)*c^3)*m^2 + 4*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m)*n)*x*x^n*e \\
& ^{(m*log(e) + m*log(x)) + (A*a*c^3*m^5 + 120*A*a*c^3*n^5 + 5*A*a*c^3*m^4 + 1 \\
& 0*A*a*c^3*m^3 + 10*A*a*c^3*m^2 + 5*A*a*c^3*m + A*a*c^3 + 274*(A*a*c^3*m + A \\
& *a*c^3)*n^4 + 225*(A*a*c^3*m^2 + 2*A*a*c^3*m + A*a*c^3)*n^3 + 85*(A*a*c^3*m \\
& ^3 + 3*A*a*c^3*m^2 + 3*A*a*c^3*m + A*a*c^3)*n^2 + 15*(A*a*c^3*m^4 + 4*A*a*c \\
& ^3*m^3 + 6*A*a*c^3*m^2 + 4*A*a*c^3*m + A*a*c^3)*n)*x*e^{(m*log(e) + m*log(x) \\
& )}/(m^6 + 120*(m + 1)*n^5 + 6*m^5 + 274*(m^2 + 2*m + 1)*n^4 + 15*m^4 + 225* \\
& (m^3 + 3*m^2 + 3*m + 1)*n^3 + 20*m^3 + 85*(m^4 + 4*m^3 + 6*m^2 + 4*m + 1)*n \\
& ^2 + 15*m^2 + 15*(m^5 + 5*m^4 + 10*m^3 + 10*m^2 + 5*m + 1)*n + 6*m + 1)
\end{aligned}$$

**giac [B]** time = 1.06, size = 6927, normalized size = 32.99

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="giac")

[Out] (B\*b\*d^3\*m^5\*x\*x^m\*x^(5\*n)\*e^m + 10\*B\*b\*d^3\*m^4\*n\*x\*x^m\*x^(5\*n)\*e^m + 35\*B\*b\*d^3\*m^3\*n^2\*x\*x^m\*x^(5\*n)\*e^m + 50\*B\*b\*d^3\*m^2\*n^3\*x\*x^m\*x^(5\*n)\*e^m + 24\*B\*b\*d^3\*m\*n^4\*x\*x^m\*x^(5\*n)\*e^m + 3\*B\*b\*c\*d^2\*m^5\*x\*x^m\*x^(4\*n)\*e^m + B\*a\*d^3\*m^5\*x\*x^m\*x^(4\*n)\*e^m + A\*b\*d^3\*m^5\*x\*x^m\*x^(4\*n)\*e^m + 33\*B\*b\*c\*d^2\*m^4\*n\*x\*x^m\*x^(4\*n)\*e^m + 11\*B\*a\*d^3\*m^4\*n\*x\*x^m\*x^(4\*n)\*e^m + 11\*A\*b\*d^3\*m^4\*n\*x\*x^m\*x^(4\*n)\*e^m + 123\*B\*b\*c\*d^2\*m^3\*n^2\*x\*x^m\*x^(4\*n)\*e^m + 41\*B\*a\*d^3\*m^3\*n^2\*x\*x^m\*x^(4\*n)\*e^m + 41\*A\*b\*d^3\*m^3\*n^2\*x\*x^m\*x^(4\*n)\*e^m + 183\*B\*b\*c\*d^2\*m^2\*n^3\*x\*x^m\*x^(4\*n)\*e^m + 61\*B\*a\*d^3\*m^2\*n^3\*x\*x^m\*x^(4\*n)\*e^m + 61\*A\*b\*d^3\*m^2\*n^3\*x\*x^m\*x^(4\*n)\*e^m + 90\*B\*b\*c\*d^2\*m\*n^4\*x\*x^m\*x^(4\*n)\*e^m + 30\*B\*a\*d^3\*m\*n^4\*x\*x^m\*x^(4\*n)\*e^m + 30\*A\*b\*d^3\*m\*n^4\*x\*x^m\*x^(4\*n)\*e^m + 3\*B\*b\*c^2\*d\*m^5\*x\*x^m\*x^(3\*n)\*e^m + 3\*B\*a\*c\*d^2\*m^5\*x\*x^m\*x^(3\*n)\*e^m + 3\*A\*b\*c\*d^2\*m^5\*x\*x^m\*x^(3\*n)\*e^m + A\*a\*d^3\*m^5\*x\*x^m\*x^(3\*n)\*e^m + 36\*B\*b\*c^2\*d\*m^4\*n\*x\*x^m\*x^(3\*n)\*e^m + 36\*B\*a\*c\*d^2\*m^4\*n\*x\*x^m\*x^(3\*n)\*e^m + 36\*A\*b\*c\*d^2\*m^4\*n\*x\*x^m\*x^(3\*n)\*e^m + 12\*A\*a\*d^3\*m^4\*n\*x\*x^m\*x^(3\*n)\*e^m + 147\*B\*b\*c^2\*d\*m^3\*n^2\*x\*x^m\*x^(3\*n)\*e^m + 147\*B\*a\*c\*d^2\*m^3\*n^2\*x\*x^m\*x^(3\*n)\*e^m + 147\*A\*b\*c\*d^2\*m^3\*n^2\*x\*x^m\*x^(3\*n)\*e^m + 49\*A\*a\*d^3\*m^3\*n^2\*x\*x^m\*x^(3\*n)\*e^m + 234\*B\*b\*c^2\*d\*m^2\*n^3\*x\*x^m\*x^(3\*n)\*e^m + 234\*B\*a\*c\*d^2\*m^2\*n^3\*x\*x^m\*x^(3\*n)\*e^m + 234\*A\*b\*c\*d^2\*m^2\*n^3\*x\*x^m\*x^(3\*n)\*e^m + 78\*A\*a\*d^3\*m^2\*n^3\*x\*x^m\*x^(3\*n)\*e^m + 120\*B\*b\*c^2\*d\*m\*n^4\*x\*x^m\*x^(3\*n)\*e^m + 120\*B\*a\*c\*d^2\*m\*n^4\*x\*x^m\*x^(3\*n)\*e^m + 120\*A\*b\*c\*d^2\*m\*n^4\*x\*x^m\*x^(3\*n)\*e^m + 40\*A\*a\*d^3\*m\*n^4\*x\*x^m\*x^(3\*n)\*e^m + B\*b\*c^3\*m^5\*x\*x^m\*x^(2\*n)\*e^m + 3\*B\*a\*c^2\*d\*m^5\*x\*x^m\*x^(2\*n)\*e^m + 3\*A\*b\*c^2\*d\*m^5\*x\*x^m\*x^(2\*n)\*e^m + 3\*A\*a\*c\*d^2\*m^5\*x\*x^m\*x^(2\*n)\*e^m + 13\*B\*b\*c^3\*m^4\*n\*x\*x^m\*x^(2\*n)\*e^m + 39\*B\*a\*c^2\*d\*m^4

$$\begin{aligned}
& *n*x*x^m*x^{(2*n)}*e^m + 39*A*b*c^2*d*m^4*n*x*x^m*x^{(2*n)}*e^m + 39*A*a*c*d^2*m^4*n*x*x^m*x^{(2*n)}*e^m + 59*B*b*c^3*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 177*B*a*c^2*d*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 177*A*b*c^2*d*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 177*A*a*c*d^2*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 107*B*b*c^3*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 321*B*a*c^2*d*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 321*A*b*c^2*d*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 321*A*a*c*d^2*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 60*B*b*c^3*m*n^4*x*x^m*x^{(2*n)}*e^m + 180*B*a*c^2*d*m*n^4*x*x^m*x^{(2*n)}*e^m + 180*A*b*c^2*d*m*n^4*x*x^m*x^{(2*n)}*e^m + 180*A*a*c*d^2*m*n^4*x*x^m*x^{(2*n)}*e^m + B*a*c^3*m^5*x*x^m*x^n*e^m + A*b*c^3*m^5*x*x^m*x^n*e^m + 3*A*a*c^2*d*m^5*x*x^m*x^n*e^m + 14*B*a*c^3*m^4*n*x*x^m*x^n*e^m + 14*A*b*c^3*m^4*n*x*x^m*x^n*e^m + 42*A*a*c^2*d*m^4*n*x*x^m*x^n*e^m + 71*B*a*c^3*m^3*n^2*x*x^m*x^n*e^m + 71*A*b*c^3*m^3*n^2*x*x^m*x^n*e^m + 213*A*a*c^2*d*m^3*n^2*x*x^m*x^n*e^m + 154*B*a*c^3*m^2*n^3*x*x^m*x^n*e^m + 154*A*b*c^3*m^2*n^3*x*x^m*x^n*e^m + 462*A*a*c^2*d*m^2*n^3*x*x^m*x^n*e^m + 120*B*a*c^3*m*n^4*x*x^m*x^n*e^m + 120*A*b*c^3*m*n^4*x*x^m*x^n*e^m + 360*A*a*c^2*d*m*n^4*x*x^m*x^n*e^m + A*a*c^3*m^5*x*x^m*e^m + 15*A*a*c^3*m^4*n*x*x^m*e^m + 85*A*a*c^3*m^3*n^2*x*x^m*e^m + 225*A*a*c^3*m^2*n^3*x*x^m*e^m + 274*A*a*c^3*m*n^4*x*x^m*e^m + 120*A*a*c^3*n^5*x*x^m*e^m + 5*B*b*d^3*m^4*x*x^m*x^{(5*n)}*e^m + 40*B*b*d^3*m^3*n*x*x^m*x^{(5*n)}*e^m + 105*B*b*d^3*m^2*n^2*x*x^m*x^{(5*n)}*e^m + 100*B*b*d^3*m*n^3*x*x^m*x^{(5*n)}*e^m + 24*B*b*d^3*n^4*x*x^m*x^{(5*n)}*e^m + 15*B*b*c*d^2*m^4*x*x^m*x^{(4*n)}*e^m + 5*B*a*d^3*m^4*x*x^m*x^{(4*n)}*e^m + 5*A*b*d^3*m^4*x*x^m*x^{(4*n)}*e^m + 132*B*b*c*d^2*m^3*n*x*x^m*x^{(4*n)}*e^m + 44*B*a*d^3*m^3*n*x*x^m*x^{(4*n)}*e^m + 44*A*b*d^3*m^3*n*x*x^m*x^{(4*n)}*e^m + 369*B*b*c*d^2*m^2*n^2*x*x^m*x^{(4*n)}*e^m + 123*B*a*d^3*m^2*n^2*x*x^m*x^{(4*n)}*e^m + 123*A*b*d^3*m^2*n^2*x*x^m*x^{(4*n)}*e^m + 366*B*b*c*d^2*m*n^3*x*x^m*x^{(4*n)}*e^m + 122*B*a*d^3*m*n^3*x*x^m*x^{(4*n)}*e^m + 122*A*b*d^3*m*n^3*x*x^m*x^{(4*n)}*e^m + 90*B*b*c*d^2*n^4*x*x^m*x^{(4*n)}*e^m + 30*B*a*d^3*n^4*x*x^m*x^{(4*n)}*e^m + 30*A*b*d^3*n^4*x*x^m*x^{(4*n)}*e^m + 15*B*b*c^2*d*m^4*x*x^m*x^{(3*n)}*e^m + 15*B*a*c*d^2*m^4*x*x^m*x^{(3*n)}*e^m + 15*A*b*c*d^2*m^4*x*x^m*x^{(3*n)}*e^m + 5*A*a*d^3*m^4*x*x^m*x^{(3*n)}*e^m + 144*B*b*c^2*d*m^3*n*x*x^m*x^{(3*n)}*e^m + 144*B*a*c*d^2*m^3*n*x*x^m*x^{(3*n)}*e^m + 144*A*b*c*d^2*m^3*n*x*x^m*x^{(3*n)}*e^m + 48*A*a*d^3*m^3*n*x*x^m*x^{(3*n)}*e^m + 441*B*b*c^2*d*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 441*B*a*c*d^2*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 441*A*b*c*d^2*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 147*A*a*d^3*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 468*B*b*c^2*d*m*n^3*x*x^m*x^{(3*n)}*e^m + 468*B*a*c*d^2*m*n^3*x*x^m*x^{(3*n)}*e^m + 468*A*b*c*d^2*m*n^3*x*x^m*x^{(3*n)}*e^m + 156*A*a*d^3*m*n^3*x*x^m*x^{(3*n)}*e^m + 120*B*b*c^2*d*n^4*x*x^m*x^{(3*n)}*e^m + 120*B*a*c*d^2*n^4*x*x^m*x^{(3*n)}*e^m + 120*A*b*c*d^2*n^4*x*x^m*x^{(3*n)}*e^m + 40*A*a*d^3*n^4*x*x^m*x^{(3*n)}*e^m + 5*B*b*c^3*m^4*x*x^m*x^{(2*n)}*e^m + 15*B*a*c^2*d*m^4*x*x^m*x^{(2*n)}*e^m + 15*A*b*c^2*d*m^4*x*x^m*x^{(2*n)}*e^m + 15*A*a*c*d^2*m^4*x*x^m*x^{(2*n)}*e^m + 52*B*b*c^3*m^3*n*x*x^m*x^{(2*n)}*e^m + 156*B*a*c^2*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 156*A*b*c^2*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 156*A*a*c*d^2*m^3*n*x*x^m*x^{(2*n)}*e^m + 177*B*b*c^3*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 531*B*a*c^2*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 531*A*b*c^2*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 531*A*a*c*d^2*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 214*B*b*c^3*m*n^3*x*x^m*x^{(2*n)}*e^m + 642*B*a*c^2*d*m*n^3*x*x^m*x^{(2*n)}*e^m + 642*A*b*c^2*d*m*n^3*x*x^m*x^{(2*n)}*e^m + 642*A*a*c*d^2*m*n^3*x*x^m*x^{(2*n)}*e^m + 60*B*b*c^3*n^4*x*x^m*x^{(2*n)}*e^m + 180*B*a*c^2*d*n^4*x*x^m*x^{(2*n)}*e^m + 180*A*b*c^2*d*n^4*x*x^m*x^{(2*n)}*e^m + 180*A*a*c*d^2*n^4*x*x^m*x^{(2*n)}*e^m + 5*B*a*c^3*m^4*x*x^m*x^n*e^m + 5*A*b*c^3*m^4*x*x^m*x^n*e^m + 15*A*a*c^2*d*m^4*x*x^m*x^n*e^m + 56*B*a*c^3*m^3*n*x*x^m*x^n*e^m + 56*A*b*c^3*m^3*n*x*x^m*x^n*e^m + 168*A*a*c^2*d*m^3*n*x*x^m*x^n*e^m + 213*B*a*c^3*m^2*n^2*x*x^m*x^n*e^m + 213*A*b*c^3*m^2*n^2*x*x^m*x^n*e^m + 639*A*a*c^2*d*m^2*n^2*x*x^m*x^n*e^m + 308*B*a*c^3*m*n^3*x*x^m*x^n*e^m + 308*A*b*c^3*m*n^3*x*x^m*x^n*e^m + 924*A*a*c^2*d*m*n^3*x*x^m*x^n*e^m + 120*B*a*c^3*n^4*x*x^m*x^n*e^m + 120*A*b*c^3*n^4*x*x^m*x^n*e^m + 360*A*a*c^2*d*n^4*x*x^m*x^n*e^m + 5*A*a*c^3*m^4*x*x^m*e^m + 60*A*a*c^3*m^3*n*x*x^m*e^m + 255*A*a*c^3*m^2*n^2*x*x^m*e^m + 450*A*a*c^3*m*n^3*x*x^m*e^m + 274*A*a*c^3*n^4*x*x^m*e^m + 10*B*b*d^3*m^3*x*x^m*x^{(5*n)}*e^m + 60*B*b*d^3*m^2*n*x*x^m*x^{(5*n)}*e^m + 105*B*b*d^3*m*n^2*x*x^m*x^{(5*n)}*e^m + 50*B*b*d^3*n^3*x*x^m*x^{(5*n)}*e^m + 30*B*b*c*d^2*m^3*x*x^m*x^{(4*n)}*e^m + 10*B*a*d^3*m^3*x*x^
\end{aligned}$$

$$\begin{aligned}
& m^4 x^4 e^m + 10 A^3 b^3 d^3 m^3 x^4 e^m + 198 B^3 b^3 c^2 d^2 m^2 n^2 x^4 e^m \\
& m^4 x^4 e^m + 66 B^3 a^3 d^3 m^2 n^2 x^4 e^m + 66 A^3 b^3 d^3 m^2 n^2 x^4 e^m \\
& x^4 e^m + 369 B^3 b^3 c^2 d^2 m^2 n^2 x^4 e^m + 123 B^3 a^3 d^3 m^2 n^2 x^4 e^m \\
& x^4 e^m + 123 A^3 b^3 d^3 m^2 n^2 x^4 e^m + 183 B^3 b^3 c^2 d^2 n^3 x^4 e^m \\
& x^4 e^m + 61 B^3 a^3 d^3 n^3 x^4 e^m + 61 A^3 b^3 d^3 n^3 x^4 e^m \\
& x^4 e^m + 30 B^3 b^3 c^2 d^2 m^3 x^3 e^m + 30 B^3 a^3 c^2 d^2 m^3 x^3 e^m \\
& x^3 e^m + 30 A^3 b^3 c^2 d^2 m^3 x^3 e^m + 10 A^3 a^3 d^3 m^3 x^3 e^m \\
& x^3 e^m + 216 B^3 b^3 c^2 d^2 m^2 n^2 x^3 e^m + 216 B^3 a^3 c^2 d^2 m^2 n^2 x^3 e^m \\
& x^3 e^m + 216 A^3 b^3 c^2 d^2 m^2 n^2 x^3 e^m + 72 A^3 a^3 d^3 m^2 n^2 x^3 e^m \\
& x^3 e^m + 441 B^3 b^3 c^2 d^2 m^2 n^2 x^3 e^m + 441 B^3 a^3 c^2 d^2 m^2 n^2 x^3 e^m \\
& x^3 e^m + 147 A^3 a^3 d^3 m^2 n^2 x^3 e^m + 234 B^3 b^3 c^2 d^2 n^3 x^3 e^m + 234 B^3 a^3 c^2 d^2 n^3 x^3 e^m \\
& x^3 e^m + 234 A^3 b^3 c^2 d^2 n^3 x^3 e^m + 78 A^3 a^3 d^3 n^3 x^3 e^m + 10 B^3 b^3 c^3 m^3 x^2 e^m \\
& x^2 e^m + 30 B^3 a^3 c^3 d^2 m^3 x^2 e^m + 30 A^3 a^3 c^3 d^2 m^3 x^2 e^m \\
& x^2 e^m + 78 B^3 b^3 c^3 m^2 n^2 x^2 e^m + 234 B^3 a^3 c^3 d^2 m^2 n^2 x^2 e^m \\
& x^2 e^m + 234 A^3 a^3 c^3 d^2 m^2 n^2 x^2 e^m + 177 B^3 b^3 c^3 m^2 n^2 x^2 e^m \\
& x^2 e^m + 531 B^3 a^3 c^3 d^2 m^2 n^2 x^2 e^m + 531 A^3 a^3 b^3 c^2 d^2 m^2 n^2 x^2 e^m \\
& x^2 e^m + 107 B^3 b^3 c^3 n^3 x^2 e^m + 321 B^3 a^3 c^3 d^2 n^3 x^2 e^m \\
& x^2 e^m + 321 A^3 a^3 b^3 c^2 d^2 n^3 x^2 e^m + 10 B^3 a^3 c^3 m^3 x^2 e^m + 10 A^3 b^3 c^3 m^3 x^2 e^m \\
& x^2 e^m + 30 A^3 a^3 c^3 d^2 m^3 x^2 e^m + 84 B^3 a^3 c^3 m^2 n^2 x^2 e^m \\
& x^2 e^m + 84 A^3 b^3 c^3 m^2 n^2 x^2 e^m + 252 A^3 a^3 c^3 d^2 m^2 n^2 x^2 e^m \\
& x^2 e^m + 213 B^3 a^3 c^3 m^2 n^2 x^2 e^m + 213 A^3 b^3 c^3 m^2 n^2 x^2 e^m \\
& x^2 e^m + 639 A^3 a^3 c^3 d^2 m^2 n^2 x^2 e^m + 154 B^3 a^3 c^3 n^3 x^2 e^m + 154 A^3 b^3 c^3 n^3 x^2 e^m \\
& x^2 e^m + 462 A^3 a^3 c^3 d^2 n^3 x^2 e^m + 10 A^3 a^3 c^3 m^3 x^2 e^m + 90 A^3 a^3 c^3 m^2 n^2 x^2 e^m \\
& x^2 e^m + 255 A^3 a^3 c^3 m^2 n^2 x^2 e^m + 225 A^3 a^3 c^3 n^3 x^2 e^m + 10 B^3 b^3 d^3 m^2 x^2 e^m \\
& x^2 e^m + 40 B^3 b^3 d^3 m^2 n^2 x^2 e^m + 35 B^3 b^3 d^3 n^2 x^2 e^m + 30 B^3 b^3 c^2 d^2 m^2 x^2 e^m \\
& x^2 e^m + 10 B^3 a^3 d^3 m^2 x^2 e^m + 10 A^3 b^3 d^3 m^2 x^2 e^m + 10 A^3 b^3 d^3 m^2 x^2 e^m \\
& x^2 e^m + 132 B^3 b^3 c^2 d^2 m^2 n^2 x^2 e^m + 44 B^3 a^3 d^3 m^2 n^2 x^2 e^m + 44 B^3 a^3 d^3 m^2 n^2 x^2 e^m \\
& x^2 e^m + 123 B^3 b^3 c^2 d^2 n^2 x^2 e^m + 41 B^3 a^3 d^3 n^2 x^2 e^m + 41 A^3 b^3 d^3 n^2 x^2 e^m \\
& x^2 e^m + 30 B^3 b^3 c^2 d^2 m^2 x^2 e^m + 30 B^3 a^3 c^2 d^2 m^2 x^2 e^m + 30 A^3 b^3 c^2 d^2 m^2 x^2 e^m \\
& x^2 e^m + 144 B^3 b^3 c^2 d^2 m^2 n^2 x^2 e^m + 144 B^3 a^3 c^2 d^2 m^2 n^2 x^2 e^m + 144 A^3 b^3 c^2 d^2 m^2 n^2 x^2 e^m \\
& x^2 e^m + 48 A^3 a^3 d^3 m^2 n^2 x^2 e^m + 147 B^3 b^3 c^2 d^2 n^2 x^2 e^m + 147 B^3 a^3 c^2 d^2 n^2 x^2 e^m \\
& x^2 e^m + 147 A^3 b^3 c^2 d^2 n^2 x^2 e^m + 49 A^3 a^3 d^3 n^2 x^2 e^m + 10 B^3 b^3 c^3 m^2 x^2 e^m \\
& x^2 e^m + 30 B^3 a^3 c^3 d^2 m^2 x^2 e^m + 30 A^3 b^3 c^3 d^2 m^2 x^2 e^m + 52 B^3 b^3 c^3 m^2 n^2 x^2 e^m \\
& x^2 e^m + 156 B^3 a^3 c^3 d^2 m^2 n^2 x^2 e^m + 156 A^3 b^3 c^3 d^2 m^2 n^2 x^2 e^m + 59 B^3 b^3 c^3 n^2 x^2 e^m \\
& x^2 e^m + 177 B^3 a^3 c^3 d^2 n^2 x^2 e^m + 177 A^3 b^3 c^3 d^2 n^2 x^2 e^m + 177 A^3 a^3 c^3 d^2 n^2 x^2 e^m \\
& x^2 e^m + 10 B^3 a^3 c^3 m^2 x^2 e^m + 10 A^3 b^3 c^3 m^2 x^2 e^m + 30 A^3 a^3 c^3 d^2 m^2 x^2 e^m \\
& x^2 e^m + 56 B^3 a^3 c^3 m^2 n^2 x^2 e^m + 56 A^3 b^3 c^3 m^2 n^2 x^2 e^m + 168 A^3 a^3 c^3 d^2 m^2 n^2 x^2 e^m \\
& x^2 e^m + 71 B^3 a^3 c^3 n^2 x^2 e^m + 71 A^3 b^3 c^3 n^2 x^2 e^m + 213 A^3 a^3 c^3 d^2 n^2 x^2 e^m \\
& x^2 e^m + 10 A^3 a^3 c^3 m^2 x^2 e^m + 60 A^3 a^3 c^3 m^2 n^2 x^2 e^m + 85 A^3 a^3 c^3 n^2 x^2 e^m + 5 B^3 b^3 d^3 m^2 x^2 e^m \\
& x^2 e^m + 10 B^3 b^3 d^3 n^2 x^2 e^m + 15 B^3 b^3 c^2 d^2 m^2 x^2 e^m + 5 B^3 a^3 d^3 m^2 x^2 e^m + 5 A^3 b^3 d^3 m^2 x^2 e^m \\
& x^2 e^m + 33 B^3 b^3 c^2 d^2 n^2 x^2 e^m + 11 B^3 a^3 d^3 n^2 x^2 e^m + 11 A^3 b^3 d^3 n^2 x^2 e^m + 15 B^3 b^3 c^2 d^2 m^2 x^2 e^m \\
& x^2 e^m + 15 B^3 a^3 c^2 d^2 m^2 x^2 e^m + 15 A^3 b^3 c^2 d^2 m^2 x^2 e^m + 5 A^3 a^3 d^3 m^2 x^2 e^m + 36 B^3 b^3 c^2 d^2 n^2 x^2 e^m \\
& x^2 e^m + 36 B^3 a^3 c^2 d^2 n^2 x^2 e^m + 36 A^3 b^3 c^2 d^2 n^2 x^2 e^m + 12 A^3 a^3 d^3 n^2 x^2 e^m + 5 B^3 b^3 c^3 m^2 x^2 e^m \\
& x^2 e^m + 15 B^3 a^3 c^3 d^2 m^2 x^2 e^m + 15 A^3 b^3 c^3 d^2 m^2 x^2 e^m
\end{aligned}$$

$$d^m x^m x^{2n} e^m + 15 A^m a^m c^2 d^2 m x^m x^{2n} e^m + 13 B^m b^m c^3 n x^m x^{2n} e^m + 39 B^m a^m c^2 d^n x^m x^{2n} e^m + 39 A^m b^m c^2 d^n x^m x^{2n} e^m + 39 A^m a^m c^2 d^n x^m x^{2n} e^m + 5 B^m a^m c^3 m x^m x^{2n} e^m + 5 A^m b^m c^3 m x^m x^{2n} e^m + 15 A^m a^m c^2 d^m x^m x^{2n} e^m + 14 B^m a^m c^3 n x^m x^{2n} e^m + 14 A^m b^m c^3 n x^m x^{2n} e^m + 42 A^m a^m c^2 d^n x^m x^{2n} e^m + 5 A^m a^m c^3 m x^m x^{2n} e^m + 15 A^m a^m c^3 n x^m x^{2n} e^m + B^m b^m d^3 x^m x^{2n} e^m + 3 B^m b^m c^2 d^2 x^m x^{2n} e^m + B^m a^m d^3 x^m x^{2n} e^m + A^m b^m d^3 x^m x^{2n} e^m + 3 B^m b^m c^2 d^2 x^m x^{2n} e^m + 3 B^m a^m c^2 d^2 x^m x^{2n} e^m + 3 A^m b^m c^2 d^2 x^m x^{2n} e^m + A^m a^m d^3 x^m x^{2n} e^m + B^m b^m c^3 x^m x^{2n} e^m + 3 B^m a^m c^2 d^2 x^m x^{2n} e^m + 3 A^m b^m c^2 d^2 x^m x^{2n} e^m + 3 A^m a^m c^2 d^2 x^m x^{2n} e^m + B^m a^m c^3 x^m x^{2n} e^m + A^m b^m c^3 x^m x^{2n} e^m + 3 A^m a^m c^2 d^2 x^m x^{2n} e^m + A^m a^m c^3 x^m x^{2n} e^m) / (m^6 + 15 m^5 n + 85 m^4 n^2 + 225 m^3 n^3 + 274 m^2 n^4 + 120 m n^5 + 6 m^5 + 75 m^4 n + 340 m^3 n^2 + 675 m^2 n^3 + 548 m n^4 + 120 n^5 + 15 m^4 + 150 m^3 n + 510 m^2 n^2 + 675 m n^3 + 274 n^4 + 20 m^3 + 150 m^2 n + 340 m n^2 + 225 n^3 + 15 m^2 + 75 m n + 85 n^2 + 6 m + 15 n + 1)$$

**maple [C]** time = 0.18, size = 4972, normalized size = 23.68

output too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((e*x)^m*(b*x^n+a)*(B*x^n+A)*(d*x^n+c)^3,x)`

[Out] `x*(44*B*a*d^3*m^3*n*(x^n)^4+123*B*a*d^3*m^2*n^2*(x^n)^4+122*B*a*d^3*m*n^3*(x^n)^4+3*B*b*c^2*d*m^5*(x^n)^3+15*B*b*c*d^2*m^4*(x^n)^4+A*a*d^3*(x^n)^3+B*b*c^3*(x^n)^2+A*b*c^3*x^n+B*a*c^3*x^n+b*B*d^3*(x^n)^5+A*b*d^3*(x^n)^4+B*a*d^3*(x^n)^4+10*A*a*c^3*m^2+85*A*a*c^3*n^2+120*A*a*c^3*n^5+A*a*c^3*m^5+5*A*a*c^3*m^4+274*A*a*c^3*n^4+10*A*a*c^3*m^3+225*A*a*c^3*n^3+a*A*c^3+5*a*A*c^3*m+15*a*A*c^3*n+40*A*a*d^3*m*n^4*(x^n)^3+3*A*b*c*d^2*m^5*(x^n)^3+44*A*b*d^3*m^3*n*(x^n)^4+123*A*b*d^3*m^2*n^2*(x^n)^4+122*A*b*d^3*m*n^3*(x^n)^4+3*B*a*c*d^2*m^5*(x^n)^3+84*B*a*c^3*m^2*n*x^n+213*B*a*c^3*m*n^2*x^n+30*B*a*c^2*d*m^2*(x^n)^2+177*B*a*c^2*d*n^2*(x^n)^2+15*B*a*c*d^2*(x^n)^3+m+36*B*a*c*d^2*(x^n)^3+n+52*B*b*c^3*m*n*(x^n)^2+15*B*b*c^2*d*(x^n)^3+m+36*B*b*c^2*d*(x^n)^3+n+30*A*a*c^2*d*m^2*x^n+213*A*a*c^2*d*n^2*x^n+15*A*a*c*d^2*(x^n)^2+m+90*A*a*c^3*m^2*n+66*B*a*d^3*m^2*n*(x^n)^4+123*B*a*d^3*m*n^2*(x^n)^4+13*B*b*c^3*m^4*n*(x^n)^2+59*B*b*c^3*m^3*n^2*(x^n)^2+107*B*b*c^3*m^2*n^3*(x^n)^2+60*B*b*c^3*m*n^4*(x^n)^2+15*B*b*c^2*d*m^4*(x^n)^3+120*B*b*c^2*d*n^4*(x^n)^3+30*B*b*c*d^2*m^3*(x^n)^4+11*B*a*d^3*m^4*n*(x^n)^4+41*B*a*d^3*m^3*n^2*(x^n)^4+39*A*a*c*d^2*(x^n)^2+n+56*A*b*c^3*m*n*x^n+15*A*b*c^2*d*(x^n)^2+m+39*A*b*c^2*d*(x^n)^2+n+213*B*a*c^3*m^2*n^2*x^n+308*B*a*c^3*m*n^3*x^n+30*B*a*c^2*d*m^3*(x^n)^2+321*B*a*c^2*d*n^3*(x^n)^2+30*B*a*c*d^2*m^2*(x^n)^3+44*B*a*d^3*m*n*(x^n)^4+52*B*b*c^3*m^3*n*(x^n)^2+177*B*b*c^3*m^2*n^2*(x^n)^2+214*B*b*c^3*m*n^3*(x^n)^2+30*B*b*c^2*d*m^3*(x^n)^3+234*B*b*c^2*d*n^3*(x^n)^3+30*B*b*c*d^2*m^2*(x^n)^4+123*B*b*c*d^2*n^2*(x^n)^4+15*A*a*c^2*d*m^4*x^n+360*A*a*c^2*d*n^4*x^n+30*A*a*c*d^2*m^3*(x^n)^2+15*A*a*c^2*d*x^n+m+42*A*a*c^2*d*x^n+n+15*A*b*c*d^2*(x^n)^3+m+36*A*b*c*d^2*(x^n)^3+n+3*A*b*c^2*d*m^5*(x^n)^2+15*A*b*c*d^2*m^4*(x^n)^3+120*A*b*c*d^2*n^4*(x^n)^3+66*A*b*d^3*m^2*n*(x^n)^4+123*A*b*d^3*m*n^2*(x^n)^4+3*B*a*c^2*d*m^5*(x^n)^2+15*B*a*c*d^2*m^4*(x^n)^3+120*B*a*c*d^2*n^4*(x^n)^3+90*B*b*c*d^2*n^4*(x^n)^4+60*B*b*d^3*m^2*n*(x^n)^5+105*B*b*d^3*m*n^2*(x^n)^5+3*A*a*c*d^2*m^5*(x^n)^2+48*A*a*d^3*m^3*n*(x^n)^3+10*B*b*d^3*m^4*n*(x^n)^5+35*B*b*d^3*m^3*n^2*(x^n)^5+147*B*a*c*d^2*n^2*(x^n)^3+78*B*b*c^3*m^2*n*(x^n)^2+177*B*b*c^3*m*n^2*(x^n)^2+30*B*b*c^2*d*m^2*(x^n)^3+147*B*b*c^2*d*n^2*(x^n)^3+15*B*b*c*d^2*(x^n)^4+m+33*B*b*c*d^2*(x^n)^4+n+30*A*a*c^2*d*m^3*x^n+462*A*a*c^2*d*n^3*x^n+321*A*a*c*d^2*n^3*(x^n)^2+48*A*a*d^3*m*n*(x^n)^3+56*A*b*c^3*m^3*n*x^n+213*A*b*c^3*m^2*n^2*x^n+308*A*b*c^3*m*n^3*x^n+30*A*b*c^2*d*m^3*(x^n)^2+321*A*b*c^2*d*n^3*(x^n)^2+30*A*b*c*d^2*m^2*(x^n)^3+255*A*a*c^3*m*n^2+60*A*a*c^3*m*n+61*B*a*d^3*m^2*n^3*(x^n)^4+30*B*a*d^3*m*n^4*(x^n)^4+3*B*b*c*d^2*m^5*(x^n)^4+40*B*b*d^3*m^3*n*(x^n)^5+105*B*b*d^3*m^2*n^2*(x^n)^5+100*B`

$$\begin{aligned}
& *b*d^3*m*n^3*(x^n)^5+12*A*a*d^3*m^4*n*(x^n)^3+49*A*a*d^3*m^3*n^2*(x^n)^3+78 \\
& *A*a*d^3*m^2*n^3*(x^n)^3+50*B*b*d^3*m^2*n^3*(x^n)^5+24*B*b*d^3*m*n^4*(x^n)^5+11*A*b*d^3*m^4*n*(x^n)^4+41*A*b*d^3*m^3*n^2*(x^n)^4+61*A*b*d^3*m^2*n^3*(x^n)^4+30*A*a*c*d^2*m^2*(x^n)^2+177*A*a*c*d^2*m^2*(x^n)^2+84*A*b*c^3*m^2*n*x^n+213*A*b*c^3*m*n^2*x^n+30*A*b*c^2*d*m^2*(x^n)^2+177*A*b*c^2*d*n^2*(x^n)^2+15*B*a*c^2*d*m^4*(x^n)^2+180*B*a*c^2*d*n^4*(x^n)^2+30*B*a*c*d^2*m^3*(x^n)^3+234*B*a*c*d^2*n^3*(x^n)^3+24*B*b*d^3*n^4*(x^n)^5+A*b*c^3*m^5*x^n+10*A*b*d^3*m^2*(x^n)^4+41*A*b*d^3*n^2*(x^n)^4+B*a*c^3*m^5*x^n+10*B*a*d^3*m^2*(x^n)^4+41*B*a*d^3*n^2*(x^n)^4+5*B*b*c^3*m^4*(x^n)^2+60*B*b*c^3*n^4*(x^n)^2+5*m*b*B*d^3*(x^n)^5+147*A*b*c*d^2*n^2*(x^n)^3+56*B*a*c^3*m^3*n*x^n+183*B*b*c*d^2*n^3*(x^n)^4+40*B*b*d^3*m*n*(x^n)^5+3*A*a*c^2*d*m^5*x^n+15*A*a*c*d^2*m^4*(x^n)^2+180*A*a*c*d^2*n^4*(x^n)^2+72*A*a*d^3*m^2*n*(x^n)^3+147*A*a*d^3*m*n^2*(x^n)^3+14*A*b*c^3*m^4*n*x^n+71*A*b*c^3*m^3*n^2*x^n+154*A*b*c^3*m^2*n^3*x^n+120*A*b*c^3*m*n^4*x^n+15*A*b*c^2*d*m^4*(x^n)^2+180*A*b*c^2*d*n^4*(x^n)^2+30*A*b*c*d^2*m^3*(x^n)^3+234*A*b*c*d^2*n^3*(x^n)^3+44*A*b*d^3*m*n*(x^n)^4+14*B*a*c^3*m^4*n*x^n+71*B*a*c^3*m^3*n^2*x^n+154*B*a*c^3*m^2*n^3*x^n+120*B*a*c^3*m*n^4*x^n+147*A*a*d^3*m^2*n^2*(x^n)^3+156*A*a*d^3*m*n^3*(x^n)^3+50*B*b*d^3*n^3*(x^n)^5+5*A*a*d^3*m^4*(x^n)^3+154*B*a*c^3*n^3*x^n+10*B*b*c^3*m^2*(x^n)^2+59*B*b*c^3*n^2*(x^n)^2+10*A*b*c^3*m^2*x^n+71*A*b*c^3*n^2*x^n+10*B*a*c^3*m^2*x^n+30*A*b*d^3*m*n^4*(x^n)^4+A*a*d^3*m^5*(x^n)^3+5*A*b*d^3*m^4*(x^n)^4+30*A*b*d^3*n^4*(x^n)^4+5*B*a*d^3*m^4*(x^n)^4+30*B*a*d^3*n^4*(x^n)^4+10*B*b*d^3*m^3*(x^n)^5+B*b*d^3*m^5*(x^n)^5+A*b*d^3*m^5*(x^n)^4+B*a*d^3*m^5*(x^n)^4+5*B*b*d^3*m^4*(x^n)^5+5*A*a*d^3*(x^n)^3+m+12*A*a*d^3*(x^n)^3+n+10*A*b*c^3*m^3*x^n+154*A*b*c^3*n^3*x^n+10*B*a*c^3*m^3*x^n+10*B*b*d^3*m^2*(x^n)^5+35*B*b*d^3*n^2*(x^n)^5+10*A*a*d^3*m^3*(x^n)^3+78*A*a*d^3*n^3*(x^n)^3+40*A*a*d^3*n^4*(x^n)^3+10*A*b*d^3*m^3*(x^n)^4+61*A*b*d^3*n^3*(x^n)^4+60*A*a*c^3*m^3*n+255*A*a*c^3*m^2*n^2+450*A*a*c^3*m*n^3+15*A*a*c^3*m^4*n+85*A*a*c^3*m^3*n^2+225*A*a*c^3*m^2*n^3+274*A*a*c^3*m*n^4+10*B*a*d^3*m^3*(x^n)^4+61*B*a*d^3*n^3*(x^n)^4+B*b*c^3*m^5*(x^n)^2+3*(x^n)^2*d*c^2*A*b+3*(x^n)^2*d*c^2*B*a+3*(x^n)^4*b*B*c*d^2+10*b*B*d^3*(x^n)^5*n+10*A*a*d^3*m^2*(x^n)^3+49*A*a*d^3*n^2*(x^n)^3+5*A*b*c^3*m^4*x^n+120*A*b*c^3*n^4*x^n+5*A*b*d^3*(x^n)^4*m+11*A*b*d^3*(x^n)^4*n+5*B*a*c^3*m^4*x^n+120*B*a*c^3*n^4*x^n+5*B*a*d^3*(x^n)^4*m+11*B*a*d^3*(x^n)^4*n+10*B*b*c^3*m^3*(x^n)^2+107*B*b*c^3*n^3*(x^n)^2+3*x^n*a*A*c^2*d+3*(x^n)^3*A*b*c*d^2+3*(x^n)^3*B*a*c*d^2+3*(x^n)^3*b*B*c^2*d+3*(x^n)^2*a*A*c*d^2+71*B*a*c^3*n^2*x^n+5*B*b*c^3*(x^n)^2*m+13*B*b*c^3*(x^n)^2*n+5*A*b*c^3*x^n*m+14*A*b*c^3*x^n*n+5*B*a*c^3*x^n*m+14*B*a*c^3*x^n*n+441*A*b*c*d^2*m^2*n^2*(x^n)^3+39*A*b*c^2*d*m^4*n*(x^n)^2+177*A*b*c^2*d*m^3*n^2*(x^n)^2+321*A*b*c^2*d*m^2*n^3*(x^n)^2+180*A*b*c^2*d*m*n^4*(x^n)^2+144*A*b*c*d^2*m^3*n*(x^n)^3+639*A*a*c^2*d*m^2*n^2*x^n+924*A*a*c^2*d*m*n^3*x^n+234*A*a*c*d^2*m^2*n*(x^n)^2+531*A*a*c*d^2*m*n^2*(x^n)^2+177*A*a*c*d^2*m^3*n^2*(x^n)^2+321*A*a*c*d^2*m^2*n^3*(x^n)^2+180*A*a*c*d^2*m*n^4*(x^n)^2+144*B*a*c*d^2*m*n*(x^n)^3+144*B*b*c^2*d*m*n*(x^n)^3+252*A*a*c^2*d*m^2*n*x^n+639*A*a*c^2*d*m*n^2*x^n+441*B*b*c^2*d*m*n^2*(x^n)^3+132*B*b*c*d^2*m*n*(x^n)^4+168*A*a*c^2*d*m^3*n*x^n+468*B*b*c^2*d*m*n^3*(x^n)^3+234*A*b*c^2*d*m^2*n*(x^n)^2+531*A*b*c^2*d*m*n^2*(x^n)^2+144*A*b*c*d^2*m*n*(x^n)^3+234*B*a*c^2*d*m^2*n*(x^n)^2+531*B*a*c^2*d*m*n^2*(x^n)^2+180*B*a*c^2*d*m*n^4*(x^n)^2+144*B*a*c*d^2*m^3*n*(x^n)^3+441*B*a*c*d^2*m^2*n^2*(x^n)^3+468*B*a*c*d^2*m*n^3*(x^n)^3+144*B*b*c^2*d*m^3*n*(x^n)^3+441*B*b*c^2*d*m^2*n^2*(x^n)^3+360*A*a*c^2*d*m*n^4*x^n+156*A*a*c*d^2*m^3*n*(x^n)^2+468*A*b*c*d^2*m*n^3*(x^n)^3+39*B*a*c^2*d*m^4*n*(x^n)^2+177*B*a*c^2*d*m^3*n^2*(x^n)^2+321*B*a*c^2*d*m^2*n^3*(x^n)^2+366*B*b*c*d^2*m*n^3*(x^n)^4+39*A*a*c*d^2*m^4*n*(x^n)^2+120*B*a*c*d^2*m*n^4*(x^n)^3+36*B*b*c^2*d*m^4*n*(x^n)^3+147*B*b*c^2*d*m^3*n^2*(x^n)^3+234*B*b*c^2*d*m^2*n^3*(x^n)^3+120*B*b*c^2*d*m*n^4*(x^n)^3+132*B*b*c*d^2*m^3*n*(x^n)^4+369*B*b*c*d^2*m^2*n^2*(x^n)^4+168*A*a*c^2*d*m*n*x^n+147*A*b*c*d^2*m^3*n^2*(x^n)^3+234*A*b*c*d^2*m^2*n^3*(x^n)^3+120*A*b*c*d^2*m*n^4*(x^n)^3+36*B*a*c*d^2*m^4*n*(x^n)^3+147*B*a*c*d^2*m^3*n^2*(x^n)^3+234*B*a*c*d^2*m^2*n^3*(x^n)^3+216*B*a*c*d^2*m^2*n*(x^n)^3+441*B*a*c*d^2*m*n^2*(x^n)^3+216*B*b*c^2*d*m^2*n*(x^n)^3+531*A*a*c*d^2*m^2*n^2*(x^n)^2+156*A*a*c*d^2*m*n*(x^n)^2+156*A*b*c^2*d*m*n*(x^n)^2+156*B*a*c^2*d*m*n*(x^n)^2+531*A*b*c^2*d*m^2*n^2*(x^n)^2+642*A*b*c^2*d*m*
\end{aligned}$$



$$n^3(x^n)^2 + 216A^2b^2c^2d^2m^2n^2(x^n)^3 + 441A^2b^2c^2d^2m^2n^2(x^n)^3 + 156B^2a^2c^2d^2m^3n^2(x^n)^2 + 531B^2a^2c^2d^2m^2n^2(x^n)^2 + 642B^2a^2c^2d^2m^2n^3(x^n)^2 + 198B^2b^2c^2d^2m^2n^2(x^n)^4 + 369B^2b^2c^2d^2m^2n^2(x^n)^4 + 42A^2a^2c^2d^2m^4n^2x^n + 213A^2a^2c^2d^2m^3n^2x^n + 462A^2a^2c^2d^2m^2n^3x^n + 642A^2a^2c^2d^2m^2n^3(x^n)^2 + 156A^2b^2c^2d^2m^3n^2(x^n)^2 + 33B^2b^2c^2d^2m^4n^2(x^n)^4 + 123B^2b^2c^2d^2m^3n^2(x^n)^4 + 183B^2b^2c^2d^2m^2n^3(x^n)^4 + 90B^2b^2c^2d^2m^2n^4(x^n)^4 + 36A^2b^2c^2d^2m^4n^2(x^n)^3 / (m+1) / (m+n+1) / (m+2n+1) / (m+3n+1) / (m+4n+1) / ((1+m+5n) * \exp(1/2 * (-I * \pi * \operatorname{csgn}(I * e) * \operatorname{csgn}(I * x) * \operatorname{csgn}(I * e * x)) + I * \pi * \operatorname{csgn}(I * e) * \operatorname{csgn}(I * e * x))^2 + I * \pi * \operatorname{csgn}(I * x) * \operatorname{csgn}(I * e * x))^2 - I * \pi * \operatorname{csgn}(I * e * x))^3 + 2 * \ln(e) + 2 * \ln(x)) * m)$$

**maxima [B]** time = 1.01, size = 464, normalized size = 2.21

---

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="maxima")

[Out]  $B^2b^2d^3e^m x^m e^{(m \log(x) + 5n \log(x)) / (m + 5n + 1)} + 3B^2b^2c^2d^2e^m x^m e^{(m \log(x) + 4n \log(x)) / (m + 4n + 1)} + B^2a^2d^3e^m x^m e^{(m \log(x) + 4n \log(x)) / (m + 4n + 1)} + 3B^2b^2c^2d^2e^m x^m e^{(m \log(x) + 3n \log(x)) / (m + 3n + 1)} + 3B^2a^2c^2d^2e^m x^m e^{(m \log(x) + 3n \log(x)) / (m + 3n + 1)} + 3A^2b^2c^2d^2e^m x^m e^{(m \log(x) + 3n \log(x)) / (m + 3n + 1)} + A^2a^2d^3e^m x^m e^{(m \log(x) + 3n \log(x)) / (m + 3n + 1)} + B^2b^2c^3e^m x^m e^{(m \log(x) + 2n \log(x)) / (m + 2n + 1)} + 3B^2a^2c^2d^2e^m x^m e^{(m \log(x) + 2n \log(x)) / (m + 2n + 1)} + 3A^2b^2c^2d^2e^m x^m e^{(m \log(x) + 2n \log(x)) / (m + 2n + 1)} + 3A^2a^2c^2d^2e^m x^m e^{(m \log(x) + 2n \log(x)) / (m + 2n + 1)} + B^2a^2c^3e^m x^m e^{(m \log(x) + n \log(x)) / (m + n + 1)} + A^2b^2c^3e^m x^m e^{(m \log(x) + n \log(x)) / (m + n + 1)} + 3A^2a^2c^2d^2e^m x^m e^{(m \log(x) + n \log(x)) / (m + n + 1)} + (e*x)^{m+1} * A^2a^2c^3 / (e^{m+1})$

**mupad [B]** time = 5.65, size = 1089, normalized size = 5.19

---

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)\*(c + d\*x^n)^3,x)

[Out]  $(A^2a^2c^3x^m(e*x)^m) / (m + 1) + (d^2x^m x^{(4n)}(e*x)^m(A^2b^2d + B^2a^2d + 3B^2b^2c) * (4m^2 + 11n^2 + 33m^2n + 82m^2n^2 + 33m^2n^2 + 61m^2n^3 + 11m^2n^3 + 6m^2n^2 + 4m^2n^3 + m^4 + 41n^2 + 61n^3 + 30n^4 + 41m^2n^2 + 1)) / (5m + 15n + 60m^2n + 255m^2n^2 + 90m^2n^2 + 450m^2n^3 + 60m^2n^3 + 274m^2n^4 + 15m^2n^4n + 10m^2n^2 + 10m^2n^3 + 5m^2n^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2n^2 + 225m^2n^3 + 85m^2n^3n^2 + 1) + (c^2x^m x^{(2n)}(e*x)^m(3A^2a^2d^2 + B^2b^2c^2 + 3A^2b^2c^2d + 3B^2a^2c^2d) * (4m^2 + 13n^2 + 39m^2n + 118m^2n^2 + 39m^2n^2 + 107m^2n^3 + 13m^2n^3 + 6m^2n^2 + 4m^2n^3 + m^4 + 59n^2 + 107n^3 + 60n^4 + 59m^2n^2 + 1)) / (5m + 15n + 60m^2n + 255m^2n^2 + 90m^2n^2 + 450m^2n^3 + 60m^2n^3 + 274m^2n^4 + 15m^2n^4n + 10m^2n^2 + 10m^2n^3 + 5m^2n^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2n^2 + 225m^2n^3 + 85m^2n^3n^2 + 1) + (d^2x^m x^{(3n)}(e*x)^m(A^2a^2d^2 + 3B^2b^2c^2 + 3A^2b^2c^2d + 3B^2a^2c^2d) * (4m^2 + 12n^2 + 36m^2n + 98m^2n^2 + 36m^2n^2 + 78m^2n^3 + 12m^2n^3 + 6m^2n^2 + 4m^2n^3 + m^4 + 49n^2 + 78n^3 + 40n^4 + 49m^2n^2 + 1)) / (5m + 15n + 60m^2n + 255m^2n^2 + 90m^2n^2 + 450m^2n^3 + 60m^2n^3 + 274m^2n^4 + 15m^2n^4n + 10m^2n^2 + 10m^2n^3 + 5m^2n^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2n^2 + 225m^2n^3 + 85m^2n^3n^2 + 1) + (c^2x^m x^n(e*x)^m(3A^2a^2d + A^2b^2c + B^2a^2c) * (4m^2 + 14n^2 + 42m^2n + 142m^2n^2 + 42m^2n^2 + 154m^2n^3 + 14m^2n^3 + 6m^2n^2 + 4m^2n^3 + m^4 + 71n^2 + 154n^3 + 120n^4 + 71m^2n^2 + 1)) / (5m + 15n + 60m^2n + 255m^2n^2 + 90m^2n^2 + 450m^2n^3 + 60m^2n^3 + 274m^2n^4 + 15m^2n^4n + 10m^2n^2 + 10m^2n^3 + 5m^2n^4 + m^5 + 85n^2 + 225n^3 + 274n^4$

$$+ 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (B*b*d^3*x*x^{(5*n)}*(e*x)^m*(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1)$$

**sympy** [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*3,x)

[Out] Timed out

### 3.12 $\int (ex)^m (A + Bx^n) (c + dx^n)^3 dx$

**Optimal.** Leaf size=137

$$\frac{c^2 x^{n+1} (ex)^m (3Ad + Bc)}{m + n + 1} + \frac{d^2 x^{3n+1} (ex)^m (Ad + 3Bc)}{m + 3n + 1} + \frac{3cdx^{2n+1} (ex)^m (Ad + Bc)}{m + 2n + 1} + \frac{Ac^3 (ex)^{m+1}}{e(m + 1)} + \frac{Bd^3 x^{4n+1} (ex)^m}{m + 4n + 1}$$

**Rubi [A]** time = 0.11, antiderivative size = 137, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 3, integrand size = 22,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$ , Rules used = {448, 20, 30}

$$\frac{c^2 x^{n+1} (ex)^m (3Ad + Bc)}{m + n + 1} + \frac{d^2 x^{3n+1} (ex)^m (Ad + 3Bc)}{m + 3n + 1} + \frac{3cdx^{2n+1} (ex)^m (Ad + Bc)}{m + 2n + 1} + \frac{Ac^3 (ex)^{m+1}}{e(m + 1)} + \frac{Bd^3 x^{4n+1} (ex)^m}{m + 4n + 1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out] (c^2\*(B\*c + 3\*A\*d)\*x^(1 + n)\*(e\*x)^m)/(1 + m + n) + (3\*c\*d\*(B\*c + A\*d)\*x^(1 + 2\*n)\*(e\*x)^m)/(1 + m + 2\*n) + (d^2\*(3\*B\*c + A\*d)\*x^(1 + 3\*n)\*(e\*x)^m)/(1 + m + 3\*n) + (B\*d^3\*x^(1 + 4\*n)\*(e\*x)^m)/(1 + m + 4\*n) + (A\*c^3\*(e\*x)^(1 + m))/(e\*(1 + m))

#### Rule 20

Int[(u\_)\*((a\_)\*(v\_))^(m\_)\*((b\_)\*(v\_))^(n\_), x\_Symbol] := Dist[(b^IntPart[n]\*(b\*v)^FracPart[n])/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m + n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

#### Rule 30

Int[(x\_)^(m\_), x\_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

#### Rule 448

Int[((e\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_), x\_Symbol] := Int[ExpandIntegrand[(e\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[b\*c - a\*d, 0] && IGtQ[p, 0] && IGtQ[q, 0]

#### Rubi steps

$$\begin{aligned} \int (ex)^m (A + Bx^n) (c + dx^n)^3 dx &= \int (Ac^3(ex)^m + c^2(Bc + 3Ad)x^n(ex)^m + 3cd(Bc + Ad)x^{2n}(ex)^m + d^2(3Bc + Ad)x^{3n}(ex)^m + Bd^3x^{4n}(ex)^m) dx \\ &= \frac{Ac^3(ex)^{1+m}}{e(1+m)} + (Bd^3) \int x^{4n}(ex)^m dx + (3cd(Bc + Ad)) \int x^{2n}(ex)^m dx + (d^2(3Bc + Ad)) \int x^{3n}(ex)^m dx + Bd^3 \int x^{4n}(ex)^m dx \\ &= \frac{Ac^3(ex)^{1+m}}{e(1+m)} + (Bd^3x^{-m}(ex)^m) \int x^{m+4n} dx + (3cd(Bc + Ad)x^{-m}(ex)^m) \int x^{m+2n} dx + (d^2(3Bc + Ad)x^{-m}(ex)^m) \int x^{m+n} dx \\ &= \frac{c^2(Bc + 3Ad)x^{1+n}(ex)^m}{1+m+n} + \frac{3cd(Bc + Ad)x^{1+2n}(ex)^m}{1+m+2n} + \frac{d^2(3Bc + Ad)x^{1+3n}(ex)^m}{1+m+3n} + \frac{Bd^3x^{1+4n}(ex)^m}{1+m+4n} \end{aligned}$$

**Mathematica [A]** time = 0.18, size = 106, normalized size = 0.77

$$x(ex)^m \left( \frac{c^2 x^n (3Ad + Bc)}{m + n + 1} + \frac{d^2 x^{3n} (Ad + 3Bc)}{m + 3n + 1} + \frac{3cdx^{2n} (Ad + Bc)}{m + 2n + 1} + \frac{Ac^3}{m + 1} + \frac{Bd^3 x^{4n}}{m + 4n + 1} \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(e*x)^m*(A + B*x^n)*(c + d*x^n)^3,x]
```

```
[Out] x*(e*x)^m*((A*c^3)/(1 + m) + (c^2*(B*c + 3*A*d)*x^n)/(1 + m + n) + (3*c*d*(B*c + A*d)*x^(2*n))/(1 + m + 2*n) + (d^2*(3*B*c + A*d)*x^(3*n))/(1 + m + 3*n) + (B*d^3*x^(4*n))/(1 + m + 4*n))
```

**IntegrateAlgebraic [F]** time = 0.11, size = 0, normalized size = 0.00

$$\int (ex)^m (A + Bx^n) (c + dx^n)^3 dx$$

Verification is not applicable to the result.

```
[In] IntegrateAlgebraic[(e*x)^m*(A + B*x^n)*(c + d*x^n)^3,x]
```

```
[Out] Defer[IntegrateAlgebraic] [(e*x)^m*(A + B*x^n)*(c + d*x^n)^3, x]
```

**fricas [B]** time = 0.47, size = 1104, normalized size = 8.06

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="fricas")
```

```
[Out] ((B*d^3*m^4 + 4*B*d^3*m^3 + 6*B*d^3*m^2 + 4*B*d^3*m + B*d^3 + 6*(B*d^3*m + B*d^3)*n^3 + 11*(B*d^3*m^2 + 2*B*d^3*m + B*d^3)*n^2 + 6*(B*d^3*m^3 + 3*B*d^3*m^2 + 3*B*d^3*m + B*d^3)*n)*x*x^(4*n)*e^(m*log(e) + m*log(x)) + ((3*B*c*d^2 + A*d^3)*m^4 + 3*B*c*d^2 + A*d^3 + 4*(3*B*c*d^2 + A*d^3)*m^3 + 8*(3*B*c*d^2 + A*d^3 + (3*B*c*d^2 + A*d^3)*m)*n^3 + 6*(3*B*c*d^2 + A*d^3)*m^2 + 14*(3*B*c*d^2 + A*d^3 + (3*B*c*d^2 + A*d^3)*m)*n^2 + 2*(3*B*c*d^2 + A*d^3)*m)*n^2 + 4*(3*B*c*d^2 + A*d^3)*m + 7*(3*B*c*d^2 + A*d^3 + (3*B*c*d^2 + A*d^3)*m^3 + 3*(3*B*c*d^2 + A*d^3)*m^2 + 3*(3*B*c*d^2 + A*d^3)*m)*n)*x*x^(3*n)*e^(m*log(e) + m*log(x)) + 3*((B*c^2*d + A*c*d^2)*m^4 + B*c^2*d + A*c*d^2 + 4*(B*c^2*d + A*c*d^2)*m^3 + 12*(B*c^2*d + A*c*d^2 + (B*c^2*d + A*c*d^2)*m)*n^3 + 6*(B*c^2*d + A*c*d^2)*m^2 + 19*(B*c^2*d + A*c*d^2 + (B*c^2*d + A*c*d^2)*m)*n^2 + 2*(B*c^2*d + A*c*d^2)*m)*n^2 + 4*(B*c^2*d + A*c*d^2)*m + 8*(B*c^2*d + A*c*d^2 + (B*c^2*d + A*c*d^2)*m^3 + 3*(B*c^2*d + A*c*d^2)*m^2 + 3*(B*c^2*d + A*c*d^2)*m)*n)*x*x^(2*n)*e^(m*log(e) + m*log(x)) + ((B*c^3 + 3*A*c^2*d)*m^4 + B*c^3 + 3*A*c^2*d + 4*(B*c^3 + 3*A*c^2*d)*m^3 + 24*(B*c^3 + 3*A*c^2*d + (B*c^3 + 3*A*c^2*d)*m)*n^3 + 6*(B*c^3 + 3*A*c^2*d)*m^2 + 26*(B*c^3 + 3*A*c^2*d*d + (B*c^3 + 3*A*c^2*d)*m^2 + 2*(B*c^3 + 3*A*c^2*d)*m)*n^2 + 4*(B*c^3 + 3*A*c^2*d)*m + 9*(B*c^3 + 3*A*c^2*d + (B*c^3 + 3*A*c^2*d)*m^3 + 3*(B*c^3 + 3*A*c^2*d)*m^2 + 3*(B*c^3 + 3*A*c^2*d)*m)*n)*x*x^n*e^(m*log(e) + m*log(x)) + (A*c^3*m^4 + 24*A*c^3*n^4 + 4*A*c^3*m^3 + 6*A*c^3*m^2 + 4*A*c^3*m + A*c^3 + 50*(A*c^3*m + A*c^3)*n^3 + 35*(A*c^3*m^2 + 2*A*c^3*m + A*c^3)*n^2 + 10*(A*c^3*m^3 + 3*A*c^3*m^2 + 3*A*c^3*m + A*c^3)*n)*x*x^n*e^(m*log(e) + m*log(x)))/(m^5 + 24*(m + 1)*n^4 + 5*m^4 + 50*(m^2 + 2*m + 1)*n^3 + 10*m^3 + 35*(m^3 + 3*m^2 + 3*m + 1)*n^2 + 10*m^2 + 10*(m^4 + 4*m^3 + 6*m^2 + 4*m + 1)*n + 5*m + 1)
```

**giac [B]** time = 0.75, size = 2278, normalized size = 16.63

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="giac")
```

```
[Out] (B*d^3*m^4*x*x^m*x^(4*n)*e^m + 6*B*d^3*m^3*n*x*x^m*x^(4*n)*e^m + 11*B*d^3*m^2*n^2*x*x^m*x^(4*n)*e^m + 6*B*d^3*m*n^3*x*x^m*x^(4*n)*e^m + 3*B*c*d^2*m^4*x*x^m*x^(3*n)*e^m + A*d^3*m^4*x*x^m*x^(3*n)*e^m + 21*B*c*d^2*m^3*n*x*x^m*x^(3*n)*e^m + 7*A*d^3*m^3*n*x*x^m*x^(3*n)*e^m + 42*B*c*d^2*m^2*n^2*x*x^m*x^(3
```

$$\begin{aligned}
& *n) * e^m + 14 * A * d^3 * m^2 * n^2 * x^m * x^{(3*n)} * e^m + 24 * B * c * d^2 * m * n^3 * x^m * x^{(3*n)} * e^m \\
& + 8 * A * d^3 * m * n^3 * x^m * x^{(3*n)} * e^m + 3 * B * c^2 * d * m^4 * x^m * x^{(2*n)} * e^m \\
& + 3 * A * c * d^2 * m^4 * x^m * x^{(2*n)} * e^m + 24 * B * c^2 * d * m^3 * n * x^m * x^{(2*n)} * e^m + 24 \\
& * A * c * d^2 * m^3 * n * x^m * x^{(2*n)} * e^m + 57 * B * c^2 * d * m^2 * n^2 * x^m * x^{(2*n)} * e^m + 5 \\
& 7 * A * c * d^2 * m^2 * n^2 * x^m * x^{(2*n)} * e^m + 36 * B * c^2 * d * m * n^3 * x^m * x^{(2*n)} * e^m + \\
& 36 * A * c * d^2 * m * n^3 * x^m * x^{(2*n)} * e^m + B * c^3 * m^4 * x^m * x^n * e^m + 3 * A * c^2 * d * m^4 \\
& 4 * x^m * x^n * e^m + 9 * B * c^3 * m^3 * n * x^m * x^n * e^m + 27 * A * c^2 * d * m^3 * n * x^m * x^n * e^m \\
& + 26 * B * c^3 * m^2 * n^2 * x^m * x^n * e^m + 78 * A * c^2 * d * m^2 * n^2 * x^m * x^n * e^m + 2 \\
& 4 * B * c^3 * m * n^3 * x^m * x^n * e^m + 72 * A * c^2 * d * m * n^3 * x^m * x^n * e^m + A * c^3 * m^4 * x^m \\
& x^n * e^m + 10 * A * c^3 * m^3 * n * x^m * x^n * e^m + 35 * A * c^3 * m^2 * n^2 * x^m * x^n * e^m + 50 * A * c^3 * m \\
& m * n^3 * x^m * x^n * e^m + 24 * A * c^3 * m^4 * x^m * x^n * e^m + 4 * B * d^3 * m^3 * x^m * x^{(4*n)} * e^m + \\
& 18 * B * d^3 * m^2 * n * x^m * x^{(4*n)} * e^m + 22 * B * d^3 * m * n^2 * x^m * x^{(4*n)} * e^m + 6 * B * d \\
& ^3 * n^3 * x^m * x^{(4*n)} * e^m + 12 * B * c * d^2 * m^3 * x^m * x^{(3*n)} * e^m + 4 * A * d^3 * m^3 * x \\
& ^m * x^{(3*n)} * e^m + 63 * B * c * d^2 * m^2 * n * x^m * x^{(3*n)} * e^m + 21 * A * d^3 * m^2 * n * x^m * x^{(3*n)} * e^m \\
& + 84 * B * c * d^2 * m * n^2 * x^m * x^{(3*n)} * e^m + 28 * A * d^3 * m * n^2 * x^m * x^{(3*n)} * e^m + 24 * B * c * d^2 * n^3 \\
& * x^m * x^{(3*n)} * e^m + 8 * A * d^3 * n^3 * x^m * x^{(3*n)} * e^m + 12 * B * c^2 * d * m^3 * x^m * x^{(2*n)} * e^m + 12 * A * c * d^2 * m^3 \\
& * x^m * x^{(2*n)} * e^m + 72 * B * c^2 * d * m^2 * n * x^m * x^{(2*n)} * e^m + 72 * A * c * d^2 * m^2 * n * x^m * x^{(2*n)} * e^m + 1 \\
& 14 * B * c^2 * d * m * n^2 * x^m * x^{(2*n)} * e^m + 114 * A * c * d^2 * m * n^2 * x^m * x^{(2*n)} * e^m + 36 * B * c^2 * d * n^3 \\
& * x^m * x^{(2*n)} * e^m + 36 * A * c * d^2 * n^3 * x^m * x^{(2*n)} * e^m + 4 * B * c^3 * m^3 * x^m * x^n * e^m + 12 * A * c^2 * d * m^3 \\
& * x^m * x^n * e^m + 27 * B * c^3 * m^2 * n * x^m * x^n * e^m + 81 * A * c^2 * d * m^2 * n * x^m * x^n * e^m + 52 * B * c^3 * m * n^2 \\
& * x^m * x^n * e^m + 156 * A * c^2 * d * m * n^2 * x^m * x^n * e^m + 24 * B * c^3 * n^3 * x^m * x^n * e^m + 72 * A * c^2 * d * n^3 \\
& * x^m * x^n * e^m + 4 * A * c^3 * m^3 * x^m * x^n * e^m + 30 * A * c^3 * m^2 * n * x^m * x^n * e^m + 70 * A * c^3 * m * n^2 \\
& * x^m * x^n * e^m + 50 * A * c^3 * n^3 * x^m * x^n * e^m + 6 * B * d^3 * m^2 * x^m * x^{(4*n)} * e^m + 18 * B * d^3 * m * n * x^m \\
& * x^{(4*n)} * e^m + 11 * B * d^3 * n^2 * x^m * x^{(4*n)} * e^m + 18 * B * c * d^2 * m^2 * x^m * x^{(3*n)} * e^m + 6 * A * d^3 * m^2 \\
& * x^m * x^{(3*n)} * e^m + 63 * B * c * d^2 * m * n * x^m * x^{(3*n)} * e^m + 21 * A * d^3 * m * n * x^m * x^{(3*n)} * e^m + 42 * B * c * d^2 * n^2 \\
& * x^m * x^{(3*n)} * e^m + 14 * A * d^3 * n^2 * x^m * x^{(3*n)} * e^m + 18 * B * c^2 * d * m^2 * x^m * x^{(2*n)} * e^m + 18 * A * c * d^2 * m^2 \\
& * x^m * x^{(2*n)} * e^m + 72 * B * c^2 * d * m * n * x^m * x^{(2*n)} * e^m + 72 * A * c * d^2 * m * n * x^m * x^{(2*n)} * e^m + 57 * B * c^2 * d * n^2 \\
& * x^m * x^{(2*n)} * e^m + 57 * A * c * d^2 * n^2 * x^m * x^{(2*n)} * e^m + 6 * B * c^3 * m^2 * x^m * x^n * e^m + 18 * A * c^2 * d * m^2 * x^m \\
& * x^n * e^m + 27 * B * c^3 * m * n * x^m * x^n * e^m + 81 * A * c^2 * d * m * n * x^m * x^n * e^m + 26 * B * c^3 * n^2 * x^m * x^n * e^m \\
& + 78 * A * c^2 * d * n^2 * x^m * x^n * e^m + 6 * A * c^3 * m^2 * x^m * x^n * e^m + 30 * A * c^3 * m * n * x^m * x^n * e^m + 35 * A * c^3 * n^2 \\
& * x^m * x^n * e^m + 4 * B * d^3 * m * x^m * x^{(4*n)} * e^m + 6 * B * d^3 * n * x^m * x^{(4*n)} * e^m + 12 * B * c * d^2 * m * x^m * x^{(3*n)} * e^m \\
& + 4 * A * d^3 * m * x^m * x^{(3*n)} * e^m + 21 * B * c * d^2 * n * x^m * x^{(3*n)} * e^m + 7 * A * d^3 * n * x^m * x^{(3*n)} * e^m + 12 * B * c^2 * d * m * x^m * x^{(2*n)} * e^m \\
& + 12 * A * c * d^2 * m * x^m * x^{(2*n)} * e^m + 24 * B * c^2 * d * n * x^m * x^{(2*n)} * e^m + 24 * A * c * d^2 * n * x^m * x^{(2*n)} * e^m + 4 * B * c^3 * m * x^m * x^n * e^m \\
& + 12 * A * c^2 * d * m * x^m * x^n * e^m + 9 * B * c^3 * n * x^m * x^n * e^m + 27 * A * c^2 * d * n * x^m * x^n * e^m + 4 * A * c^3 * m * x^m * x^n * e^m + 10 * A * c^3 * n * x^m * x^n * e^m \\
& + B * d^3 * x^m * x^{(4*n)} * e^m + 3 * B * c * d^2 * x^m * x^{(3*n)} * e^m + A * d^3 * x^m * x^{(3*n)} * e^m + 3 * B * c^2 * d * x^m * x^{(2*n)} * e^m + 3 * A * c * d^2 * x^m * x^{(2*n)} * e^m + B * c^3 * x^m * x^n * e^m + 3 * A * c^2 * d * x^m * x^n * e^m + A * c^3 * x^m * x^n * e^m) / (m^5 + 10 * m^4 * n + 35 * m^3 * n^2 + 50 * m^2 * n^3 + 24 * m * n^4 + 5 * m^4 + 40 * m^3 * n + 105 * m^2 * n^2 + 100 * m * n^3 + 24 * n^4 + 10 * m^3 + 60 * m^2 * n + 105 * m * n^2 + 50 * n^3 + 10 * m^2 + 40 * m * n + 35 * n^2 + 5 * m + 10 * n + 1)
\end{aligned}$$

**maple [C]** time = 0.13, size = 1609, normalized size = 11.74

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(B*x^n+A)*(d*x^n+c)^3,x)$

[Out]  $x*(57*B*c^2*d*m^2*n^2*(x^n)^2+36*B*c^2*d*m*n^3*(x^n)^2+24*B*c^2*d*m^3*n*(x^n)^2+11*B*d^3*n^2*(x^n)^4+B*d^3*m^4*(x^n)^4+8*A*d^3*n^3*(x^n)^3+6*B*d^3*m^2*(x^n)^4+24*B*c^3*n^3*x^n+A*d^3*m^4*(x^n)^3+4*B*d^3*m^3*(x^n)^4+6*B*d^3*n^3*(x^n)^4+4*A*d^3*m^3*(x^n)^3+4*B*c^3*m^3*x^n+6*B*d^3*(x^n)^4*n+4*A*d^3*(x^n)^3*m+7*A*d^3*(x^n)^3*n+B*c^3*m^4*x^n+4*m*B*d^3*(x^n)^4+26*B*c^3*n^2*x^n+6*$

$A*d^3*m^2*(x^n)^3+14*A*d^3*n^2*(x^n)^3+3*A*c^2*d*x^n+3*B*c*d^2*(x^n)^3+3*A*c*d^2*(x^n)^2+4*B*c^3*x^n*m+9*B*c^3*x^n*n+6*B*c^3*m^2*x^n+3*B*c^2*d*(x^n)^2+10*A*c^3*m^3*n+35*A*c^3*m^2*n^2+50*A*c^3*m*n^3+30*A*c^3*m^2*n+70*A*c^3*m*n^2+30*A*c^3*m*n+36*A*c*d^2*m*n^3*(x^n)^2+24*A*c*d^2*m^3*n*(x^n)^2+57*A*c*d^2*m^2*n^2*(x^n)^2+72*B*c^2*d*m^2*n*(x^n)^2+114*B*c^2*d*m*n^2*(x^n)^2+63*B*c*d^2*m*n*(x^n)^3+21*B*c*d^2*m^3*n*(x^n)^3+42*B*c*d^2*m^2*n^2*(x^n)^3+24*B*c*d^2*m*n^3*(x^n)^3+84*B*c*d^2*m*n^2*(x^n)^3+27*A*c^2*d*m^3*n*x^n+78*A*c^2*d*m^2*n^2*x^n+72*A*c^2*d*m*n^3*x^n+72*A*c*d^2*m^2*n*(x^n)^2+114*A*c*d^2*m*n^2*(x^n)^2+81*A*c^2*d*m^2*n*x^n+156*A*c^2*d*m*n^2*x^n+72*A*c*d^2*m*n*(x^n)^2+72*B*c^2*d*m*n*(x^n)^2+63*B*c*d^2*m^2*n*(x^n)^3+81*A*c^2*d*m*n*x^n+A*c^3+(x^n)^4*B*d^3+(x^n)^3*A*d^3+12*B*c^2*d*m^3*(x^n)^2+36*B*c^2*d*n^3*(x^n)^2+4*A*c^3*m+10*A*c^3*n+24*A*c^3*n^4+4*A*c^3*m^3+50*A*c^3*n^3+6*A*c^3*m^2+35*A*c^3*n^2+x^n*B*c^3+A*c^3*m^4+72*A*c^2*d*n^3*x^n+18*A*c*d^2*m^2*(x^n)^2+57*A*c*d^2*n^2*(x^n)^2+27*B*c^3*m^2*n*x^n+18*B*c*d^2*m^2*(x^n)^3+3*A*c*d^2*m^4*(x^n)^2+21*A*d^3*m^2*n*(x^n)^3+28*A*d^3*m*n^2*(x^n)^3+3*B*c^2*d*m^4*(x^n)^2+26*B*c^3*m^2*n^2*x^n+7*A*d^3*m^3*n*(x^n)^3+14*A*d^3*m^2*n^2*(x^n)^3+8*A*d^3*m*n^3*(x^n)^3+3*B*c*d^2*m^4*(x^n)^3+18*B*d^3*m^2*n*(x^n)^4+22*B*d^3*m*n^2*(x^n)^4+78*A*c^2*d*n^2*x^n+12*A*c*d^2*(x^n)^2*m+24*A*c*d^2*(x^n)^2*n+27*B*c^3*m*n*x^n+12*B*c^2*d*(x^n)^2*m+24*B*c^2*d*(x^n)^2*n+12*A*c^2*d*x^n*m+27*A*c^2*d*x^n*n+42*B*c*d^2*n^2*(x^n)^3+12*A*c^2*d*m^3*x^n+18*B*d^3*m*n*(x^n)^4+3*A*c^2*d*m^4*x^n+12*A*c*d^2*m^3*(x^n)^2+36*A*c*d^2*n^3*(x^n)^2+21*A*d^3*m*n*(x^n)^3+9*B*c^3*m^3*n*x^n+24*B*c^3*m*n^3*x^n+12*B*c*d^2*m^3*(x^n)^3+24*B*c*d^2*n^3*(x^n)^3+6*B*d^3*m^3*n*(x^n)^4+11*B*d^3*m^2*n^2*(x^n)^4+6*B*d^3*m*n^3*(x^n)^4+52*B*c^3*m*n^2*x^n+18*B*c^2*d*m^2*(x^n)^2+57*B*c^2*d*n^2*(x^n)^2+12*B*c*d^2*(x^n)^3*m+21*B*c*d^2*(x^n)^3*n+18*A*c^2*d*m^2*x^n)/(m+1)/(m+n+1)/(m+2*n+1)/(m+3*n+1)/(m+4*n+1)*exp(1/2*(-I*Pi*csgn(I*e)*csgn(I*x)*csgn(I*e*x)+I*Pi*csgn(I*e)*csgn(I*e*x)^2+I*Pi*csgn(I*x)*csgn(I*e*x)^2-I*Pi*csgn(I*e*x)^3+2*ln(e)+2*ln(x))*m)$

**maxima [A]** time = 0.84, size = 219, normalized size = 1.60

$$\frac{Bd^3e^{m \ln(x)+4n \ln(x)}}{m+4n+1} + \frac{3Bcd^2e^{m \ln(x)+3n \ln(x)}}{m+3n+1} + \frac{Ad^3e^{m \ln(x)+3n \ln(x)}}{m+3n+1} + \frac{3Bc^2de^{m \ln(x)+2n \ln(x)}}{m+2n+1} + \frac{3Ac^2de^{m \ln(x)+2n \ln(x)}}{m+2n+1} + \frac{Bc^3e^{m \ln(x)+n \ln(x)}}{m+n+1} + \frac{3Ac^2de^{m \ln(x)+n \ln(x)}}{m+n+1} + \frac{(ex)^{m+1}Ac^3}{e(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="maxima")
[Out] B*d^3*e^m*x*e^(m*log(x) + 4*n*log(x))/(m + 4*n + 1) + 3*B*c*d^2*e^m*x*e^(m*log(x) + 3*n*log(x))/(m + 3*n + 1) + A*d^3*e^m*x*e^(m*log(x) + 3*n*log(x))/(m + 3*n + 1) + 3*B*c^2*d*e^m*x*e^(m*log(x) + 2*n*log(x))/(m + 2*n + 1) + 3*A*c*d^2*e^m*x*e^(m*log(x) + 2*n*log(x))/(m + 2*n + 1) + B*c^3*e^m*x*e^(m*log(x) + n*log(x))/(m + n + 1) + 3*A*c^2*d*e^m*x*e^(m*log(x) + n*log(x))/(m + n + 1) + (e*x)^(m + 1)*A*c^3/(e*(m + 1))
```

**mupad [B]** time = 5.31, size = 563, normalized size = 4.11

$$\frac{A^3d^3e^{m \ln(x)+4n \ln(x)}}{m+4n+1} + \frac{3Bcd^2e^{m \ln(x)+3n \ln(x)}}{m+3n+1} + \frac{Ad^3e^{m \ln(x)+3n \ln(x)}}{m+3n+1} + \frac{3Bc^2de^{m \ln(x)+2n \ln(x)}}{m+2n+1} + \frac{3Ac^2de^{m \ln(x)+2n \ln(x)}}{m+2n+1} + \frac{Bc^3e^{m \ln(x)+n \ln(x)}}{m+n+1} + \frac{3Ac^2de^{m \ln(x)+n \ln(x)}}{m+n+1} + \frac{(ex)^{m+1}Ac^3}{e(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(A + B*x^n)*(c + d*x^n)^3,x)
[Out] (A*c^3*x*(e*x)^m)/(m + 1) + (d^2*x*x^(3*n)*(e*x)^m*(A*d + 3*B*c)*(3*m + 7*n + 14*m*n + 14*m*n^2 + 7*m^2*n + 3*m^2 + m^3 + 14*n^2 + 8*n^3 + 1))/(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1) + (c^2*x*x^n*(e*x)^m*(3*A*d + B*c)*(3*m + 9*n + 18*m*n + 26*m*n^2 + 9*m^2*n + 3*m^2 + m^3 + 26*n^2 + 24*n^3 + 1))/(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1) + (B*d^3*x*x^(4*n)*(e*x)^m*(3*m + 6*n + 12*m*n + 11*m*n^2 + 6*m^2*n + 3*m^2 + m^3 + 11*n^2 + 6*n^3 + 1))/(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m
```

$$\frac{(n^3 + 10m^3n + 6m^2 + 4m^3 + m^4 + 35n^2 + 50n^3 + 24n^4 + 35m^2n^2 + 1) + (3cdx^2x^{2n})(e^x)^m(A*d + B*c)(3m + 8n + 16mn + 19m^2n^2 + 8m^2n + 3m^2 + m^3 + 19n^2 + 12n^3 + 1)}{(4m + 10n + 30mn + 70m^2n^2 + 30m^2n + 50mn^3 + 10m^3n + 6m^2 + 4m^3 + m^4 + 35n^2 + 50n^3 + 24n^4 + 35m^2n^2 + 1)}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*3,x)

[Out] Timed out





# Chapter 4

## Appendix

### Local contents

4.1	Download section . . . . .	122
4.2	Listing of Grading functions . . . . .	122

## 4.1 Download section

The following zip files contain the raw integrals used in this test.

This is a subset of Rubi test suite thanks to Albert Rich, which includes only the algebraic integrals with elementray optimal antiderivatives. It also includes a subset of a test file provided thanks to Sam Blake.

**Mathematica format** Mathematica\_syntax\_CAS\_integration\_elementary\_version.zip

**Maple and Mupad format** Maple\_syntax\_CAS\_integration\_elementary\_version.zip

**Sympy format** SYMPY\_syntax\_CAS\_integration\_elementary\_version.zip

**Sage math format** SAGE\_syntax\_CAS\_integration\_elementary\_version.zip

## 4.2 Listing of Grading functions

The following are the current version of the grading functions used for grading the quality of the antiderivative with reference to the optimal antiderivative included in the test suite.

There is a version for Maple and for Mathematica/Rubi. There is a version for grading Sympy and version for use with Sagemath.

The following are links to the current source code.

The following are the listings of source code of the grading functions.

### 4.2.1 Mathematica and Rubi grading function

```
(* Original version thanks to Albert Rich emailed on 03/21/2017 *)
(* ::Package:: *)

(* ::Subsection:: *)
(*GradeAntiderivative[result,optimal]*)

(* ::Text:: *)
(*If result and optimal are mathematical expressions, *)
(*      GradeAntiderivative[result,optimal] returns*)
(* "F" if the result fails to integrate an expression that*)
(*      is integrable*)
(* "C" if result involves higher level functions than necessary*)
(* "B" if result is more than twice the size of the optimal*)
(*      antiderivative*)
(* "A" if result can be considered optimal*)

GradeAntiderivative[result_,optimal_] :=
  If[ExpnType[result]<=ExpnType[optimal],
    If[FreeQ[result,Complex] || Not[FreeQ[optimal,Complex]],
      If[LeafCount[result]<=2*LeafCount[optimal],
        "A",
        "B"],
      "C"],
    If[FreeQ[result,Integrate] && FreeQ[result,Int],
      "C",
      "F"]]

(* ::Text:: *)
(*The following summarizes the type number assigned an *)
(*expression based on the functions it involves*)
(*1 = rational function*)
```

```

(*2 = algebraic function*)
(*3 = elementary function*)
(*4 = special function*)
(*5 = hyperpergeometric function*)
(*6 = appell function*)
(*7 = rootsum function*)
(*8 = integrate function*)
(*9 = unknown function*)

ExpnType[expn_] :=
  If[AtomQ[expn],
    1,
  If[ListQ[expn],
    Max[Map[ExpnType, expn]],
  If[Head[expn]===Power,
    If[IntegerQ[expn[[2]]],
      ExpnType[expn[[1]]],
    If[Head[expn[[2]]]===Rational,
      If[IntegerQ[expn[[1]]] || Head[expn[[1]]]===Rational,
        1,
        Max[ExpnType[expn[[1]], 2]],
      Max[ExpnType[expn[[1]], ExpnType[expn[[2]], 3]]],
  If[Head[expn]===Plus || Head[expn]===Times,
    Max[ExpnType[First[expn]], ExpnType[Rest[expn]]],
  If[ElementaryFunctionQ[Head[expn]],
    Max[3, ExpnType[expn[[1]]]],
  If[SpecialFunctionQ[Head[expn]],
    Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 4]],
  If[HypergeometricFunctionQ[Head[expn]],
    Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 5]],
  If[AppellFunctionQ[Head[expn]],
    Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 6]],
  If[Head[expn]===RootSum,
    Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 7]],
  If[Head[expn]===Integrate || Head[expn]===Int,
    Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 8]],
  9]]]]]]]]]]

ElementaryFunctionQ[func_] :=
  MemberQ[{
    Exp, Log,
    Sin, Cos, Tan, Cot, Sec, Csc,
    ArcSin, ArcCos, ArcTan, ArcCot, ArcSec, ArcCsc,
    Sinh, Cosh, Tanh, Coth, Sech, Csch,
    ArcSinh, ArcCosh, ArcTanh, ArcCoth, ArcSech, ArcCsch
  }, func]

SpecialFunctionQ[func_] :=
  MemberQ[{
    Erf, Erfc, Erfi,
    FresnelS, FresnelC,
    ExpIntegralE, ExpIntegralEi, LogIntegral,
    SinIntegral, CosIntegral, SinhIntegral, CoshIntegral,
    Gamma, LogGamma, PolyGamma,
    Zeta, PolyLog, ProductLog,
    EllipticF, EllipticE, EllipticPi
  }, func]

HypergeometricFunctionQ[func_] :=

```

```
MemberQ[{Hypergeometric1F1,Hypergeometric2F1,HypergeometricPFQ},func]
```

```
AppellFunctionQ[func_] :=
  MemberQ[{AppellF1},func]
```

## 4.2.2 Maple grading function

```
# File: GradeAntiderivative.mpl
# Original version thanks to Albert Rich emailed on 03/21/2017

#Nasser 03/22/2017 Use Maple leaf count instead since buildin
#Nasser 03/23/2017 missing 'ln' for ElementaryFunctionQ added
#Nasser 03/24/2017 corrected the check for complex result
#Nasser 10/27/2017 check for leafsize and do not call ExpnType()
#                    if leaf size is "too large". Set at 500,000
#Nasser 12/22/2019 Added debug flag, added 'dilog' to special functions
#                    see problem 156, file Apostol_Problems

GradeAntiderivative := proc(result,optimal)
local leaf_count_result, leaf_count_optimal,ExpnType_result,ExpnType_optimal,
    debug:=false;

    leaf_count_result:=leafcount(result);
    #do NOT call ExpnType() if leaf size is too large. Recursion problem
    if leaf_count_result > 500000 then
        return "B";
    fi;

    leaf_count_optimal:=leafcount(optimal);

    ExpnType_result:=ExpnType(result);
    ExpnType_optimal:=ExpnType(optimal);

    if debug then
        print("ExpnType_result",ExpnType_result," ExpnType_optimal=",
ExpnType_optimal);
    fi;

# If result and optimal are mathematical expressions,
# GradeAntiderivative[result,optimal] returns
# "F" if the result fails to integrate an expression that
# is integrable
# "C" if result involves higher level functions than necessary
# "B" if result is more than twice the size of the optimal
# antiderivative
# "A" if result can be considered optimal

#This check below actually is not needed, since I only
#call this grading only for passed integrals. i.e. I check
#for "F" before calling this. But no harm of keeping it here.
#just in case.

if not type(result,freeof('int')) then
    return "F";
end if;

if ExpnType_result<=ExpnType_optimal then
    if debug then
        print("ExpnType_result<=ExpnType_optimal");
    fi;
end if;
```

```

if is_contains_complex(result) then
  if is_contains_complex(optimal) then
    if debug then
      print("both result and optimal complex");
    fi;
    #both result and optimal complex
    if leaf_count_result<=2*leaf_count_optimal then
      return "A";
    else
      return "B";
    end if
  else #result contains complex but optimal is not
    if debug then
      print("result contains complex but optimal is not");
    fi;
    return "C";
  end if
else # result do not contain complex
  # this assumes optimal do not as well
  if debug then
    print("result do not contain complex, this assumes optimal do
not as well");
  fi;
  if leaf_count_result<=2*leaf_count_optimal then
    if debug then
      print("leaf_count_result<=2*leaf_count_optimal");
    fi;
    return "A";
  else
    if debug then
      print("leaf_count_result>2*leaf_count_optimal");
    fi;
    return "B";
  end if
end if
else #ExpnType(result) > ExpnType(optimal)
  if debug then
    print("ExpnType(result) > ExpnType(optimal)");
  fi;
  return "C";
end if

end proc:

#
# is_contains_complex(result)
# takes expressions and returns true if it contains "I" else false
#
#Nasser 032417
is_contains_complex:= proc(expression)
  return (has(expression,I));
end proc:

# The following summarizes the type number assigned an expression
# based on the functions it involves
# 1 = rational function
# 2 = algebraic function
# 3 = elementary function
# 4 = special function
# 5 = hyperpergeometric function
# 6 = appell function
# 7 = rootsum function
# 8 = integrate function

```

```

# 9 = unknown function

ExpnType := proc(expn)
  if type(expn,'atomic') then
    1
  elif type(expn,'list') then
    apply(max,map(ExpnType,expn))
  elif type(expn,'sqrt') then
    if type(op(1,expn),'rational') then
      1
    else
      max(2,ExpnType(op(1,expn)))
    end if
  elif type(expn,'^^') then
    if type(op(2,expn),'integer') then
      ExpnType(op(1,expn))
    elif type(op(2,expn),'rational') then
      if type(op(1,expn),'rational') then
        1
      else
        max(2,ExpnType(op(1,expn)))
      end if
    else
      max(3,ExpnType(op(1,expn)),ExpnType(op(2,expn)))
    end if
  elif type(expn,'`+`') or type(expn,'`*`') then
    max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
  elif ElementaryFunctionQ(op(0,expn)) then
    max(3,ExpnType(op(1,expn)))
  elif SpecialFunctionQ(op(0,expn)) then
    max(4,apply(max,map(ExpnType,[op(expn)])))
  elif HypergeometricFunctionQ(op(0,expn)) then
    max(5,apply(max,map(ExpnType,[op(expn)])))
  elif AppellFunctionQ(op(0,expn)) then
    max(6,apply(max,map(ExpnType,[op(expn)])))
  elif op(0,expn)='int' then
    max(8,apply(max,map(ExpnType,[op(expn)]))) else
    9
  end if
end proc:

ElementaryFunctionQ := proc(func)
  member(func,[
    exp,log,ln,
    sin,cos,tan,cot,sec,csc,
    arcsin,arccos,arctan,arccot,arcsec,arccsc,
    sinh,cosh,tanh,coth,sech,csch,
    arcsinh,arccosh,arctanh,arccoth,arcsech,arccsch])
end proc:

SpecialFunctionQ := proc(func)
  member(func,[
    erf,erfc,erfi,
    FresnelS,FresnelC,
    Ei,Ei,Li,Si,Ci,Shi,Chi,
    GAMMA,lnGAMMA,Psi,Zeta,polylog,dilog,LambertW,
    EllipticF,EllipticE,EllipticPi])
end proc:

HypergeometricFunctionQ := proc(func)
  member(func,[Hypergeometric1F1,hypergeom,HypergeometricPFQ])
end proc:

```

```

AppellFunctionQ := proc(func)
  member(func,[AppellF1])
end proc:

# u is a sum or product. rest(u) returns all but the
# first term or factor of u.
rest := proc(u) local v;
  if nops(u)=2 then
    op(2,u)
  else
    apply(op(0,u),op(2..nops(u),u))
  end if
end proc:

#leafcount(u) returns the number of nodes in u.
#Nasser 3/23/17 Replaced by build-in leafCount from package in Maple
leafcount := proc(u)
  MmaTranslator[Mma][LeafCount](u);
end proc:

```

### 4.2.3 Sympy grading function

```

#Dec 24, 2019. Nasser M. Abbasi:
#           Port of original Maple grading function by
#           Albert Rich to use with Sympy/Python
#Dec 27, 2019 Nasser. Added `RootSum`. See problem 177, Timofeev file
#           added 'exp_polar'
from sympy import *

def leaf_count(expr):
  #sympy do not have leaf count function. This is approximation
  return round(1.7*count_ops(expr))

def is_sqrt(expr):
  if isinstance(expr,Pow):
    if expr.args[1] == Rational(1,2):
      return True
    else:
      return False
  else:
    return False

def is_elementary_function(func):
  return func in [exp,log,ln,sin,cos,tan,cot,sec,csc,
                 asin,acos,atan,acot,asec,acsc,sinh,cosh,tanh,coth,sech,csch,
                 asinh,acosh,atanh,acoth,asech,acsch
                 ]

def is_special_function(func):
  return func in [ erf,erfc,erfi,
                 fresnels,fresnelc,Ei,Ei,Li,Si,Ci,Shi,Chi,
                 gamma,loggamma,digamma,zeta,polylog,LambertW,
                 elliptic_f,elliptic_e,elliptic_pi,exp_polar
                 ]

def is_hypergeometric_function(func):
  return func in [hyper]

def is_appell_function(func):
  return func in [appellf1]

def is_atom(expn):

```

```

try:
    if expn.isAtom or isinstance(expn,int) or isinstance(expn,float):
        return True
    else:
        return False

except AttributeError as error:
    return False

def expnType(expn):
    debug=False
    if debug:
        print("expn=",expn,"type(expn)=",type(expn))

    if is_atom(expn):
        return 1
    elif isinstance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
            return 1
        else:
            return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
    elif isinstance(expn,Pow): #type(expn,'^^')
        if isinstance(expn.args[1],Integer): #type(op(2,expn),'integer')
            return expnType(expn.args[0]) #ExpnType(op(1,expn))
        elif isinstance(expn.args[1],Rational): #type(op(2,expn),'rational')
            if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
                return 1
            else:
                return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
    elif isinstance(expn,Add) or isinstance(expn,Mul): #type(expn,'^+^') or
    type(expn,'*^')
        m1 = expnType(expn.args[0])
        m2 = expnType(list(expn.args[1:]))
        return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
    elif is_elementary_function(expn.func): #ElementaryFunctionQ(op(0,expn))
        return max(3,expnType(expn.args[0])) #max(3,ExpnType(op(1,expn)))
    elif is_special_function(expn.func): #SpecialFunctionQ(op(0,expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(4,m1) #max(4,apply(max,map(ExpnType,[op(expn)])))
    elif is_hypergeometric_function(expn.func): #HypergeometricFunctionQ(op(0,
    expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(5,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif is_appell_function(expn.func):
        m1 = max(map(expnType, list(expn.args)))
        return max(6,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif isinstance(expn,RootSum):
        m1 = max(map(expnType, list(expn.args))) #Apply[Max,Append[Map[ExpnType
    ,Apply[List,expn]],7]],
        return max(7,m1)
    elif str(expn).find("Integral") != -1:
        m1 = max(map(expnType, list(expn.args)))
        return max(8,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    else:
        return 9

#main function

```



```

def grade_antiderivative(result,optimal):

    leaf_count_result = leaf_count(result)
    leaf_count_optimal = leaf_count(optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

    if str(result).find("Integral") != -1:
        return "F"

    if expnType_result <= expnType_optimal:
        if result.has(I):
            if optimal.has(I): #both result and optimal complex
                if leaf_count_result <= 2*leaf_count_optimal:
                    return "A"
                else:
                    return "B"
            else: #result contains complex but optimal is not
                return "C"
        else: # result do not contain complex, this assumes optimal do not as
well
            if leaf_count_result <= 2*leaf_count_optimal:
                return "A"
            else:
                return "B"
    else:
        return "C"

```

#### 4.2.4 SageMath grading function

```

#Dec 24, 2019. Nasser: Ported original Maple grading function by
#           Albert Rich to use with Sagemath. This is used to
#           grade Fracas, Giac and Maxima results.
#Dec 24, 2019. Nasser: Added 'exp_integral_e' and 'sng', 'sin_integral'
#           'arctan2','floor','abs','log_integral'

from sage.all import *
from sage.symbolic.operators import add_vararg, mul_vararg

debug=False;

def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)

def is_sqrt(expr):
    if expr.operator() == operator.pow: # isinstance(expr,Pow):
        if expr.operands()[1]==1/2: #expr.args[1] == Rational(1,2):
            if debug: print ("expr is sqrt")
            return True
        else:
            return False

```

```

else:
    return False

def is_elementary_function(func):
    debug=False
    m = func.name() in ['exp','log','ln',
        'sin','cos','tan','cot','sec','csc',
        'arcsin','arccos','arctan','arccot','arcsec','arccsc',
        'sinh','cosh','tanh','coth','sech','csch',
        'arcsinh','arccosh','arctanh','arccoth','arcsech','arccsch','sgn',
        'arctan2','floor','abs'
    ]
    if debug:
        if m:
            print ("func ", func , " is elementary_function")
        else:
            print ("func ", func , " is NOT elementary_function")

    return m

def is_special_function(func):
    debug=False
    if debug: print ("type(func)=", type(func))

    m= func.name() in ['erf','erfc','erfi','fresnel_sin','fresnel_cos','Ei',
        'Ei','Li','Si','sin_integral','Ci','cos_integral','Shi','
sinh_integral'
        'Chi','cosh_integral','gamma','log_gamma','psi,zeta',
        'polylog','lambert_w','elliptic_f','elliptic_e',
        'elliptic_pi','exp_integral_e','log_integral']

    if debug:
        print ("m=",m)
        if m:
            print ("func ", func ," is special_function")
        else:
            print ("func ", func ," is NOT special_function")

    return m

def is_hypergeometric_function(func):
    return func.name() in ['hypergeometric','hypergeometric_M',
        hypergeometric_U']

def is_appell_function(func):
    return func.name() in ['hypergeometric']    #[appellf1] can't find this in
    sagemath

def is_atom(expn):

    debug=False
    if debug: print ("Enter is_atom")

    #thanks to answer at https://ask.sagemath.org/question/49179/what-is-
    sagemath-equivalent-to-atomic-type-in-maple/
    try:
        if expn.parent() is SR:
            return expn.operator() is None
        if expn.parent() in (ZZ, QQ, AA, QQbar):

```

```

        return expn in expn.parent() # Should always return True
        if hasattr(expn.parent(),"base_ring") and hasattr(expn.parent(),"gens")
:
            return expn in expn.parent().base_ring() or expn in expn.parent().
gens()
        return False

    except AttributeError as error:
        return False

def expnType(expn):

    if debug:
        print (">>>>>Enter expnType, expn=", expn)
        print (">>>>>is_atom(expn)=", is_atom(expn))

    if is_atom(expn):
        return 1
    elif type(expn)==list: #isinstance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if type(expn.operands()[0])==Rational: #type(isinstance(expn.args[0],
Rational):
            return 1
        else:
            return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.
args[0]))
    elif expn.operator() == operator.pow: #isinstance(expn,Pow)
        if type(expn.operands()[1])==Integer: #isinstance(expn.args[1],Integer
)
            return expnType(expn.operands()[0]) #expnType(expn.args[0])
        elif type(expn.operands()[1])==Rational: #isinstance(expn.args[1],
Rational)
            if type(expn.operands()[0])==Rational: #isinstance(expn.args[0],
Rational)
                return 1
            else:
                return max(2,expnType(expn.operands()[0])) #max(2,expnType(
expn.args[0]))
        else:
            return max(3,expnType(expn.operands()[0]),expnType(expn.operands()
[1])) #max(3,expnType(expn.operands()[0]),expnType(expn.operands()[1]))
    elif expn.operator() == add_vararg or expn.operator() == mul_vararg: #
isinstance(expn,Add) or isinstance(expn,Mul)
        m1 = expnType(expn.operands()[0]) #expnType(expn.args[0])
        m2 = expnType(expn.operands()[1:]) #expnType(list(expn.args[1:]))
        return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn)))
    elif is_elementary_function(expn.operator()): #is_elementary_function(expn
.func)
        return max(3,expnType(expn.operands()[0]))
    elif is_special_function(expn.operator()): #is_special_function(expn.func)
        m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))
        return max(4,m1) #max(4,m1)
    elif is_hypergeometric_function(expn.operator()): #
is_hypergeometric_function(expn.func)
        m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))
        return max(5,m1) #max(5,m1)
    elif is_appell_function(expn.operator()):
        m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))

```

```

    return max(6,m1)    #max(6,m1)
elif str(expn).find("Integral") != -1: #this will never happen, since it
    #is checked before calling the grading function that is passed.
    #but kept it here.
    m1 = max(map(expnType, expn.operands()))    #max(map(expnType, list(
expn.args)))
    return max(8,m1)    #max(5,apply(max,map(ExpnType,[op(expn)])))
else:
    return 9

#main function
def grade_antiderivative(result,optimal):

    if debug: print ("Enter grade_antiderivative for sagemath")

    leaf_count_result = tree_size(result) #leaf_count(result)
    leaf_count_optimal = tree_size(optimal) #leaf_count(optimal)

    if debug: print ("leaf_count_result=", leaf_count_result, "
leaf_count_optimal=",leaf_count_optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

    if debug: print ("expnType_result=", expnType_result, "expnType_optimal=",
expnType_optimal)

    if expnType_result <= expnType_optimal:
        if result.has(I):
            if optimal.has(I): #both result and optimal complex
                if leaf_count_result <= 2*leaf_count_optimal:
                    return "A"
                else:
                    return "B"
            else: #result contains complex but optimal is not
                return "C"
        else: # result do not contain complex, this assumes optimal do not as
well
            if leaf_count_result <= 2*leaf_count_optimal:
                return "A"
            else:
                return "B"
    else:
        return "C"

```